

فيزياء ١٤١

الحل التفصيلي للدوائر الموجودة في

Test bank

إعداد الرباعي:

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لانسونا من صالح وحاتم بظهر الغيب

CHAPTER 1

- 1) (Ans: E) from the book "None"
- 2) (Ans: B) "ns" nanosecond = 10^{-9} s
from the book
- 3) (Ans: E) the speed of light
from the book
- 4) (Ans: C) The Def. relates the current ...
- 5) (Ans: C) 1 yard = $\frac{3600}{3937}$ meters
1 yard = 0.914 \approx 1 m.
- 6) (Ans: D) "can be expressed in terms of m^2 "
- 7) (Ans: C) kg
- 8) (Ans: B) 1 kg = 10^{-3} kg
- 9) (Ans: B) 1 pound = 0.453 kg
* "خطأ في الجواب" \approx 0.5 كجم
- 10) (Ans: C) $(5.0 \times 10^4)(3.0 \times 10^6) =$
 $= (5.0 \times 3.0) 10^{6+4}$
 $= 1.5 \times 10^{10} = 1.5 \times 10^{10}$
- 11) (Ans: B) " 1.5×10^{-1} "
the same as 10
- 12) (Ans: E) $5.0 \times 10^5 + 3.0 \times 10^6 =$
 $= 0.5 \times 10^6 + 3.0 \times 10^6 =$
 $= 3.5 \times 10^6$
- 13) (Ans: E) $(7.0 \times 10^6) / (2.0 \times 10^6) =$
 $(\frac{7.0}{2.0}) 10^{6-6} = 3.5 \times 10^0$
- 14) (Ans: B) 0.00150 "3" signi. nom.
- 15) (Ans: C) 15.0 "3" signi. nom.
- 16) (Ans: C) $3.2 \times 2.7 = 8.64$
 $8.64 \approx 8.6$
- 17) (Ans: B) $1.51\bar{3} + 27.3 =$
 $= 28.8\bar{3} \approx 28.8$ ^{least}
- 18) (Ans: B) 1 mi = 1609 m
55 = y m
 $y = 55 \times 1609 = 88.495$ me
 $88.495 \text{ meter/h} = \frac{88.495 \text{ meter}}{3600 \text{ s}}$
 $= 24.58 \approx 25$
- 19) (Ans: A) $V_{\text{sphere}} = \frac{4}{3} \pi r^3$
 $= (\frac{4}{3})(3.14)(1.7 \times 10^{-2})^3$
 $= 20.569 \approx 2.1 \times 10^{-5} \text{ m}^3$
- 20) (Ans: C) $A_{\text{sphere}} = 4 \pi r^2$
 $= (4)(3.14)(1.7 \times 10^{-2})^2$
 $= 3.6298 \approx 3.6 \times 10^{-3} \text{ m}^2$

Ans: D

$$\begin{aligned}
 21) V_{\text{cylinder}} &= (\text{Area of base}) (\text{height}) \\
 &= (\pi r^2) (h) \\
 &= (\pi) (2.3 \times 10^{-2})^2 (1.4) \\
 &= 2.3 \times 10^{-3} \text{ m}^3
 \end{aligned}$$

$$\begin{aligned}
 22) \text{Ans: D} \quad A_{\text{cylinder}} &= 2 \times \text{Area base} + 2\pi rh \\
 &= 2\pi r^2 + 2\pi rh \\
 &= (2) (3.14) (2.3 \times 10^{-2})^2 + (2) (3.14) (2.3 \times 10^{-2}) (1.4) \\
 &= 5.344 \times 10^{-3} \text{ m}^2
 \end{aligned}$$

$$23) \text{Ans: B} \quad V_{\text{cube}} = L^3 = (1 \times 10^{-2})^3 = 10^{-6} \text{ m}^3$$

$$24) \text{Ans: B} \quad A_{\text{square}} = L^2 = (1 \times 10^{-2})^2 = 10^{-4} \text{ m}^2$$

$$\begin{aligned}
 25) \text{Ans: B} \quad 1 \text{ m} &\rightarrow 3.281 \text{ ft} \\
 1.5 \text{ ft} &\leftarrow y \text{ m} \\
 y &= \frac{1.5}{3.281} = 0.457 \\
 V_{\text{cube}} = L^3 &= (0.457)^3 = 0.0955 \\
 &\approx 0.096
 \end{aligned}$$

