
Web: Search, Web Size Estimate, Ads and Duplicates Removal

Web Search History

- In 1993, early web robots (spiders) were built to collect URL's:
 - Wanderer
 - ALIWEB (Archie-Like Index of the WEB)
 - WWW Worm (indexed URL's and titles for regex search)
- In 1994, Stanford grad students David Filo and Jerry Yang started manually collecting popular web sites into a topical hierarchy called Yahoo.

Web Search History (cont)

- In early 1994, Brian Pinkerton developed WebCrawler as a class project at U Wash. (eventually became part of Excite and AOL).
- A few months later, Fuzzy Maudlin, a grad student at CMU developed Lycos. First to use a standard IR system as developed for the DARPA Tipster project. First to index a large set of pages.
- In late 1995, DEC developed Altavista. Used a large farm of Alpha machines to quickly process large numbers of queries. Supported boolean operators, phrases, and “reverse pointer” queries.

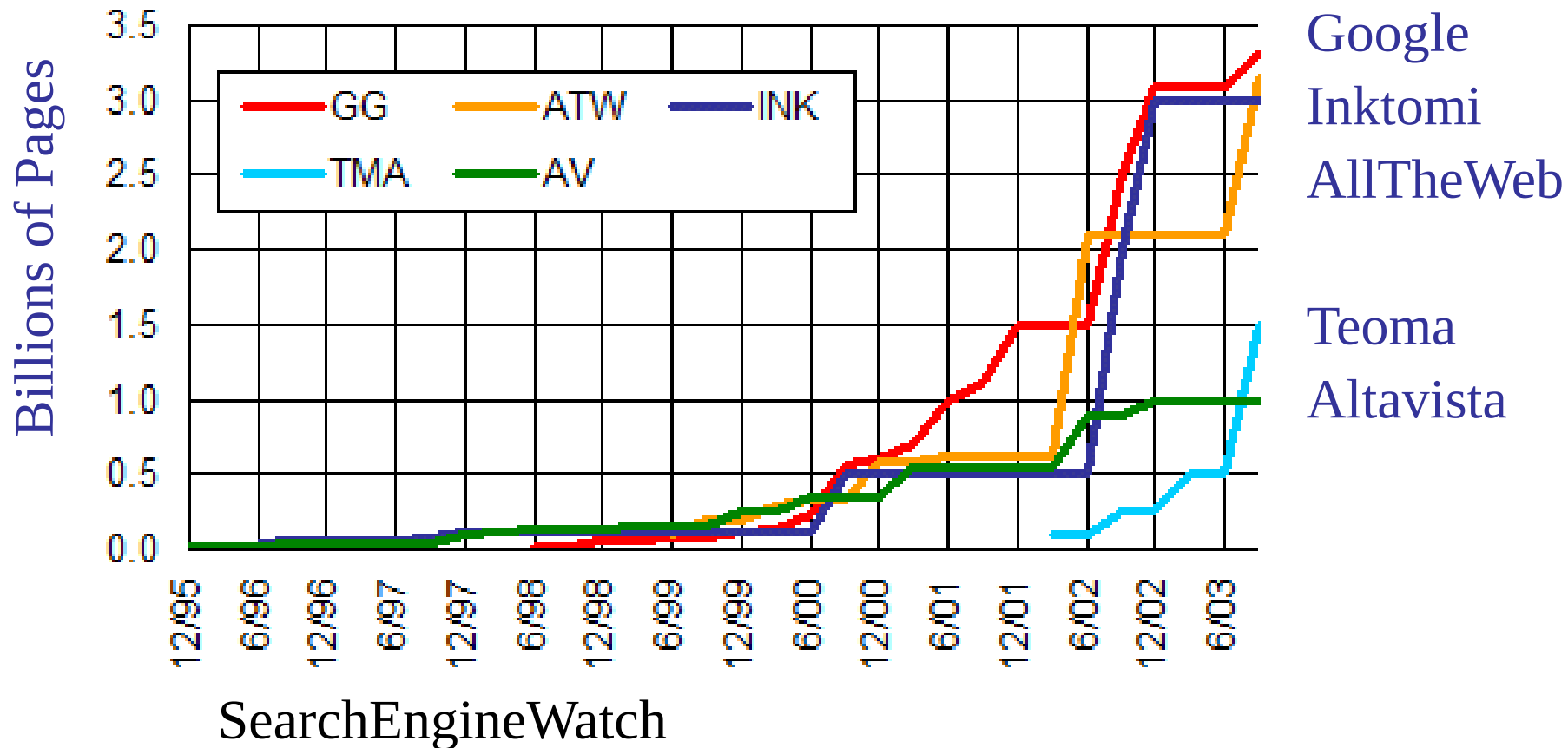
Web Search Recent History

- In 1998, Larry Page and Sergey Brin, Ph.D. students at Stanford, started Google. Main advance is use of *link analysis* to rank results partially based on authority.

