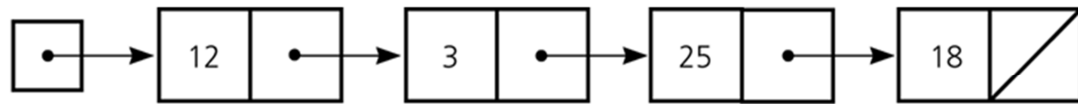




Linked List

Algorithm - abstract way to perform computation tasks

Data Structure - abstract way to organize information



Linked List:

Node:



Node code:

```
public class Node<T> {
    private T data;
    private Node<T> next;

    public Node(T data) { this.data = data; }

    public void setData(T data) { this.data = data; }
    public T getData() { return data; }

    public Node<T> getNext() { return next; }
    public void setNext(Node<T> next) { this.next = next; }
}
```

Linked List Code:

```
public class LinkedList<T> {
    private Node<T> head;
}
```

Inserting a new node:

Inserting a Node into a Specified Position of a Linked List:

Three steps to insert a new node into a linked list

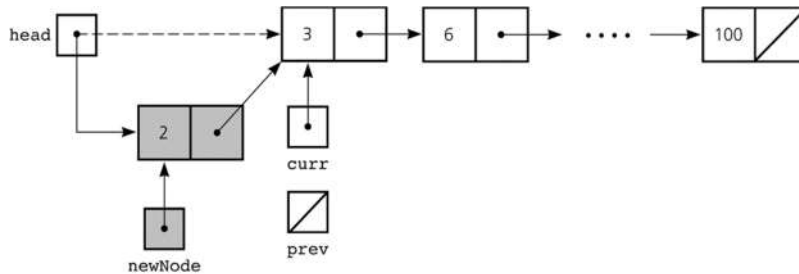
- Determine the point of insertion
- Create a new node and store the new data in it
- Connect the new node to the linked list by changing references





Case 1: To insert a node at the beginning of a linked list: ($\text{curr} == \text{head}$)

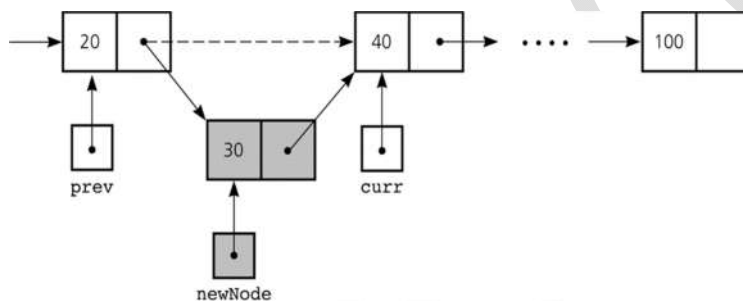
```
newNode.next = head;
head = newNode;
```



What's the time complexity of inserting an item to the head?? → **$O(1)$**

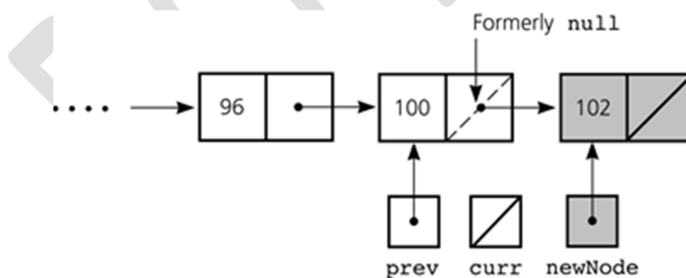
Case 2: To insert a node between two nodes:

```
newNode.next = curr;
prev.next = newNode;
```



Case 3: Inserting at the end of a linked list is a special case if curr is **null**:

```
newNode.next = curr;
prev.next = newNode;
```



Time Complexity → **$O(n)$**

H.W. → implement insert into a sorted linked list

Determining **curr** and **prev**

Determining the point of insertion or deletion for a sorted linked list of objects

```
for ( prev = null , curr = head;
      (curr != null) && (newValue.compareTo(curr.item) > 0);
```





```
prev = curr , curr = curr.next ) ; // end for
```

Create a driver class to test linked list classes.