$$26) \text{Ans: D} \quad V = at^2 + bt^3$$

$\Rightarrow V$ is in m/s

So at^2 is in m/s

$$(a) (s^2) = \text{m/s}$$

$$a = \frac{s^3}{m}$$

$\Rightarrow bt^3$ is in m/s

$$(b) (s^3) = \text{m/s}$$

$$b = \frac{s^4}{m}$$

$$27) \text{Ans: A} \quad A = BC \Rightarrow B = \frac{A}{C}$$

$$B = \frac{L/m}{L/T} = T/m$$

$$\begin{aligned}
 28) \text{Ans: D} \quad A &= B^m C^n \\
 B &= L^2 T^{-1} / A = L T / C = L T^2 \\
 (L^2 T^{-1})^m (L T^2)^n &= L^1 T^1 \\
 L^{2m+n} T^{-m+2n} &= L^1 T^1 \\
 \begin{cases} 2m+n=1 \\ -m+2n=1 \end{cases} &\Rightarrow \boxed{1} \\
 \begin{cases} 2m+n=1 \\ -m+2n=1 \end{cases} &\Rightarrow \boxed{2}
 \end{aligned}$$

$$29) \text{Ans: B}$$

$$2 \times \boxed{1} - \boxed{2}$$

$$4n + 2m = 1$$

$$-(n + 2m = 1)$$

$$5n = 1 \quad n = \frac{1}{5}$$

$$(2)(\frac{1}{5}) + m = 1$$

$$m = 1 - \frac{2}{5} = \frac{3}{5}$$

$$m = \frac{3}{5}$$

1. $\Delta x = x_f - x_i$

So E because

$\Delta x = 4 - 4 = 8$ is the largest.

2. $\Delta x = x_f - x_i$

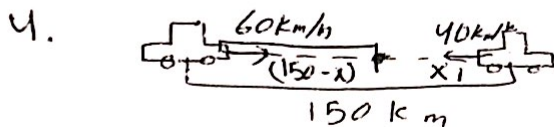
B because

$\Delta x = -8 - 4 = -12$
It is the only negative result.

3. $S_{avg} = \frac{\text{total distance}}{\Delta t}$

So B the distance

كل المسافة التي مشيتها
فترات الفترة على الفترة



~~So the average velocity is 0~~
~~at t = 0~~

$v_1 = 40 \text{ km/h} = 11.1 \text{ m/s}$

$v_2 = 60 \text{ km/h} = 16.7 \text{ m/s}$

$x_1 = v_1 t + \frac{1}{2} a t^2$

$x_1 = 16.7 t$

$x_2 = 150 \times 10^3 - x_1$

$x_2 = 150 \times 10^3 - v_2 t - \frac{1}{2} a t^2$
 $= 150 \times 10^3 - 16.7 t$

$150000 - 16.7 t = 11.1 t$

$150000 = 27.8 t$

$t = \frac{5402.5}{3600}$

$= 1.5 \text{ h}$

5. $S_{avg} = \frac{\text{total distance}}{\Delta t}$

$S_1 = \frac{d_1}{\Delta t_1}$

$\Delta t_1 = \frac{d_1}{S_1} = \frac{40}{80} = \frac{1}{2} \text{ h}$

$\Delta t_2 = \frac{d_2}{S_2} = \frac{40}{40} = 1 \text{ h}$

the total time = $\frac{1}{2} + 1 = 1.5 \text{ h}$
على أساس أن المسافة هي 80 كم
1.5 ساعة

$S_{avg} = \frac{80}{1.5} = 53.3$
D



$v_{avg} = \frac{\Delta x}{\Delta t}$

و على ان سرعة السيارة

تبقى ثابتة

$\Delta x = 0$

$v_{avg} = 0$ لأن

$$7. \text{ } S_{\text{avg}} = \frac{d}{\Delta t} = \frac{50+50}{2} \text{ km}, 50 \text{ km/h}$$

(B)

$$8. x(t) = 16t - 30t^3$$

$$v(t) = 0$$

$$v(t) = x' = 16 - 90t^2$$

$$16 - 90t^2 = 0$$

$$90t^2 = 16$$

$$t^2 = \frac{16}{90}$$

$$t = \frac{4}{3} = 1.33$$

(B)

$$9. v = bt^2$$

$$v = \frac{dx}{dt}$$

$$\int_0^t dx = \int_0^t v dt$$

$$x = \int_0^t bt^2 dt$$

$$x(t) = \frac{b}{3} t^3$$

(B)