Web Challenges for IR

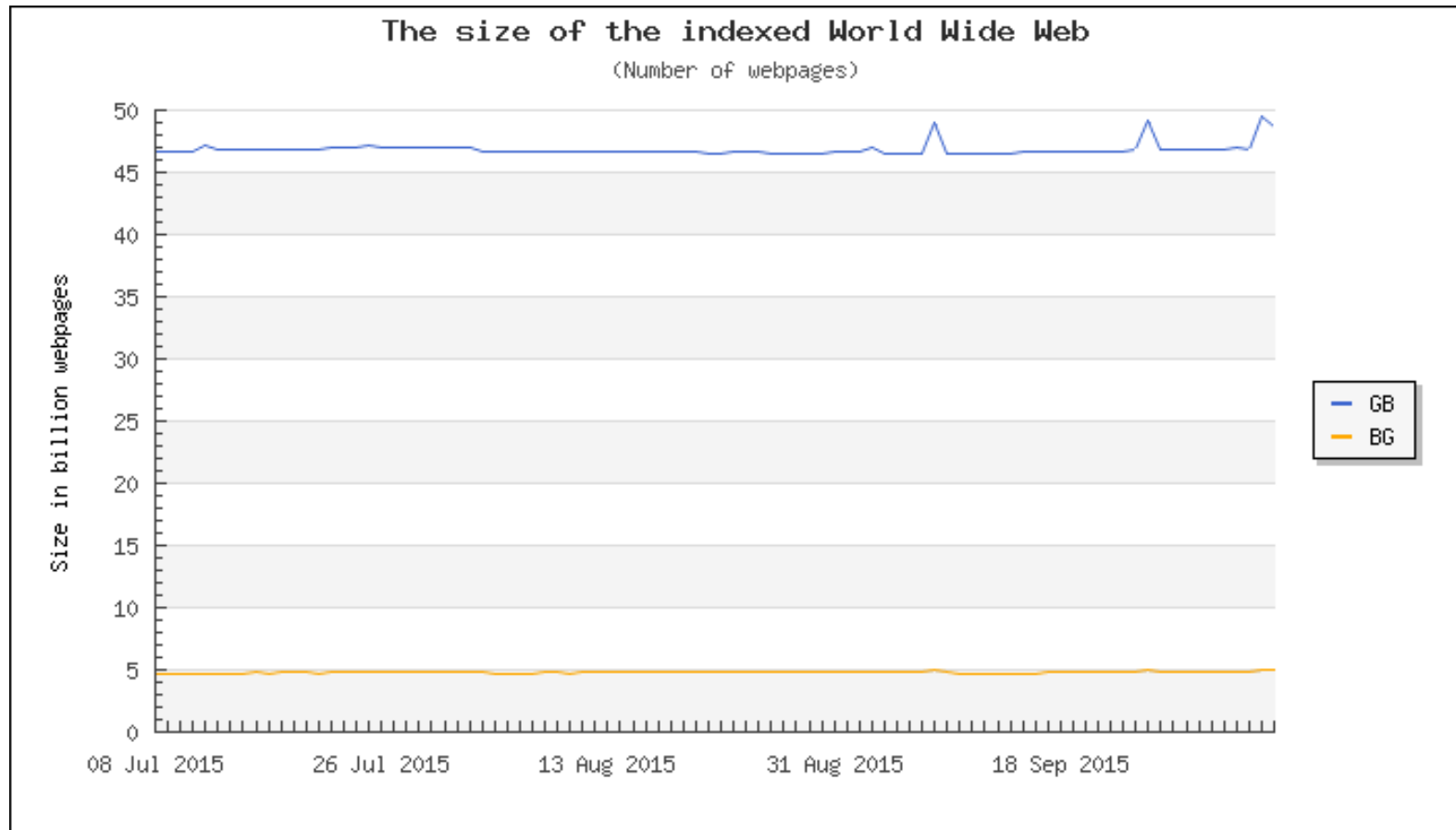
- **Distributed Data:** Documents spread over millions of different web servers.
- **Volatile Data:** Many documents change or disappear rapidly (e.g. dead links).
- **Large Volume:** Billions of separate documents.
- **Unstructured and Redundant Data:** No uniform structure, HTML errors, up to 30% (near) duplicate documents.
- **Quality of Data:** No editorial control, false information, poor quality writing, typos, etc.
- **Heterogeneous Data:** Multiple media types (images, video, VRML), languages, character sets, etc.

Growth of Web Pages Indexed

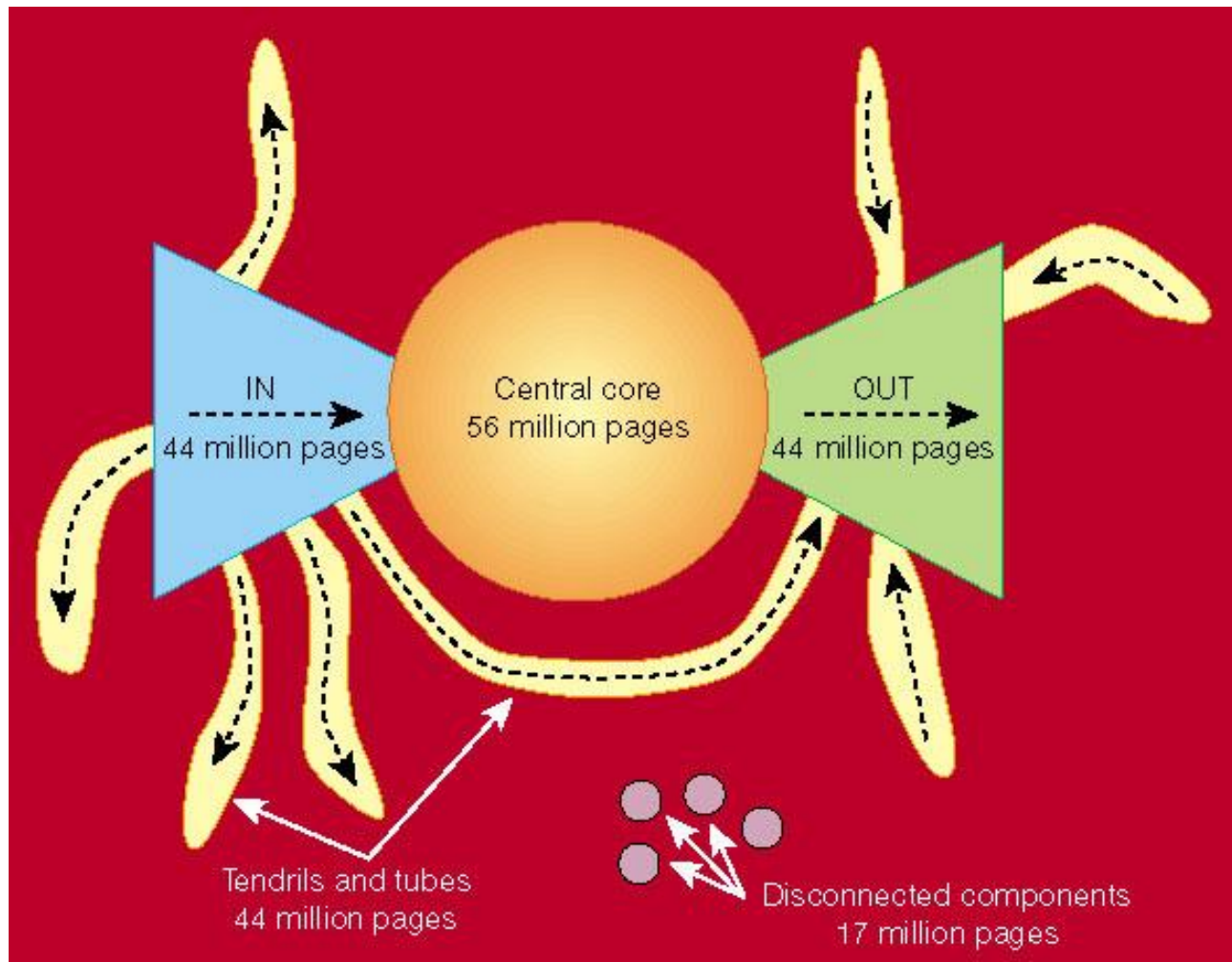


Assuming 20KB per page,
1 billion pages is about 20 terabytes of data.