Override the **toString** methods first

Node toString:

@Override

```
public String toString() { return data.toString(); }
```

LinkedList toString:

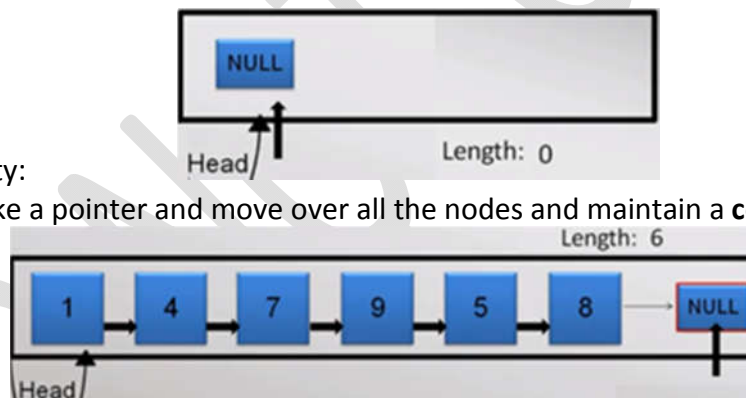
@Override

```
public String toString() {
    String res = "→";
    Node<T> curr = head;
    while (curr != null) {
        res += curr + "→ ";
        curr = curr.next;
    }
    return res + "NULL";
}
```

Length of Linked List?

Case 1: If it's empty:

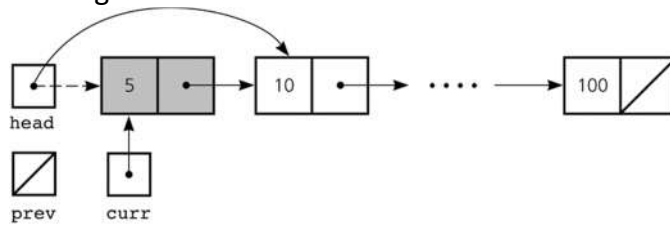
Case 2: If not: Make a pointer and move over all the nodes and maintain a **counter**



Length code: Time Complexity → $O(n)$

```
public int length() {
    int length = 0;
    Node<T> curr = head;
    while (curr != null) {
        length++;
        curr = curr.next;
    }
    return length;
}
```

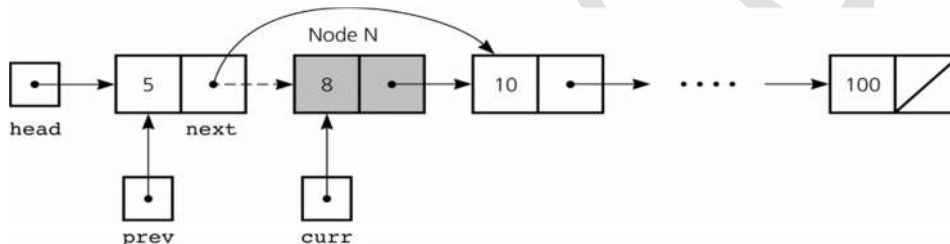


**Deleting Nodes:****Case 1: Deleting the head node:**Simply move the **head** to the **head.next**: `head = head.next;`Now first Node has no reference to it → **Garbage**Time Complexity → **O(1)****Delete at head code:** // make sure linked list is not empty

```

public Node<T> deleteAtStart() {
    Node<T> toDel = head;
    head = head.next;
    return toDel;
}

```

Case 2: Delete node N which curr references:Set **next** in the node that precedes **N** to reference the node that follows **N**`prev.next = curr.next; // prev.next = prev.next.next;`**Searching for an Item in a Linked List:**Time Complexity: linear growth → **O(n)**