$$10. a_{\text{avg}} = \frac{\Delta v}{\Delta t} = \frac{v(8) - v(3)}{8 - 3}$$

$$= \frac{0 - 20}{8 - 3} = -4 \text{ cm/s}^2$$

(B)

$$(11), x = 7t - 3t^2$$

$$v_{\text{avg}} = \frac{\Delta x}{\Delta t} = \frac{x(4) - x(0)}{4}$$

$$= \frac{-20 - 0}{4} = -5 \text{ m/s}$$

(B)

$$(12) v = 4t - 3t^2$$

$$x = \int v \cdot dt$$

$$\int 4t - 3t^2 \cdot dt$$

$$x = 2t^2 - t^3$$

$$v_{\text{avg}} = \frac{\Delta x}{\Delta t} = \frac{x(2) - x(0)}{2}$$

$$= \frac{8 - 8 - 0}{2} = \frac{0}{2} = 0$$

(A)

(B)

$$x = 4t^2 - 3t^3$$

$$v = 8t - 9t^2$$

$$a_{\text{avg}} = \frac{\Delta v}{\Delta t}$$

$$= \frac{v(2) - v(0)}{2}$$

$$= \frac{16 - 36 - 0}{2}$$

$$= -10 \text{ m/s}^2$$

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14. ~~14.1~~

16

particle 1, 2
ثابت التغير
بسرعة ثابتة

$$(3) \Rightarrow 3.5 + 2.7t + 2$$

$$v = 5.4t$$

$$a = 5.4 \text{ m/s}^2$$

$$(4) \Rightarrow 3.5 - 3.4t - 2.7t^2$$

$$v = -3.4 - 5.4t$$

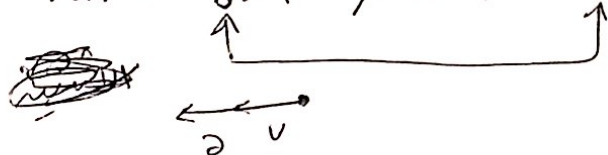
$$a = -5.4 \text{ m/s}^2$$

so only 3 and 4

(D)

15. particle 1 = $x(t) = 3.5 - 2.7t^3$

$$v(t) = -8.1t^2 / a(t) = -16.2t$$



الاجم يتجه بالاتجاه السالب والسرعة
سالب و التارم يتغير الاتجاه
اذن عم يتزايد سرعته

particle 2 $\Rightarrow x(t) = 3.5 + 2.7t^3$

$$v = 8.1t^2 / a(t) = 16.2t$$



فتر الاشارة
بعد بالاتجاه الموجب

particle 3 = $3.5 + 2.7t^2$

$$v = 5.4t \quad a = 5.4$$

فتر الاشارة
وتكون ثابتة

$v_0 = 0$ ~~constant~~ $a = 4 \text{ m/s}^2$

$$v_{avg} = \frac{\Delta x}{\Delta t}$$

~~$x = v_0 t + \frac{1}{2} a t^2$~~
 ~~$x = 0 + \frac{1}{2} (4) t^2$~~
 ~~$x = 2t^2$~~

~~$x = 2t^2$~~
 ~~$x = 2(1)^2$~~
 ~~$x = 2$~~

$$x = v_0 t + \frac{1}{2} a t^2 + \frac{1}{2} a t^2$$

$$2 = 2t^2 + 2$$

$$t = 1 \text{ s}$$

~~8~~

$$8 = 2t^2$$

$$t^2 = 4$$

$$t = 2$$

$$v_{avg} = \frac{\Delta x}{\Delta t}$$

$$= \frac{8 - 2}{2 - 1} = 6 \text{ m/s}$$

17 E

متغير يكون جسم متحرك
تغير بين سرعة ثابتة
ثابتة
لا تزداد

$$a = \frac{dv}{dt}$$

18 C

S increase

(B) $a \neq 0$ and $a \neq v$

in the same direction

لا يتزايد لانهم يتحركون بنفس الاتجاه

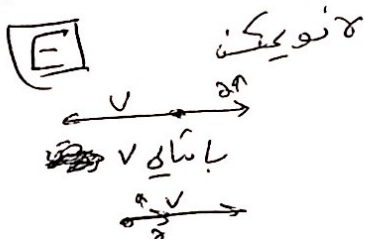
والجواب الوصف السري الاثر

(C) negative & negative

والاثر speed ثابت عند كل الاثا

فما يتبين الاثارة

19



من شرط ان يكون

(E)

20 $y = at - bt^2$

y position L

$a \rightarrow \frac{L}{T}$ $b \rightarrow \frac{L}{T^2}$

(C)