Current Size of the Web



Graph Structure in the Web

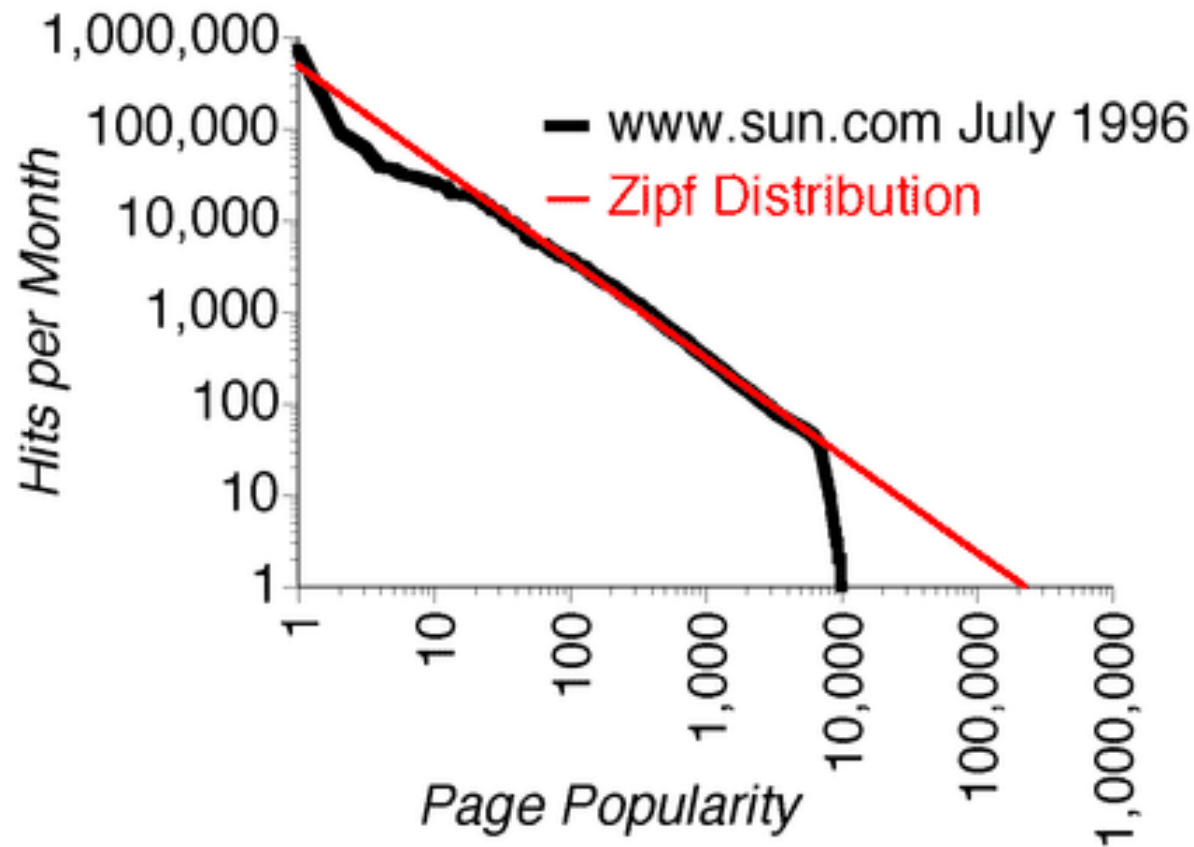


<http://www9.org/w9cdrom/160/160.html>

Zipf's Law on the Web

- Number of in-links/out-links to/from a page has a Zipfian distribution.
- Length of web pages has a Zipfian distribution.
- Number of hits to a web page has a Zipfian distribution.

Zipfs Law and Web Page Popularity



“Small World” (Scale-Free) Graphs

- Social networks and six degrees of separation.
 - [Stanley Milgram Experiment](#)
- Power law distribution of in and out degrees.
- Distinct from purely random graphs.
- “Rich get richer” generation of graphs (preferential attachment).
- Erdos number.
- Networks in biochemistry, roads, telecommunications, Internet, etc are “small world”

Manual Hierarchical Web Taxonomies

- **Yahoo** approach of using human editors to assemble a large hierarchically structured directory of web pages (closed in 2014).
- **Open Directory Project** is a similar approach based on the distributed labor of volunteer editors (“net-citizens provide the collective brain”). Used by most other search engines. Started by Netscape.
 - <http://www.dmoz.org/>
 - **Wikipedia:**

SIZE OF THE WEB

What is the size of the web ?

- Issues
 - The web is really infinite
 - Dynamic content, e.g., calendars
 - Soft 404: www.yahoo.com/<anything> is a valid page
 - Static web contains syntactic duplication, mostly due to mirroring (~30%)
 - Some servers are seldom connected
- Who cares?
 - Media, and consequently the user
 - Engine design
 - Engine crawl policy. • Impact on recall.

What can we attempt to measure?

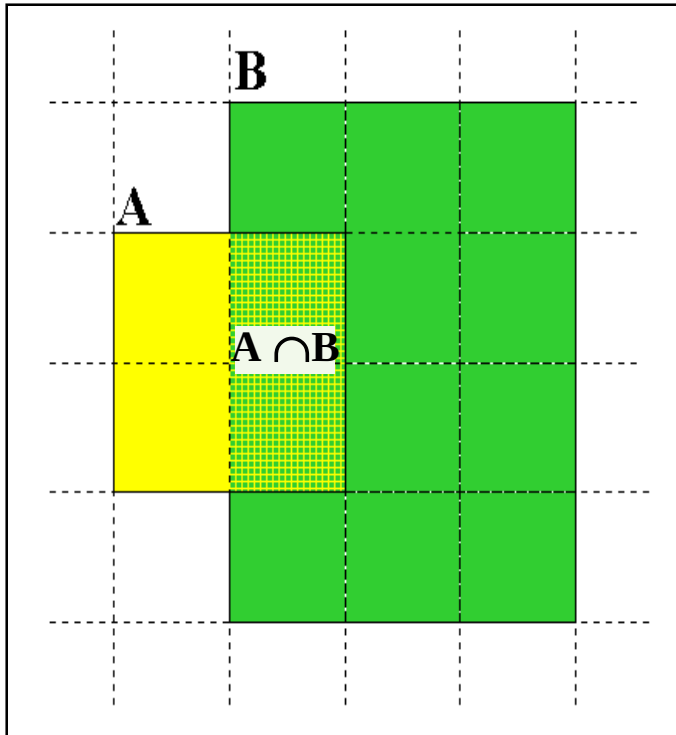
- The relative sizes of search engines
 - The notion of a page being indexed is still *reasonably* well defined.
 - Already there are problems
 - Document extension: e.g., engines index pages not yet crawled, by indexing anchor text.
 - Document restriction: All engines restrict what is indexed (first n words, only relevant words, etc.)

New definition?

- The statically indexable web is whatever search engines index.
- IQ is whatever the IQ tests measure.
- Different engines have different preferences
 - max url depth, max count/host, anti-spam rules, priority rules, etc.
- Different engines index different things under the same URL:
 - frames, meta-keywords, document restrictions, document extensions, ...

Relative Size from Overlap

Given two engines A and B



Sample URLs randomly from A

Check if contained in B and vice versa

$$A \cap B = (1/2) * \text{Size A}$$

$$A \cap B = (1/6) * \text{Size B}$$

$$(1/2) * \text{Size A} = (1/6) * \text{Size B}$$

$$\therefore \text{Size A} / \text{Size B} =$$

$$(1/6) / (1/2) = 1/3$$

Each test involves: (i) Sampling (ii) Checking

Sampling URLs

- Ideal strategy: Generate a random URL and check for containment in each index.
- Problem: Random URLs are hard to find!
Enough to generate a random URL contained in a given Engine.
- Approach 1: Generate a random URL contained in a given engine
 - Suffices for the estimation of relative size
- Approach 2: Random walks / IP addresses
 - In theory: might give us a true estimate of the size of the web (as opposed to just relative sizes of indexes)

Statistical methods

- Approach 1
 - Random queries
 - Random searches
- Approach 2
 - Random IP addresses
 - Random walks

Random URLs from random queries

- Generate random query: how?
 - **Lexicon:** 400,000+ words from a web crawl
 - **Conjunctive Queries:** w_1 and w_2
e.g., vocalists AND rsi
- Get 100 result URLs from engine A
- Choose a random URL as the candidate to check for presence in engine B
- This distribution induces a probability weight $W(p)$ for each page.