Find code:

```

public Node<T> find(T data) {
    Node<T> curr = head;
    while (curr != null) {
        if (curr.getData() == data) // if (curr.getData().equals(data))
            return curr;
        curr = curr.next;
    }
    return null;
}

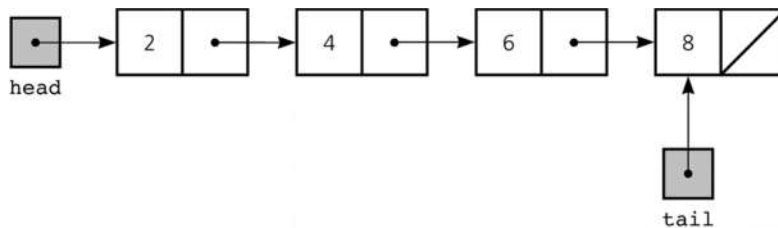
```



**Variations of the Linked List:****1- Tail References (Doubly Ended Linked List)**

- Remembers where the end of the linked list is.
- Therefore, we can add and delete at both ends.
- To add a node to the end of a linked list

tail.next = new Node(request, null);



```

public class DoubleEndedList<T> extends LinkedList<T> {
    private Node<T> tail;
    public Node<T> getTail() { return tail; }

    public void addAtEnd(T data) {
        Node<T> newNode = new Node<T>(data);
        if (head == null) { // empty
            head = newNode;
            tail = newNode;
        }
        else {
            tail.setNext(newNode);
            tail = newNode;
        }
    }
}
  
```

Make sure to override addAtStart to set the tail pointer correctly:

```

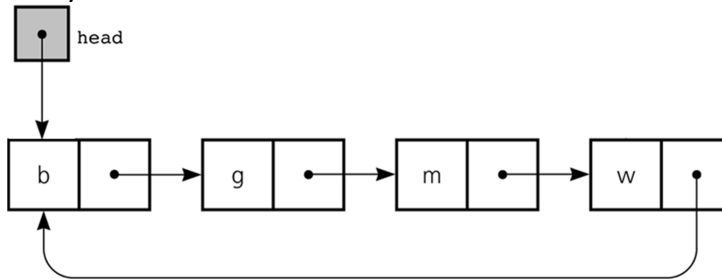
@Override
public void addAtStart(T data) {
    Node<T> newNode = new Node<T>(data);
    if (head == null) { // empty
        head = newNode;
        tail = newNode;
    }
    else{
        newNode.setNext(head);
        head = newNode;
    }
}
  
```





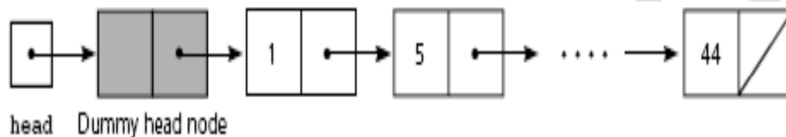
2- Circular Linked List

- Last node references the first node
- Every node has a successor



3- Dummy Head Nodes

- Always present, even when the linked list is empty
- Insertion and deletion algorithms initialize **prev** to reference the dummy head node, rather than **null**



Processing Linked Lists Recursively:

• Traversal

- Recursive strategy to display a list
- Write the first node of the list
- Write the list minus its first node

```

public static void traversList(Node curr) {
    if(curr == null)
        System.out.println("NULL");
    else {
        System.out.print "[" + curr + "-->";
        traversList(curr.next);
    }
}
  
```

- Recursive strategies to display a list backward

• writeListBackward strategy

Write the last node of the list

Write the list minus its last node backward

```

public static void traversListBackward(Node curr) {
    if(curr == null)
        System.out.print("NULL");
    else {
        traversListBackward(curr.next);
        System.out.print("<--[" + curr + "]");
    }
}
  
```



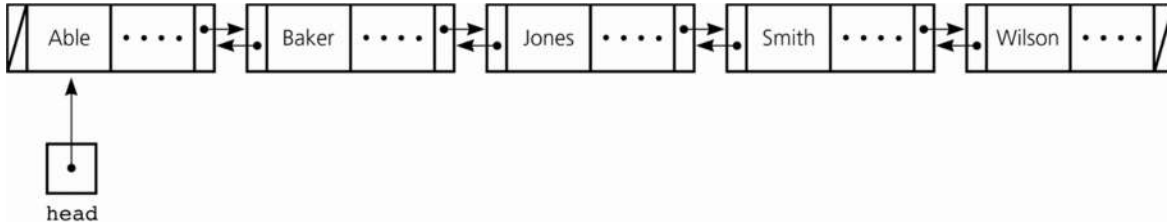


Doubly Linked List

Node:

Date
Next → null
null ← Prev

Doubly Linked List: Each node references both its predecessor and its successor:



Doubly Node Code:

```

public class DNode <T extends Comparable<T>>{
    T data;
    DNode next;
    DNode prev;

    public DNode(T data) { this.data = data; }
    public T getData() { return data; }
    public DNode getNext () { return next; }
    public DNode getPrev () { return prev; }

    public void setNext(DNode next) { this.next = next; }
    public void setPrev(DNode prev) { this.prev = prev; }
    public String toString() { return this.data.toString(); }
}

```

Doubly Linked List code:

```

public class DLinkedList <T extends Comparable<T>>{
    DNode head;
}

```

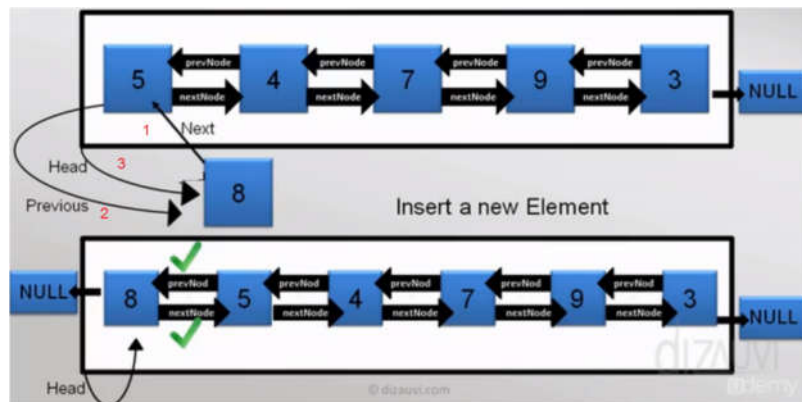
Override toString method code:

```

public String toString() {
    String res = "Head-->";
    DNode<T> curr = this.head;
    while (curr != null) {
        res += "["+curr + "]";
        curr = curr.getNext();
        if(curr!=null)
            res += "<=>";
    }
    return res + "-->NULL";
}

```



**Insert a new node (not sorted)****Case 1: Insert at head:**

```

public void insertAtHead(T data) {
    DNode<T> newNode = new DNode(data);
    if(head==null) // empty linkedlist
        head = newNode;
    else {
        newNode.setNext(this.head);
        head.setPrev(newNode);
        head = newNode;
    }
}

```

Case 2: Insert at end:**Student Activity: insert at last**

```

public void insertAtEnd(T data) {
    DNode<T> newNode = new DNode(data);
    if (head == null) // empty linkedlist
        head = newNode;
    else { // find last node
        DNode<T> last = head;
        while(last.getNext() != null)
            last = last.getNext();
        last.setNext(newNode);
        newNode.setPrev(last);
    }
}

```

Length of a doubly linked list code:

```

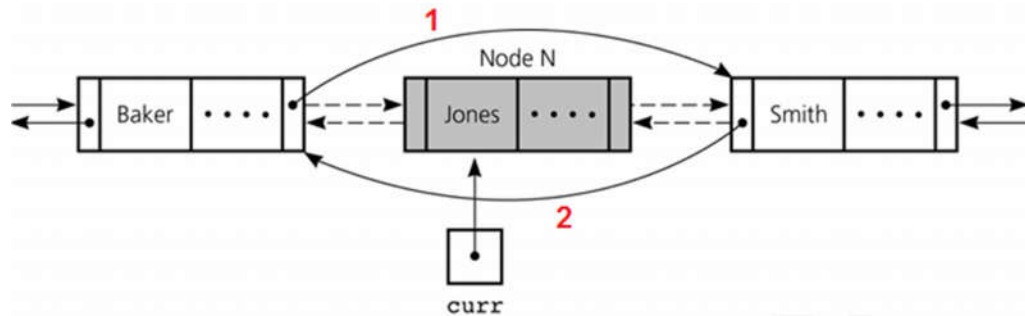
public int length() {
    int length = 0;
    DNode<T> curr = this.head;
    while (curr != null) {
        length++;
        curr = curr.getNext();
    }
    return length;
}