2

21

$x = 6t^2$

(E) لا نو ولا ديرة

$a = 12t$

تبقى الاغوات سابه
مشرعان $6t^2$ خارج
لكن سابه

و بمانه خارج
يكون سابه ثمان صيد ينتقل
لارج يكون

$a = 12t$

22

$x(t) = 27t - 4t^3$

$v = 27 - 12t^2$

$a = -24t$

$a(1) = -24 \text{ m/s}$

23

$x(t) = 27t - 4t^3$

$v(t) = 27 - 12t^2$

$v(0) = 27$

$a(t) = -24t$

$a(0) = 0$

(C)

24

$v = 16 \text{ m/s} \rightarrow t = 0$

$a = -0.5t$

$a = \frac{dv}{dt}$

$v = \int a dt$

$v = -0.5t^2 + c$

24) $V = -0.25t^2 + c$

$V(0) = c$

$c = 16$

$V = -0.25t^2 + 16$

$-0.25t^2 + 16 = 0$

$0.25t^2 = 16$

$t^2 = 64$

$t = 8$

D

25) $\frac{24}{\text{سفر السوان}}$

$V = -0.25t^2 + 16$

$X = \int_0^t V \cdot dt$

$\Delta X = \frac{-0.25}{3} t^3 + 16t$

$\Delta X = 58.7 = 59 \text{ m}$

E

26) $\frac{24, 52}{\text{سفر السوان}}$

$\frac{1}{2} t \text{ stopped}$

$t = 8$

so $\Delta X = \frac{-0.25}{3} t^3 + 16t = 85$

D

27) $V(t) = 98 - 2t^2$

$98 - 2t^2 = 0$

$2t^2 = 98$

$t^2 = 49$

$t = 7$

$a(t) = -4t$

$= -4 \times 7 = -28 \text{ m/s}^2$

D

28) $x(t) = 75t - t^3$

$V(t) = 75 - 3t^2$

$75 - 3t^2 = 0$

$3t^2 = 75$

$t^2 = 25$

$t = 5$

$a(t) = -6t$

$= -6 \times 5 = -30 \text{ m/s}^2$

C

29) 20 m in 4s

$\Delta x = v_0 t + \frac{1}{2} a t^2$

$20 = 0 + \frac{1}{2} a (16)$

$a = \frac{20}{8} = 2.5 \text{ m/s}^2$

C

(3)

$$\boxed{30} \quad v^2 = v_0^2 + 2ax$$

$$2500 = 100 + 2(60)a$$

$$2400 = 120a$$

$$a = 20 \text{ m/s}^2$$

$$v = v_0 + at$$

$$50 = 10 + 20t$$

$$40 = 20t$$

$$\boxed{t = 2s}$$

(A) ~~جواب~~

(B) ~~جواب~~

$$S_{avg} = \frac{d}{\Delta t}$$

$$\frac{10450}{2} = \frac{60}{\Delta t}$$

$$30 = \frac{60}{\Delta t}$$

$$\boxed{4t = 2s}$$

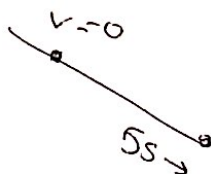
جواب

$$\boxed{31} \quad a = 5 \text{ m/s}^2$$

$$v = v_0 + at$$

$$= 5 \times 5 = 25 \text{ m/s}$$

(C)



$$\boxed{32} \quad v_0 = 25 \text{ m/s} \uparrow$$

$$a = 3 \text{ m/s}^2 \downarrow$$

$$v = v_0 + at$$

$$v = 25 - 3(6)$$

$$25 - 18 = 7 \text{ m/s}$$

(A)

$$\boxed{33} \quad v_0 = 12 \text{ m/s} \leftarrow$$

$$a = 4 \text{ m/s}^2 \leftarrow$$

$$\Delta x = v_0 t + \frac{1}{2} a t^2$$

$$\Delta x = 12(3) + \frac{1}{2}(4)(3)^2$$

$$= 36 + 18 = 54 \text{ m}$$

(D)

