Ch2 Part 1
Wednesday, September 22, 2021 12:27 PM limits and Continuity Def f(x) has limit L as x approaches xo if J= (1) = V $\lim_{x \to x_0} f(x) = L$ $\lim_{x \to \infty} f(x) = \lim_{x \to \infty} f(x) = L$ lim: limit X >> Xo: X approaches Xo (this does not mean x = x.) X. : from left xt : from right $\beta = f(x)$ lim f(x)=L x→x₆

$$\frac{E \times p}{E}$$
 () $\lim_{x \to 0} (x^2 - 3) = \frac{3}{6} - 3 = 0 - 3 = \frac{-3}{6}$ (Since we see Exp. 1)

$$\frac{2}{5} \left(\frac{2}{1} \right) \lim_{x \to -2} \frac{\left(\frac{2}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{2}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{2}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{2}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{2}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{2}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{2}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{2}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{2}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{2}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{2}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{2}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{2}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right) \left(\frac{x}{x} + \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right) \left(\frac{x}{x} - \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right) \left(\frac{x}{x} - \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right) \left(\frac{x}{x} - \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right) \left(\frac{x}{x} - \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right) \left(\frac{x}{x} - \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right) \left(\frac{x}{x} - \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right) \left(\frac{x}{x} - \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right) \left(\frac{x}{x} - \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right) \left(\frac{x}{x} - \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2} \frac{\left(\frac{x}{x} - \frac{1}{2} \right)}{x + 2} = \lim_{x \to -2}$$

f(x) underined

$$f(x) = \frac{x^2 - 4}{x + 2}$$

f(-1) undefined

$$f(x) = \frac{x^2}{x^2}$$

f is not continuous at x=-2

$$\lim_{x \to 2} (x+2)(x-1)$$

$$= \lim_{x \to 1} \frac{2x+1}{2x-1} = \frac{2+1}{2-1} = \frac{3}{1} = \frac{3}{1}$$

$$| \lim_{x \to 1} \frac{x+2}{x} = \frac{1+2}{1} = 3$$

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$$| \lim_{x \to 1} \frac{x^2 + 8 - 3}{x + 1} = \frac{\sqrt{x^2 + 8} + 3}{\sqrt{x^2 + 8} + 3}$$

$$= \lim_{x \to -1} \frac{(\sqrt{x^2 + 8} - 3)(\sqrt{x^2 + 8} + 3)}{(x + 1)(\sqrt{x^2 + 8} + 3)}$$

$$= \lim_{x \to -1} \frac{x^2 + 8 - 9}{(x + 1)(\sqrt{x^2 + 8} + 3)} = \lim_{x \to -1} \frac{x^2 - 1}{(x + 1)(\sqrt{x^2 + 8} + 3)}$$

$$= \lim_{x \to -1} \frac{(x + 1)(x + 1)}{(x + 1)(\sqrt{x^2 + 8} + 3)} = \lim_{x \to -1} \frac{(x + 1)(\sqrt{x^2 + 8} + 3)}{(x + 1)(\sqrt{x^2 + 8} + 3)}$$