```



**Delete a node:**

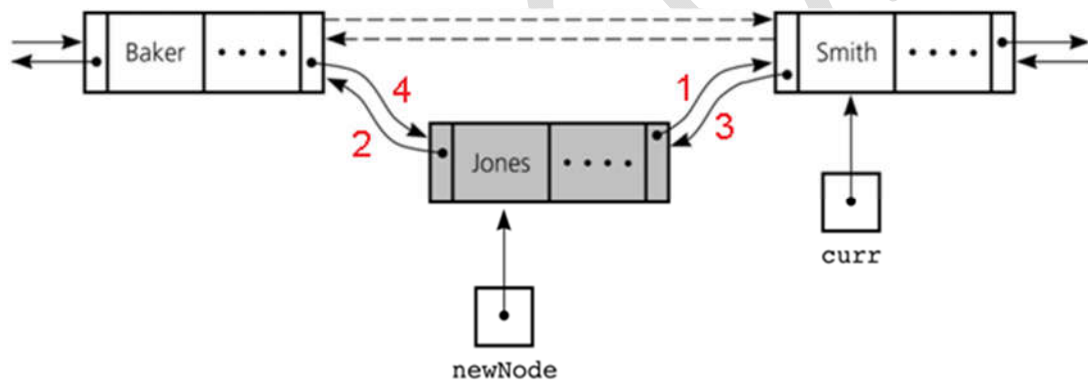
- To delete the node that **curr** pointer references



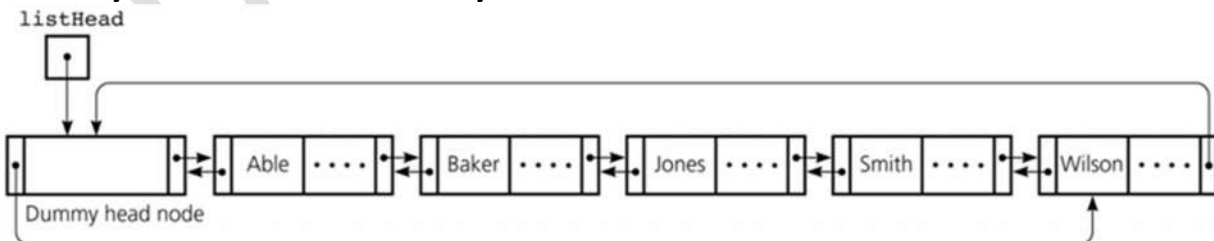
```
curr.prev.next = curr.next;
curr.next.prev = curr.prev;
```

Insert a new Node (Sorted):

- To insert a new node that **newNode** references before the node referenced by **curr**



```
newNode.next = curr;           // 1
newNode.prev = curr.prev;      // 2
curr.prev = newNode;          // 3
newNode.prev.next = newNode;   // 4
```

Circular doubly linked list with dummy head:

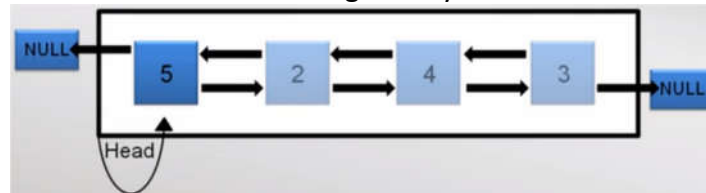
- Preceding reference of the dummy head node references the last node.
- next reference of the last node references the dummy head node.
- **Eliminates special cases for insertions and deletions.**



