

MATHEMATICS DEPARTMENT  
Stat2361 Worksheet#3

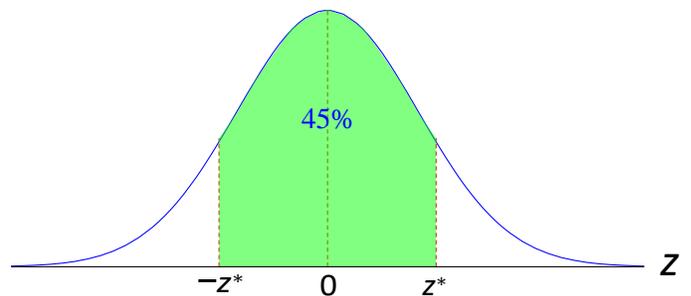
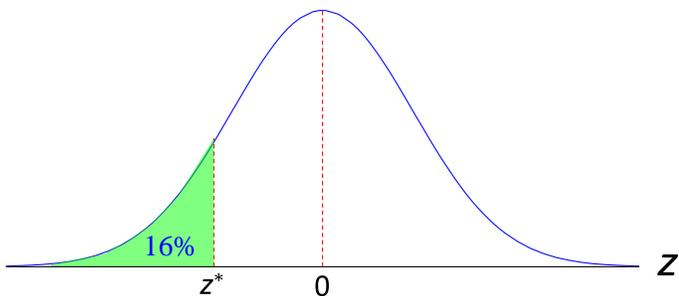
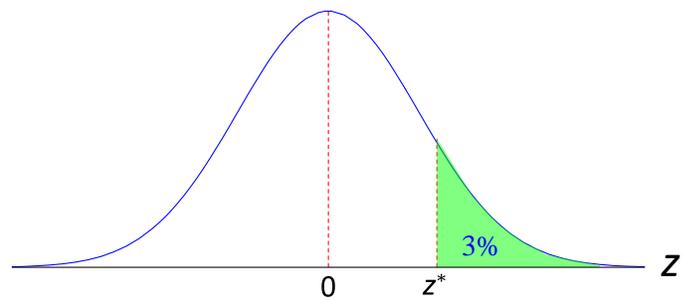
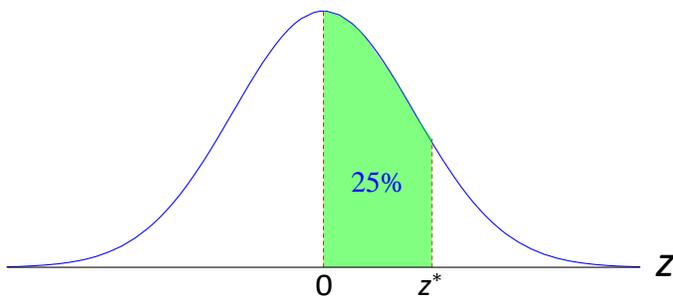
• Name.....

• Rasha Shadid

**(Q1)** Assume that  $z$  is a standard normal random variable. Find  $z$  in the following situations.

- (1) The area to the left of  $z$  is 0.9750
- (2) The area to the left of  $z$  is 0.9000
- (3) The area to the left of  $z$  is 0.9900
- (4) The area to the left of  $z$  is 0.9500
- (5) The area to the left of  $z$  is 0.1151
- (6) The area to the left of  $z$  is 0.2200
- (7) The area to the right of  $z$  is 0.0400
- (8) The area to the right of  $z$  is 0.8700
- (9) The area between 0 and  $z$  is 0.3210
- (10) The area between  $-z$  and  $z$  is 0.7500

**(Q2)** Find  $z^*$  in each situation below.



**(Q3)** Let  $x$  be a normally distributed variable with  $\mu = 120$  and  $\sigma = 12$

- (1) Find the z-score of  $x = 124$
- (2) Find  $x$  if  $z = -2.67$
- (3) Find the probability that  $x$  is at least 110
- (4) Find the percentage of  $x$  between 100 and 135
- (5) Find the minimum  $x$  in the top (upper) 10%
- (6) Find the maximum  $x$  in the bottom (lower) 20%
- (7) Find the range of  $x$  in the middle 85%

**(Q4)** A coin is tossed 7 times. What is the probability of getting exactly two heads?

**(Q5)** It is known that 30% of tennis players are left-handed.

- (1) In a sample of 8 players, what is the probability that two players are left-handed?
- (2) In a sample of 10 players, what is the probability that more than one player is left-handed?
- (3) In a sample of 20 players, what is the expected number of left-handed players?
- (4) In a sample of 6 players, what is the probability that all of them are right-handed?

**(Q6)** The students of BZU consume on average 2.68 cups of coffee per day. Suppose that the consumption of coffee is normally distributed with a standard deviation of 0.94

- (1) What is the probability that a randomly student drinks at most one cup of coffee?
- (2) What is the percentage of students who drink between two and four cups of coffee?
- (3) If 500 students are selected, approximately how many drink more than three cups of coffee?

**(Q7)** The grades of BZU students in Stat2361 are usually normally distributed with average of 71 and standard deviation of 11.6

- (1) What is the probability that a student's grade will exceed 95?
- (2) What is the percentage of students who will pass this course?
- (3) Find the 90th percentile.
- (4) A grade in the bottom 25% is considered "hopeless", what is a "hopeless" grade?

**(Q8)** If the number of baby deliveries in Ramallah's hospital is known to be Poisson distributed with an average of 2 babies per day

- (1) What is the probability that 12 babies will be delivered in a week?
- (2) What is the probability that at least two babies will be delivered in a day?
- (3) What is the probability that at most one baby will be delivered in a day?
- (4) What is the expected number of baby deliveries in a month?

(5) What is the standard deviation of the number of baby deliveries in two weeks?

**(Q9)** Assume a random sample of size 15 has a mean of 58.60 and a standard deviation of 7.54

- (1) Construct a 90% confidence interval for the population mean. Interpret your result.
- (2) Construct a 95% confidence interval for the population mean. Interpret your result.
- (3) Construct a 99% confidence interval for the population mean. Interpret your result.

**(Q10)** If the interval [30, 42] is a 95% confidence interval for  $\mu$

- (1) Find the sample mean.
- (2) Find the margin of error.
- (3) Find  $t_{\alpha/2}$  if the sample size is 24

**(Q11)** Use the  $t$  table to find the following values.

- (1)  $z_{\alpha/2}$ , for a 98% confidence interval.
- (2)  $t_{\alpha/2}$ , for a 98% confidence interval, given that  $n = 28$

**(Q12)** A researcher found that in a sample of 50 retired men, the average number of jobs they had in their lifetimes is 7.20. Assuming that the population standard deviation is 2.10, find the 95% confidence interval of the mean number of jobs. Then interpret your result.

**(Q13)** A health magazine is interested in the noise level (in decibels) at urban hospitals. A simplerandom sample of size 20 was taken. In this sample, the mean was 41.60 and the standard deviation was 7.50. Find the 95% confidence interval for the true mean noise level.

**(Q14)** What happens to the margin of error and the confidence interval of  $\mu$  in the following cases?

- (1) If the confidence level decreases.
- (2) If the sample size decreases.