Not an English dictionary

Query Based Checking

- *Strong Query* to check whether an engine B has a document D :
 - Download D . Get list of words.
 - Use 8 low frequency words as AND query to B
 - Check if D is present in result set.
- Problems:
 - Near duplicates
 - Frames
 - Redirects
 - Engine time-outs
 - Is 8-word query good enough?

Advantages & disadvantages

- Statistically sound under the induced weight.
- Biases induced by random query
 - Query Bias: Favors content-rich pages in the language(s) of the lexicon
 - Ranking Bias: *Solution:* Use conjunctive queries & fetch all
 - Checking Bias: Duplicates, impoverished pages omitted
 - Document or query restriction bias: engine might not deal properly with 8 words conjunctive query
 - Malicious Bias: Sabotage by engine
 - Operational Problems: Time-outs, failures, engine inconsistencies, index modification.

Random searches

- Choose random searches extracted from a local log [Lawrence & Giles 97] or build “random searches” [Notess]
 - Use only queries with small result sets.
 - Count normalized URLs in result sets.
 - Use ratio statistics

Advantages & disadvantages

- Advantage
 - Might be a better reflection of the human perception of coverage
- Issues
 - Samples are correlated with source of log
 - Duplicates
 - Technical statistical problems (must have non-zero results, ratio average not statistically sound)

Random searches

- 575 & 1050 queries from the NEC RI employee logs
- 6 Engines in 1998, 11 in 1999
- Implementation:
 - Restricted to queries with < 600 results in total
 - Counted URLs from each engine after verifying query match
 - Computed size ratio & overlap for individual queries
 - Estimated index size ratio & overlap by averaging over all queries

Queries from Lawrence and Giles study

- *adaptive access control*
- *neighborhood preservation topographic*
- *hamiltonian structures*
- *right linear grammar*
- *pulse width modulation neural*
- *unbalanced prior probabilities*
- *ranked assignment method*
- *internet explorer favourites importing*
- *karvel thornber*
- *zili liu*
- *softmax activation function*
- *bose multidimensional system theory*
- *gamma mlp*
- *dvi2pdf*
- *john oliensis*
- *rieke spikes exploring neural*
- *video watermarking*
- *counterpropagation network*
- *fat shattering dimension*
- *abelson amorphous computing*

Random IP addresses

- Generate random IP addresses
- Find a web server at the given address
 - If there's one
- Collect all pages from server
 - From this, choose a page at random

Random IP addresses

- HTTP requests to random IP addresses
 - Ignored: empty or authorization required or excluded
 - [Lawr99] Estimated 2.8 million IP addresses running crawlable web servers (16 million total) from observing 2500 servers.
 - OCLC using IP sampling found 8.7 M hosts in 2001
 - Netcraft [Netc02] accessed 37.2 million hosts in July 2002
- [Lawr99] exhaustively crawled 2500 servers and extrapolated

Advantages & disadvantages

- Advantages
 - Clean statistics
 - Independent of crawling strategies
- Disadvantages
 - Doesn't deal with duplication
 - Many hosts might share one IP, or not accept requests
 - No guarantee all pages are linked to root page.
 - E.g.: employee pages
 - Power law for # pages/hosts generates bias towards sites with few pages.
 - But bias can be accurately quantified IF underlying distribution understood

Random walks

- View the Web as a directed graph
- Build a random walk on this graph
 - Includes various “jump” rules back to visited sites
 - Does not get stuck in spider traps!
 - Can follow all links!
 - Converges to a stationary distribution
 - Must assume graph is finite and independent of the walk.
 - Conditions are not satisfied (cookie crumbs, flooding)
 - Time to convergence not really known
 - Sample from stationary distribution of walk
 - Use the “strong query” method to check coverage by SE

Advantages & disadvantages

- Advantages
 - “Statistically clean” method, at least in theory!
 - Could work even for infinite web (assuming convergence) under certain metrics.
- Disadvantages
 - List of seeds is a problem.
 - Practical approximation might not be valid.
 - Non-uniform distribution
 - Subject to link spamming

Conclusions Regarding Web Size

- No sampling solution is perfect.
- Lots of new ideas ...
-but the problem is getting harder
- Quantitative studies are fascinating and a good research problem

Business Models for Web Search

- Advertisers pay for banner ads on the site that do not depend on a user's query.
 - CPM: Cost Per Mille (thousand impressions). Pay for each ad display.
 - CPC: Cost Per Click. Pay only when user clicks on ad.
 - CTR: Click Through Rate. Fraction of ad impressions that result in clicks throughs. $CPC = CPM / (CTR * 1000)$
 - CPA: Cost Per Action (Acquisition). Pay only when user actually makes a purchase on target site.
- Advertisers bid for “keywords”. Ads for highest bidders displayed when user query contains a purchased keyword.
 - PPC: Pay Per Click. CPC for bid word ads (e.g. Google AdWords).

History of Business Models

- Initially, banner ads paid thru CPM were the norm.
- GoTo Inc. formed in 1997 and originates and patents bidding and PPC business model.
- Google introduces AdWords in fall 2000.
- GoTo renamed Overture in Oct. 2001.
- Overture sues Google for use of PPC in Apr. 2002.
- Overture acquired by Yahoo in Oct. 2003.
- Google settles with Overture/Yahoo for 2.7 million shares of Class A common stock in Aug. 2004.

First generation of search ads: Goto (1996)

www.goto.com/d/search/?sessionid=AQ42T4AAH0R5QFIEF3QPUQ?type=home&tr=1&Keywords=Wilmington+

Wilmington real estate.

Access 75% of all users now!
Premium Listings reach 75% of all
Internet users. [Sign up](#) for Premium
Listings today!