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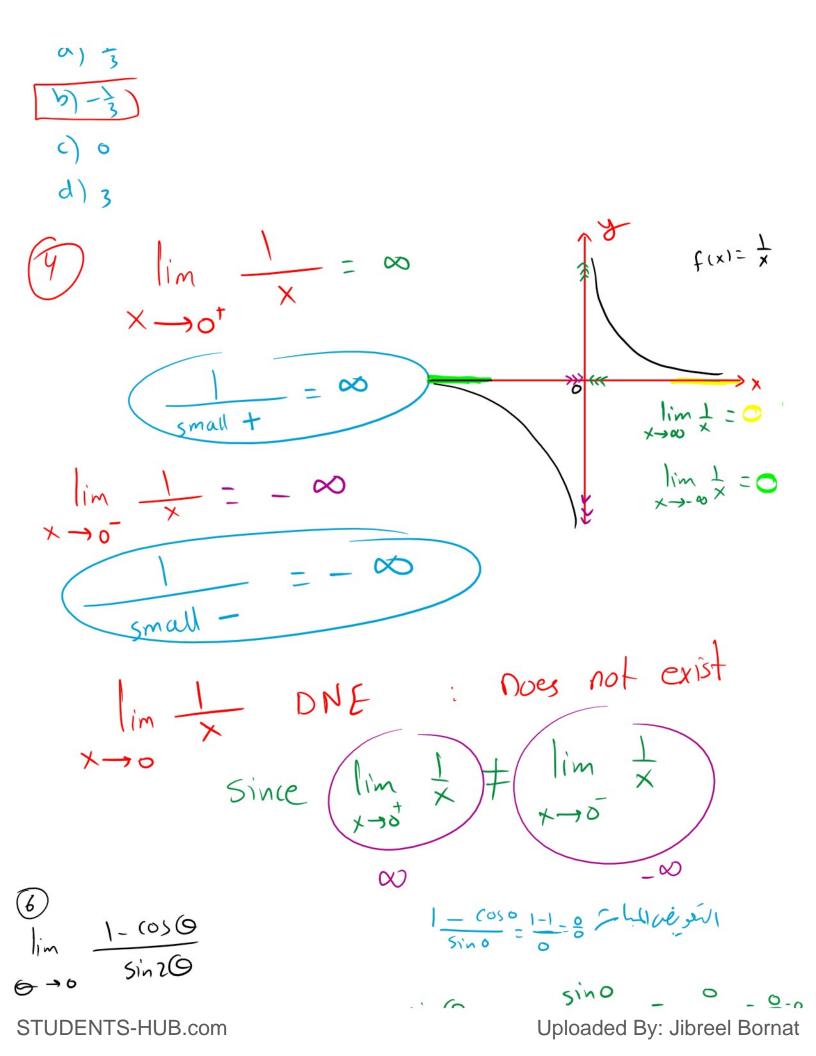
$$= \lim_{x \to -1} \frac{(x + 1)(x + 1)}{(x + 1)(\sqrt{x^2 + 8} + 3)} = \lim_{x \to -1} \frac{(x + 1)(\sqrt{x^2 + 8} + 3)}{(x + 1)(\sqrt{x^2 + 8} + 3)}$$

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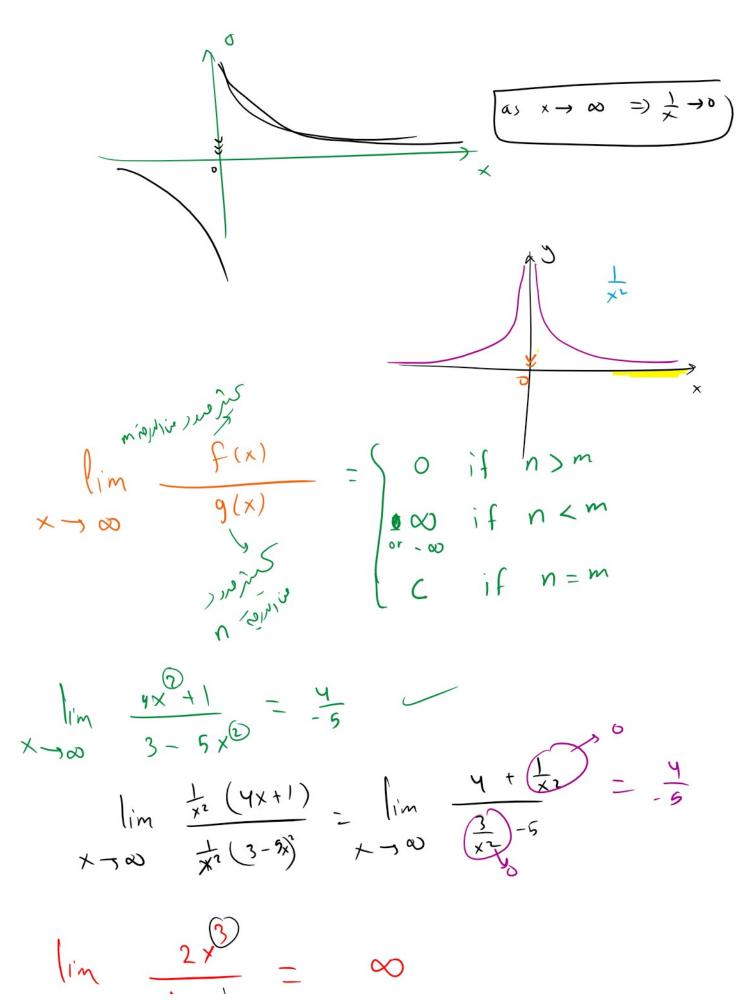
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$$\frac{\sin 2\theta}{\cos 2} = \frac{\sin 2\theta}{2\cos 2\theta} = \frac{\sin 2\theta}{2\cos 2\theta} = \frac{\cos 2\theta$$