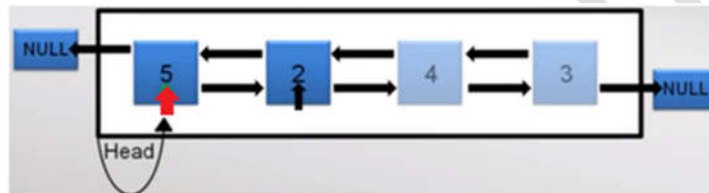
**Case Study: Insertion Sort using doubly linked list (Using NO extra space):**

Review insertion sort logic and point to problem of insertion and time needed to shift the items
Worst case if the array is reverse sorted

Example: assume we need to sort the following doubly linked list:



Assumption: 1st node is sorted. We start from the 2nd element:



Here:

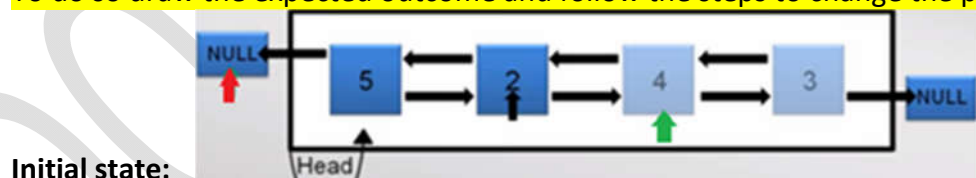
- The **black** pointer points to the **current** node to be sorted.
- The **red** pointer points to previous node of **current** node to be sorted.
- The **green** pointer points to next node of **current** node to be sorted.

Step 1: The **red** pointer keeps move backward until it reaches a node which has a value **smaller** than the **current** node **OR** reach **NULL**.

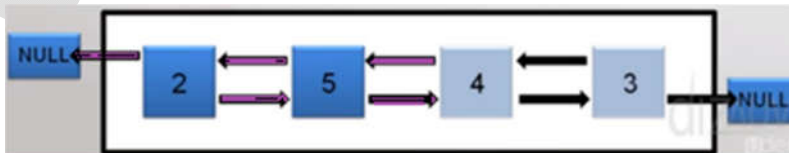
Step 2: the **current** item will be inserted after **red** pointer as follow:

Make sure you maintain references correctly.

To do so draw the expected outcome and follow the steps to change the pointers:



Final state:

**Case 1: insert to head**

Step 2.0: make new **green** pointer = **black.next**

Step 2.1: $\rightarrow$ **black.prev.next = green**



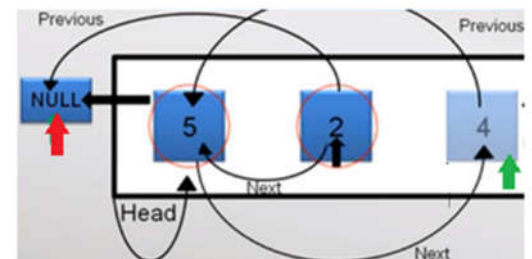
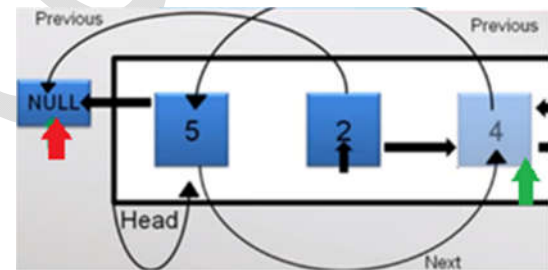
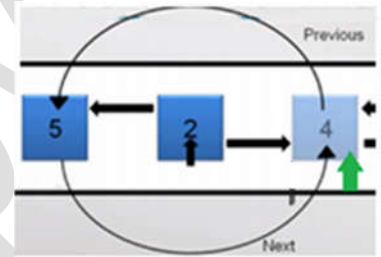
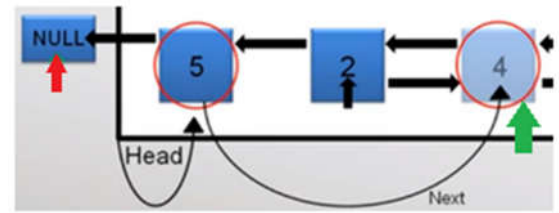