1. [Wilmington Real Estate - Buddy Blake](#)
Wilmington's information and real estate guide. This is your on
anything to do with Wilmington.
[www.buddyblake.com](#) (Cost to advertiser: **10.28**)
2. [Coldwell Banker Sea Coast Realty](#)
Wilmington's number one real estate company.
[www.cbseacoast.com](#) (Cost to advertiser: **10.37**)
3. [Wilmington, NC Real Estate Becky Bullard](#)
Everything you need to know about buying or selling a home c
on my Web site!
[www.iwwc.net](#) (Cost to advertiser: **10.35**)

Two ranked lists: web pages (left) and ads (right)

Web Images Maps News Shopping Gmail more Sign in

Google discount broker Search Advanced Search

Web Results 1 - 10 of about 807,000 for discount broker [definition]. (0.12 seconds)

Discount Broker Reviews
Information on online discount brokers emphasizing rates, charges, and customer comments and complaints.
www.broker-reviews.us/ - 94k - Cached - Similar pages

Discount Broker Rankings (2008 Broker Survey) at SmartMoney.com
Discount Brokers. Rank/ Brokerage/ Minimum to Open Account, Comments, Standard Commission*, Reduced Commission, Account Fee Per Year (How to Avoid), Avg. ...
www.smartmoney.com/brokers/index.cfm?story=2004-discount-table - 121k - Cached - Similar pages

Stock Brokers | Discount Brokers | Online Brokers
Most Recommended. Top 5 Brokers headlines. 10. Don't Pay Your Broker for Free Funds May 15 at 3:39 PM. 5. Don't Discount the Discounters Apr 18 at 2:41 PM ...
www.fool.com/investing/brokers/index.aspx - 44k - Cached - Similar pages

Discount Broker
Discount Broker - Definition of Discount Broker on Investopedia - A stockbroker who carries out buy and sell orders at a reduced commission compared to a ...
www.investopedia.com/terms/d/discountbroker.asp - 31k - Cached - Similar pages

Discount Brokerage and Online Trading for Smart Stock Market ...
Online stock broker SogoTrade offers the best in discount brokerage investing. Get stock market quotes from this Internet stock trading company.
www.sogotrade.com/ - 38k - Cached - Similar pages

15 questions to ask discount brokers - MSN Money
Jan 11, 2004 ... If you're not big on hand-holding when it comes to investing, a discount broker can be an economical way to go. Just be sure to ask these ...
moneycentral.msn.com/content/Investing/StartInvesting/P68171.asp - 34k - Cached - Similar pages

Sponsored Links

Rated #1 Online Broker
No Minimums. No Inactivity Fee
Transfer to FirstTrade for Free!
www.firsttrade.com/

Discount Broker
Commission free trades for 30 days.
No maintenance fees. Sign up now.
TDAMERITRADE.com

TradeKing - Online Broker
\$4.95 per Trade, Market or Limit
SmartMoney Top Discount Broker 2007
www.TradeKing.com

Scottrade Brokerage
\$7 Trades, No Share Limit, In-Depth Research. Start Trading Online Now!
www.Scottrade.com

Stock trades \$1.95-\$3
100 free trades, up to \$100 back for transfer costs, \$500 minimum
www.sogotrade.com

\$3.95 Online Stock Trades
Market/Limit Orders, No Share Limit and No Inactivity Fees
www.Marsco.com

INGDIRECT | ShareBuilder
Discount Broker with 24/7 Online Support

SogoTrade appears in search results.

SogoTrade appears in ads.

Do search engines rank advertisers higher than non-advertisers?

All major search engines claim no.

Do ads influence editorial content?

- Similar problem at newspapers / TV channels
- A newspaper is reluctant to publish harsh criticism of its major advertisers.
- The line often gets blurred at newspapers / on TV.
- No known case of this happening with search engines yet?

How are the ads on the right ranked?

Web Images Maps News Shopping Gmail more

Sign in



discount broker

Search

Advanced Search
Preferences

Web

Results 1 - 10 of about 807,000 for discount broker [definition]. (0.12 seconds)

Discount Broker Reviews

Information on online **discount brokers** emphasizing rates, charges, and customer comments and complaints.

www.broker-reviews.us/ - 94k - [Cached](#) - [Similar pages](#)

Discount Broker Rankings (2008 Broker Survey) at SmartMoney.com

Discount Brokers. Rank/ **Brokerage/** Minimum to Open Account, Comments, Standard Commis- sion*, Reduced Commission, Account Fee Per Year (How to Avoid), Avg. ...

www.smartmoney.com/brokers/index.cfm?story=2004-discount-table - 121k -

[Cached](#) - [Similar pages](#)

Stock Brokers | Discount Brokers | Online Brokers

Most Recommended. Top 5 **Brokers** headlines. 10. Don't Pay Your **Broker** for Free Funds May 15 at 3:39 PM. 5. Don't **Discount** the Discounters Apr 18 at 2:41 PM ...

www.fool.com/investing/brokers/index.aspx - 44k - [Cached](#) - [Similar pages](#)

Discount Broker

Discount Broker - Definition of **Discount Broker** on Investopedia - A stockbroker who carries out buy and sell orders at a reduced commission compared to a ...

www.investopedia.com/terms/d/discountbroker.asp - 31k - [Cached](#) - [Similar pages](#)

Discount Brokerage and Online Trading for Smart Stock Market ...

Online stock **broker** SogoTrade offers the best in **discount brokerage** investing. Get stock market quotes from this internet stock trading company.

www.sogotrade.com/ - 39k - [Cached](#) - [Similar pages](#)

15 questions to ask discount brokers - MSN Money

Jan 11, 2004 ... If you're not big on hand-holding when it comes to investing, a **discount broker** can be an economical way to go. Just be sure to ask these ...

moneycentral.msn.com/content/Investing/Startinvesting/P66171.asp - 34k -

[Cached](#) - [Similar pages](#)

Sponsored Links

Rated #1 Online Broker

No Minimums. No Inactivity Fee
Transfer to Firsttrade for Free!

www.firsttrade.com

Discount Broker

Commission free trades for 30 days.
No maintenance fees. Sign up now.

TDAMERITRADE.com

TradeKing - Online Broker

\$4.95 per Trade, Market or Limit

SmartMoney Top **Discount Broker** 2007

www.TradeKing.com

Scottrade Brokerage

\$7 Trades, No Share Limit. In-Depth
Research. Start Trading Online Now!

www.Scottrade.com

Stock trades \$1.50 - \$3

100 free trades, up to \$100 back
for transfer costs, \$500 minimum

www.sogotrade.com

\$3.95 Online Stock Trades

Market/Limit Orders, No Share Limit
and No Inactivity Fees

www.Marsco.com

INGDIRECT | ShareBuilder

Discount Brokerage

How are ads ranked?

- Advertisers bid for keywords – **sale by auction**.
- Open system: Anybody can participate and bid on keywords.
- Advertisers are **only charged when somebody clicks** on your ad.
- How does the auction determine an ad's **rank** and the **price paid** for the ad?
- Basis is a **second price auction**, but with twists
- For the bottom line, this is perhaps the most important research area for search engines – computational advertising.
 - Squeezing an additional fraction of **a cent** from each ad **means billions** of additional revenue for the search engine.

How are ads ranked? Auction: المزاد Second Price

Encourage higher bids with limited risk!