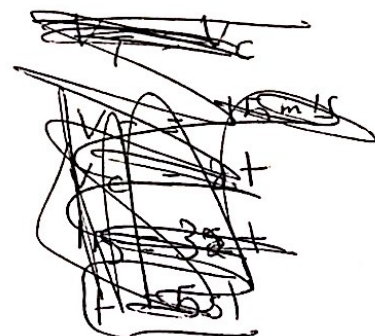
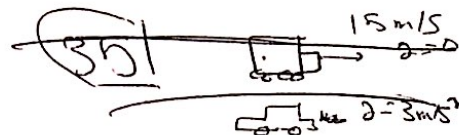
$$\boxed{34} \quad v_0 = 2 \text{ m/s} \quad t = 6s$$

$$a = 2 \text{ m/s}^2$$

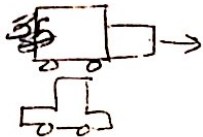
$$\Delta x = v_0 t + \frac{1}{2} a t^2$$

$$= 12 + 36 = 48 \text{ m}$$

(E)



(35)



$$X_T = X_C$$

~~$$v_T t + \frac{1}{2} a t^2 = v_C t + \frac{1}{2} a t^2$$~~

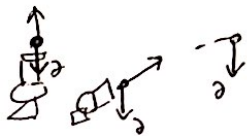
$$v_T t = \frac{1}{2} a t^2$$

$$15 = \frac{3}{2} t$$

$$t = \frac{30}{3} = 10s$$

(B)

(36)



downward

دائماً يكون التسارع
كان في الهواء
في السقوط. (A)

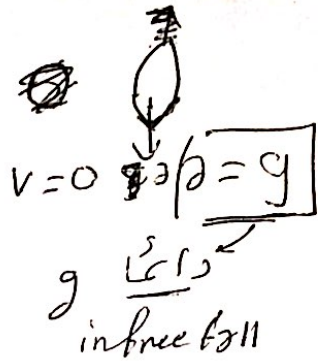
(37)

$$\begin{aligned} \Delta X &= x_2 - x_1 \\ &= x_2 - x_1 \\ &= + \end{aligned}$$

ascent
النور
104

$$\begin{aligned} \text{descent } \Delta X &= x_2 - x_1 \\ &= x_1 - x_2 \\ &= - \end{aligned}$$

(38)



(39)

$$v_{avg} = \frac{\Delta x}{\Delta t}$$

$$\Delta x = v_0 t + \frac{1}{2} a t^2$$

$$\Delta x = 4.9 + 2$$

$$\Delta x(10) = 4.9$$

$$v_{avg} = \frac{4.9 - 0}{1} = 4.9 \text{ m/s}$$

(A)

لا نواكب
بسط كل ثانية بمقدار 4.9

(C)

acceleration is
constant and
 $a = 9.8$

ما تبقى كل ثانية بمقدار 9.8

(D) \propto بمقدار 4.9
في الثانية 9.8m

(E) \propto 2 constant

دائماً بمقدار 2

$a = g$

و ما تبقى علاقة للوزن
بالمحصول

40 [C] $a = 9.8 \text{ m/s}^2$

ازن السرى رح تزداد
كل ثانية بمقدار 9.8

$$v = 0 + 9.8t$$

$v = 9.8t$ [C] ✓

وبما انه سقوط اذن

رح يكون اتجاه السرى للاسفل عشان
فصيل رح تزايد فى مقدار
زى جواب [E]

41

↓ 1 m/s

$$\Delta x = v_0 t + \frac{1}{2} g t^2$$

$$= 1(5) + \frac{1}{2} 9.8(5)^2$$

$$= 5 + 122.5$$

$$= 127.5 \text{ m}$$

ة نو v و a بنفس الاتجاه
بتكون الإشارة +

[B]

45

↑ 35 m/s

$$v = v_0 + at$$

$$v = 35 - 10(5)$$

$$= 35 - 50 = -15 \text{ m/s}$$

15 down

[B]

41

↑ v

[B]

↑ v

↓ a

رائعاً بتكون للاسفل

42

↑ 50 m/s

y_0 (level ground)

$$\Delta x = v_0 t - \frac{1}{2} g t^2$$

$$x = 50(1) - 5(1)$$

$$= 45 \text{ m}$$

[B]

نفس السواد

43

$$x = 50(8) - 5(8)^2$$

$$= 300 - 180$$

$$= 120 \text{ m}$$

[E]

و 80 م

46

[C]

لا تزداد

دائماً بمقدار ثابتة بالسقوط الحر

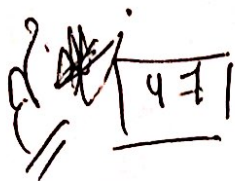
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$$\Delta x = v_0 t + \frac{1}{2} g t^2$$