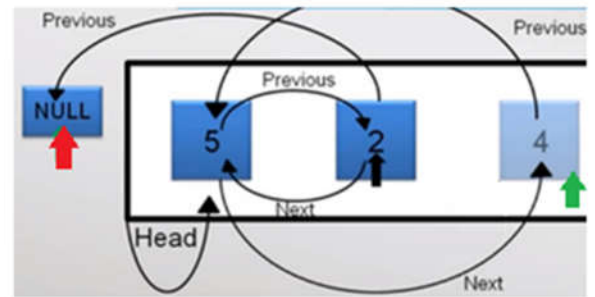
Step 2.2:  $\rightarrow$
 if (**green** != null) **green**.prev = black.prev

Step 2.3:  $\rightarrow$ **black.prev = red**

Step 2.4:  $\rightarrow$
 if (**red** == null) **black.next** = **black.next**.prev
 else **black.next** = **red.next**

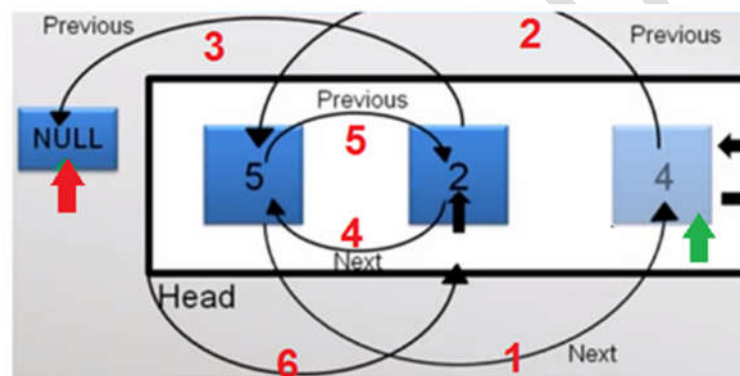
Step 2.5:  $\rightarrow$
 If (**red** == null) **black.next**.prev = **black**
 else **red.next**.prev = **black**





Step 2.6:

```
if (red == NULL) head = black;
else red.next = black;
```

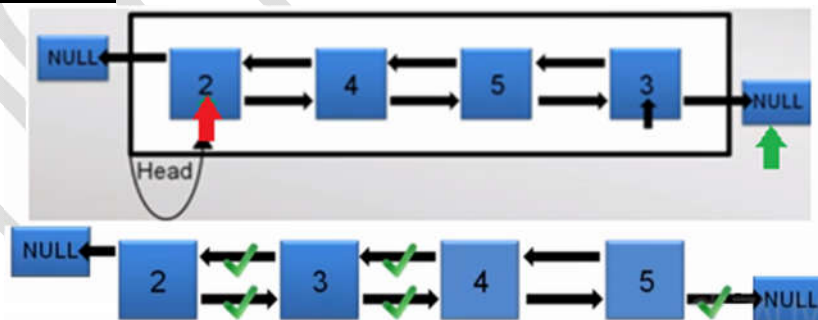


Step 2.7: black = green

Case 2: insert 4 in the middle

Practice yourself

Case 3: insert last element





Insertion Sort Code:

```
// Insertion Sort of a Doubly Linked List
public void sort() {
    DNode black = head.next;
    while (black != null) {
        DNode red = black.prev;
        while (red != null && (red.data.compareTo(black.data) > 0)) // step 1.0
            red = red.prev;

        DNode green = black.next; // step 2.0
        if (red != null || (head != black)) {
            black.prev.next = green; // step 2.1
            if (green != null) {
                green.prev = black.prev; // step 2.2
            }
            black.prev = red; // step 2.3
        }
        if (red == null) { // set the black as head
            if (head != black) {
                black.next = head; // step 2.4
                black.next.prev = black; // step 2.5
                head = black; // step 2.6
            }
        } else { // red is not null
            black.next = red.next; // step 2.4
            red.next.prev = black; // step 2.5
            red.next = black; // step 2.6
        }
        black = green; // step 2.7
    }
}
```