- First cut: according to bid price `a la Goto
 - Bad idea: open to abuse
 - Example: query [does my husband cheat?] → ad for divorce lawyer
 - We don't want to show nonrelevant ads.
- Instead: rank based on bid price **and relevance**
- Key measure of ad relevance: clickthrough rate
 - clickthrough rate = CTR = clicks per impressions
- Result: A nonrelevant ad will be ranked low.
 - Even if this decreases search engine revenue short-term
 - Hope: Overall acceptance of the system and overall revenue is maximized if users get useful information.
- Other ranking factors: location, time of day, quality and loading speed of landing page
- The main ranking factor: the query

Google's second price auction

advertiser	bid	CTR	ad rank	rank	paid
A	\$4.00	0.01	0.04	4	(minimum)
B	\$3.00	0.03	0.09	2	\$2.68
C	\$2.00	0.06	0.12	1	\$1.51
D	\$1.00	0.08	0.08	3	\$0.51

- **bid**: maximum bid for a click by advertiser
- **CTR**: click-through rate: when an ad is displayed, what percentage of time do users click on it? **CTR is a measure of relevance.**
- **ad rank**: $\text{bid} \times \text{CTR}$: this trades off (i) how much money the advertiser is willing to pay against (ii) how relevant the ad is
- **rank**: rank in auction
- **paid**: second price auction price paid by advertiser

Google's second price auction

advertiser	bid	CTR	ad rank	rank	paid
A	\$4.00	0.01	0.04	4	(minimum)
B	\$3.00	0.03	0.09	2	\$2.68
C	\$2.00	0.06	0.12	1	\$1.51
D	\$1.00	0.08	0.08	3	\$0.51

Second price auction: The advertiser pays the minimum amount necessary to maintain their position in the auction (plus 1 cent).

$\text{price}_1 \times \text{CTR}_1 = \text{bid}_2 \times \text{CTR}_2$ (this will result in $\text{rank}_1 = \text{rank}_2$)

$\text{price}_1 = \text{bid}_2 \times \text{CTR}_2 / \text{CTR}_1$

$p_1 = \text{bid}_2 \times \text{CTR}_2 / \text{CTR}_1 = 3.00 \times 0.03 / 0.06 = 1.50$

$p_2 = \text{bid}_3 \times \text{CTR}_3 / \text{CTR}_2 = 1.00 \times 0.08 / 0.03 = 2.67$

$p_3 = \text{bid}_4 \times \text{CTR}_4 / \text{CTR}_3 = 4.00 \times 0.01 / 0.08 = 0.50$

Keywords with high bids

According to <http://www.cwire.org/highest-paying-search-terms/>

\$69.1	mesothelioma treatment options
\$65.9	personal injury lawyer michigan
\$62.6	student loans consolidation
\$61.4	car accident attorney los angeles
\$59.4	online car insurance quotes
\$59.4	arizona dui lawyer
\$46.4	asbestos cancer
\$40.1	home equity line of credit
\$39.8	life insurance quotes
\$39.2	refinancing
\$38.7	equity line of credit
\$38.0	lasik eye surgery new york city
\$37.0	2nd mortgage
\$35.9	free car insurance quote

Search ads: A win-win-win?

- The **search engine** company gets revenue every time somebody clicks on an ad.
- The **user** only clicks on an ad if they are interested in the ad.
 - Search engines punish misleading and nonrelevant ads.
 - As a result, users are often satisfied with what they find after clicking on an ad.
- The **advertiser** finds new customers in a cost-effective way.

Not a win-win-win: Keyword arbitrage

- Buy a keyword on Google
- Then redirect traffic to a third party that is paying much more than you are paying Google.
 - E.g., redirect to a page full of ads
- This rarely makes sense for the user.
- Ad spammers keep inventing new tricks.
- The search engines need time to catch up with them.

Not a win-win-win: Violation of trademarks

- Example: geico
- During part of 2005: The search term “geico” on Google was bought by competitors.
- Geico lost this case in the United States.
- Louis Vuitton lost similar case in Europe.
- See http://google.com/tm_complaint.html
- It’s potentially misleading to users to trigger an ad off of a trademark if the user can’t buy the product on the site.

(Near) Duplicate Detection

- The web is full of duplicated content.
- More so than many other collections
- Exact duplicates
 - Easy to eliminate
 - E.g., use hash/fingerprint
- Near-duplicates
 - Abundant on the web
 - Difficult to eliminate
- For the user, it's annoying to get a search result with near-identical documents.
- **Marginal relevance is zero**: even a highly relevant document becomes nonrelevant if it appears below a (near-)duplicate.
- We need to eliminate near-duplicates.

Near-duplicates: Example



A screenshot of a web browser displaying the Wikipedia page for Michael Jackson. The browser's address bar shows "W Michael...". The Wikipedia logo is in the top left. The page title is "Michael Jackson" with a subtitle "From Wikipedia, the free encyclopedia". A disambiguation note reads: "For other persons named Michael Jackson, see Michael Jackson (disambiguation)." The main text begins with "Michael Joseph Jackson (August 29, 1958 – June 25, 2009) was an American recording artist, entertainer and businessman. The seventh child of the Jackson family; he made his debut as an entertainer in 1968 as a member of The". A portrait of Michael Jackson in a black military-style jacket with a red armband is shown. The left sidebar contains navigation links (Main page, Contents, Featured content, Current events, Random article) and a search box. The bottom of the browser shows a search bar with "Find: Q pric" and navigation buttons.

wapedia.

Wiki: Michael Jackson (1/6)

For other persons named Michael Jackson, see [Michael Jackson \(disambiguation\)](#).

Michael Joseph Jackson (August 29, 1958 - June 25, 2009) was an American recording artist, entertainer and businessman. The seventh child of the [Jackson family](#), he made his debut as an entertainer in 1968 as a member of [The Jackson 5](#). He then began a solo

Detecting near-duplicates

- Compute similarity with an edit-distance measure
- We want “syntactic” (as opposed to semantic) similarity.
 - True semantic similarity (similarity in content) is too difficult to compute.
- We do not consider documents near-duplicates if they have the same content, but express it with different words.
- Use similarity threshold θ to make the call “is/isn’t a near-duplicate”.
- E.g., two documents are near-duplicates if similarity $> \theta = 80\%$.

Represent each document as set of **shingles**

- 
- A shingle (قطعة قرميد) is simply a **word n-gram**.
 - Shingles are used as features to **measure syntactic similarity** of documents.
 - For example, for $n = 3$, “a rose is a rose is a rose” would be represented as this set of shingles:
 - { a-rose-is, rose-is-a, is-a-rose }
 - We can map shingles to $1..2^m$ (e.g., $m = 64$, quite large) by fingerprinting.
 - From now on: s_k refers to the shingle’s fingerprint (map) in $1..2^m$.
 - We define the similarity of two documents as the **Jaccard coefficient of their shingle sets**.

Recall: Jaccard coefficient

- A commonly used measure of overlap of two sets
- Let A and B be two sets
- Jaccard coefficient:

$$\text{JACCARD}(A, B) = \frac{|A \cap B|}{|A \cup B|}$$

$$(A \neq \emptyset \text{ or } B \neq \emptyset)$$

- $\text{JACCARD}(A, A) = 1$
- $\text{JACCARD}(A, B) = 0$ if $A \cap B = \emptyset$
- A and B don't have to be the same size.
- Always assigns a number between 0 and 1.