$$\lim_{x \to \infty} \frac{2x^{2}}{1+x^{2}} = \infty$$

$$\lim_{x \to \infty} \frac{-2x}{1+x} = -\infty$$

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$$\lim_{x \to \infty} \frac{1}{1+x} = 0$$

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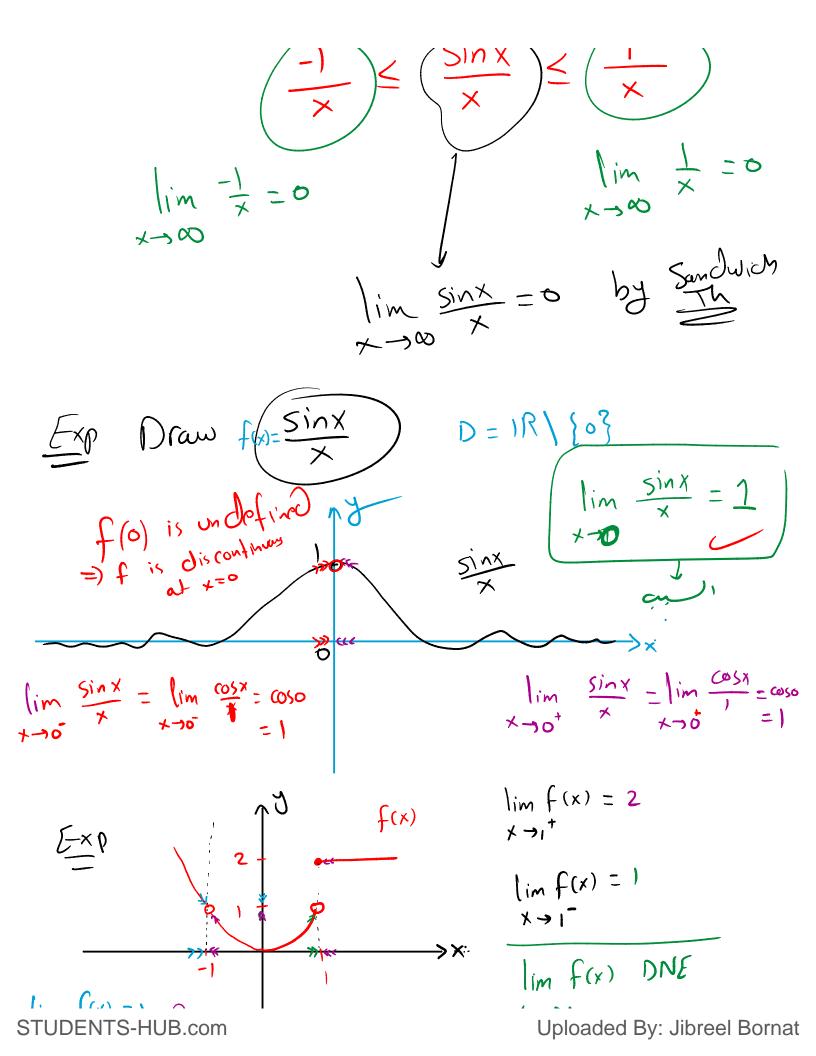
Assume
$$g(x) \le f(x) \le h(x)$$
 $\forall x \in [a, b]$

If $\lim_{x \to c} g(x) = \lim_{x \to c} h(x) = L$

Then $\lim_{x \to c} f(x) = L$
 $\lim_{x \to c} f(x) \le \frac{5 - 3x}{5}$
 $\lim_{x \to c} (5 + 3x) = 5 + 0 = 5$
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 $\lim_{x \to c$

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$$\lim_{x \to -1} f(x) = 1$$

JJ

 $\lim_{x \to 0} \frac{1}{x} = 0$