Jaccard coefficient: Example

- Three documents:

d_1 : “Jack London traveled to Oakland”

d_2 : “Jack London traveled to the city of Oakland”

d_3 : “Jack traveled from Oakland to London”

- Based on shingles of size 2 (2-grams or bigrams), what are the Jaccard coefficients $\mathcal{J}(d_1, d_2)$ and $\mathcal{J}(d_1, d_3)$?

- $\mathcal{J}(d_1, d_2) = 3/8 = 0.375$

- $\mathcal{J}(d_1, d_3) = 0$

- Note: very sensitive to dissimilarity

Represent each document as a sketch

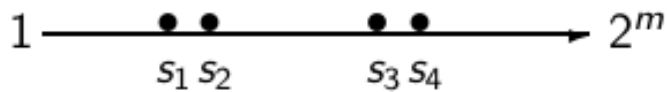
- The number of shingles per document is large (why?).
- To increase efficiency, we will use a **sketch**, a cleverly chosen **subset** of the shingles of a document.
- The size of each sketch is, say, $n = 200 \dots$
- $\dots$ and is defined by a set of permutations $\pi_1 \dots \pi_{200}$.
- Each π_i is a random permutation on $1..2^m$
- The **sketch** of d is defined as:
$$\langle \min_{s \in d} \pi_1(s), \min_{s \in d} \pi_2(s), \dots, \min_{s \in d} \pi_{200}(s) \rangle$$

(a vector of 200 numbers).

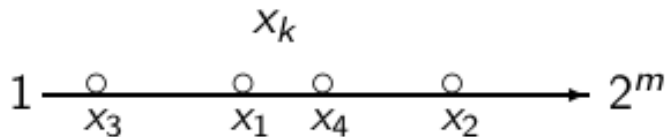
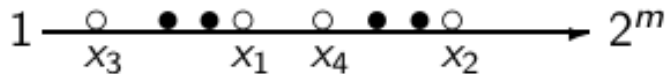
So we have 200 permutations that are computed on all docs

The Permutation and minimum: Example

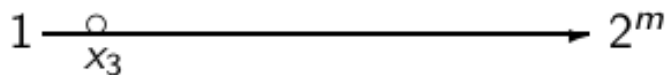
document 1: $\{s_k\}$



$$x_k = \pi(s_k)$$



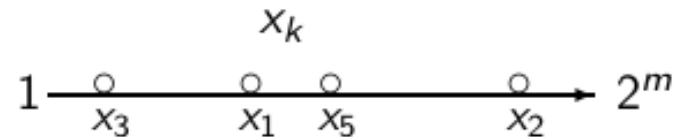
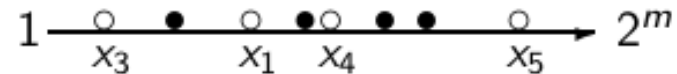
$$\min_{s_k} \pi(s_k)$$



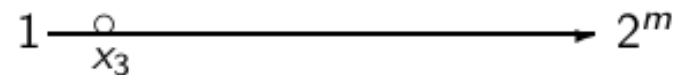
document 2: $\{s_k\}$



$$x_k = \pi(s_k)$$



$$\min_{s_k} \pi(s_k)$$



We use $\min_{s \in d_1} \pi(s) = \min_{s \in d_2} \pi(s)$ as a test for: are d_1 and d_2 near-duplicates? In this case: permutation π says: $d_1 \approx d_2$

Computing Jaccard for sketches

- Sketches: Each document is now a vector of $n = 200$ numbers.
- Much easier to deal with than the very high-dimensional space of shingles
- But how do we compute Jaccard?

Computing Jaccard for sketches (2)

- How do we compute Jaccard?
- Let U be the union of the set of shingles of d_1 and d_2 and I the intersection.
- There are $|U|!$ permutations on U .
- For $s' \in I$, for how many permutations π do we have
 $\operatorname{argmin}_{s \in d_1} \pi(s) = s' = \operatorname{argmin}_{s \in d_2} \pi(s)$?
- Answer: $(|U| - 1)!$
- There is a set of $(|U| - 1)!$ different permutations for each s in I . $\Rightarrow |I|(|U| - 1)!$ permutations make
 $\operatorname{argmin}_{s \in d_1} \pi(s) = \operatorname{argmin}_{s \in d_2} \pi(s)$ true
- Thus, the proportion of permutations that make
 $\min_{s \in d_1} \pi(s) = \min_{s \in d_2} \pi(s)$ true is:

$$\frac{|I|(|U| - 1)!}{|U|!} = \frac{|I|}{|U|} = J(d_1, d_2)$$

Estimating Jaccard

- Thus, the proportion of successful permutations is the Jaccard coefficient.
 - Permutation π is successful iff $\min_{s \in d_1} \pi(s) = \min_{s \in d_2} \pi(s)$
- Picking a permutation at random and outputting 1 (successful) or 0 (unsuccessful) is a Bernoulli trial.
- Estimator of probability of success: proportion of successes in n Bernoulli trials. ($n = 200$)
- Our sketch is based on a random selection of permutations.
- Thus, to compute Jaccard, count the number k of successful permutations for $\langle d_1, d_2 \rangle$ and divide by $n = 200$.
- $k/n = k/200$ estimates $\mathcal{J}(d_1, d_2)$.

Implementation

- We use **hash functions** as an efficient type of permutation:

$$h_i: \{1..2^m\} \rightarrow \{1..2^m\}$$

- Scan all shingles s_k in union of two sets in arbitrary order
- For each hash function h_i and documents $d_1, d_2, \dots$: keep slot for minimum value found so far
- If $h_i(s_k)$ is lower than minimum found so far: update slot

Example (2 permutations: mod functions)

d_1 d_2

s_1 1 0

s_2 0 1

s_3 1 1

s_4 1 0

s_5 0 1

$$h(x) = x \bmod 5$$

$$g(x) = (2x + 1) \bmod 5$$

$$\min(h(d_1)) = 1 \neq 0 =$$

$$\min(h(d_2)) \quad \min(g(d_1)) =$$

$$2 \neq 0 = \min(g(d_2))$$

$$\hat{J}(d_1, d_2) = \frac{0+0}{2} = 0$$

	d_1 slot		d_2 slot	
h	∞		∞	
g	∞		$\downarrow$	∞
$h(1) = 1$	1	1	$\overline{0}$	∞
$g(1) = 3$	3	3	$-$	∞
$h(2) = 2$	$\overline{0}$	$1 \downarrow$	2	2
$g(2) = 0$	$-$	3	0	0
$h(3) = 3$	3	1	3	2
$g(3) = 2$	2	2	2	0
$h(4) = 4$	4	1	$\overline{0}$	$2 \swarrow$
$g(4) = 4$	4	2	$-$	0
$h(5) = 0$	$-$	$1 \downarrow$	0	0
$g(5) = 1$	$\overline{0}$	2	1	0

final sketches

Exercise

	d_1	d_2	d_3
s_1	0	1	1
s_2	1	0	1
s_3	0	1	0
s_4	1	0	0

$$h(x) = 5x + 5 \bmod 4 \quad \text{Estimate } \hat{J}(d_1, d_2),$$
$$g(x) = (3x + 1) \bmod 4$$

$$\hat{J}(d_1, d_3), \hat{J}(d_2, d_3)$$

Solution (1)

	d_1	d_2	d_3
s_1	0	1	1
s_2	1	0	1
s_3	0	1	0
s_4	1	0	0

$$h(x) = 5x + 5 \bmod 4$$

$$g(x) = (3x + 1) \bmod 4$$

	d_1 slot	d_2 slot	d_3 slot
	∞	∞	∞
	∞	∞	∞
$h(1) = 2$	– ∞	2 2	2 2
$g(1) = 0$	– ∞	0 0	0 0
$h(2) = 3$	3 3	– 2	3 2
$g(2) = 3$	3 3	– 0	3 0
$h(3) = 0$	– 3	0 0	– 2
$g(3) = 2$	– 3	2 0	– 0
$h(4) = 1$	1 1	– 0	– 2
$g(4) = 1$	1 1	– 0	– 0

final sketches

Solution (2)

$$\hat{J}(d_1, d_2) = \frac{0 + 0}{2} = 0$$

$$\hat{J}(d_1, d_3) = \frac{0 + 0}{2} = 0$$

$$\hat{J}(d_2, d_3) = \frac{0 + 1}{2} = 1/2$$

Shingling: Summary

- Input: N documents
- Choose n -gram size for shingling, e.g., $n = 5$
- Pick 200 random permutations, represented as hash functions
- Compute N sketches: $200 \times N$ matrix shown on previous slide, one row per permutation, one column per document
- Compute pairwise similarities
- Transitive $\epsilon \frac{N \cdot (N-1)}{2}$ documents with similarity $> \theta$
- Index only one document from each equivalence class

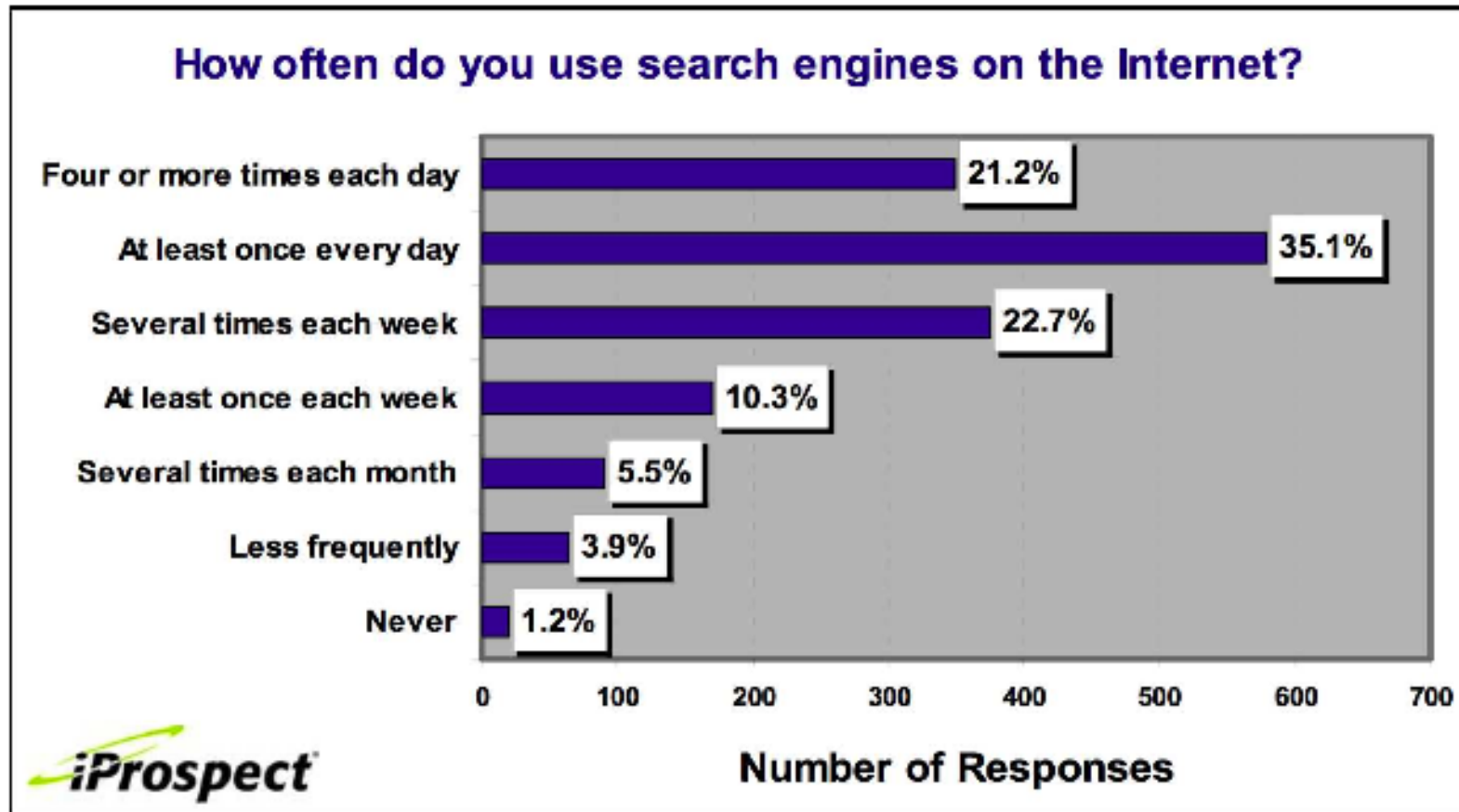
Efficient near-duplicate detection

- Now we have an extremely efficient method for estimating a Jaccard coefficient for a **single** pair of two documents.
- But we still have to estimate $O(N^2)$ coefficients where N is the number of web pages.
- Still intractable
- One solution: locality sensitive hashing (LSH)
- Another solution: sorting (Henzinger 2006)

User Interfaces

- HTML supports various types of program input in forms, including:
 - Text boxes
 - Menus
 - Check boxes
 - Radio buttons
- When user submits a form, string values for various *parameters* are sent to the server program for processing.
- Server program uses these values to compute an appropriate HTML response page.

Search is the top activity on the web



User Query Length

- Users tend to enter short queries.
 - Study in 1998 gave average length of 2.35 words.
- More recent evidence that queries are getting longer.

Percentage of U.S. clicks by number of keywords				
Subject	Jan-08	Dec-08	Jan-09	Year-over-year percent change
1 word	20.96%	20.70%	20.29%	-3%
2 words	24.91%	24.13%	23.65%	-5%
3 words	22.03%	21.94%	21.92%	0%
4 words	14.54%	14.67%	14.89%	2%
5 words	8.20%	8.37%	8.68%	6%
6 words	4.32%	4.47%	4.65%	8%
7 words	2.23%	2.40%	2.49%	12%
8+ words	2.81%	3.31%	3.43%	22%
<i>Note: Data is based on four-week rolling periods (ending Jan. 31, 2009; Dec. 27, 2008; and Jan. 26, 2008) from the Hitwise sample of 10 million U.S. Internet users.</i>				
Source: Hitwise, an Experian company				