~~$$\Delta x = v_0 t + \frac{1}{2} g t^2$$~~
~~$$= 9.8(1)^2$$~~
~~$$= 9.8$$~~
~~$$\Delta x = 9.8(2)^2$$~~
~~$$= 19.6$$~~

~~$$\Delta x = 34.3$$~~

~~$$\Delta x = 4.9(2)^2$$~~
~~$$= 19.6$$~~



$$v(1) = v_0 + gt = g$$

$$v(2) = v_0 + g(2) = 2g$$

$$v_{avg} = \frac{2g + g}{2} = \frac{3g}{2}$$

Distance moved in second

$$\text{second is } \frac{3g}{2} \times 1 = \frac{3g}{2} = \frac{3 \times 10}{2} = 15 \text{ m}$$

$$v_{avg} = \frac{\Delta x}{\Delta t}$$

$$v_{avg} \Delta t = \Delta x$$

(C)

الارتفاع

$$v_0 = 0$$

$$v(4) = v_0 + g(4) = 4g$$

$$v(3) = 3g$$

$$v_{avg} = \frac{(4+3)g}{2} = \frac{7}{2}g$$

$$v_{avg} = \frac{d}{\Delta t}$$

$$d = v_{avg} \cdot \Delta t$$

$$= \frac{7}{2}g \times 4 = 34.3 \text{ m}$$

(D)

49



على الارتفاع
تتركه القذبة

بالسلي لا يوفه

شارع صناعي شارع الجاز

(5)

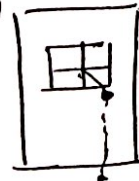
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ما انه اطلقنا
من الارتفاع
يتكون بنفس
 $v_0 = 10 \text{ m/s}$

$$v = v_0 + gt = 10 + 9.8(20) = 206 \text{ m/s}$$

51



$$\Delta x = v_0 t + \frac{1}{2}gt^2 = 0 + \frac{1}{2}(9.8)(12)^2 = 705.6 \text{ m}$$

(E)

52

$$\Delta x = v_0 t + \frac{1}{2}gt^2 = 1.75 = \frac{1}{2}(9.8)t^2$$

$$t^2 = 35.7$$

$$t = 5.9 = 6 \text{ s}$$

(C)

53

$$v_0 = 19.5 \text{ m/s}$$

$$\Delta x = v_0 t + \frac{1}{2}gt^2$$

$$\Delta x = 19.5t - 4.9t^2$$

$$v_{top} = 0$$

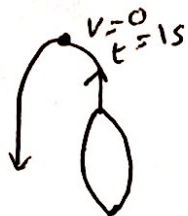
$$v = v_0 + gt$$

$$v_0 = gt$$

$$t = \frac{19.5}{9.8} = 1.98 \text{ s}$$

$$\Delta x = 39 = 19.6 \times 1.98$$

54



25

$10 \pm gt$

~~$v = v_0 + gt$~~

$v = v_0 + gt$

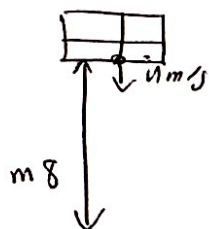
$v_0 = 9.8 \text{ m/s} = 9.8 \text{ m/s}$

$\Delta x = v_0 t - \frac{1}{2} g t^2$

$\Delta x = 9.8 t - 4.9 t^2$
 $= 9.8(1) - 4.9(1) = 4.9$

(A)

55



$\Delta x = v_0 t + \frac{1}{2} g t^2$

$8 = 4t + 4.9 t^2$

$4.9 t^2 + 4t - 8 = 0$

$t = \frac{-4 \pm \sqrt{16 + 156.8}}{9.8}$
 $= \frac{-4 \pm 13.145}{9.8}$

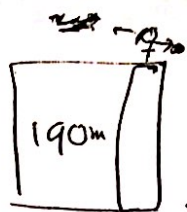
$t = 0.93$

~~$t = -1.97$~~

لا نه ساله

(B)

56



~~$v = v_0 + gt$~~

$v^2 = v_0^2 + 2gX$

$v^2 = 0 + 2g(190)$

$v = 61 \text{ m/s}$

(B)

57



$a_n = 19.6 = 2g$

~~$\Delta x_n = v_0 t - \frac{1}{2} g t^2$~~

~~$= v_0 t - \frac{1}{2} g t^2$~~

~~$v = v_0 - gt$~~
 ~~$v_0 = 2gt$~~

~~$= 2gt^2 - \frac{1}{2} g t^2$~~

~~$\Delta x_n = \frac{3}{2} g t^2$~~

~~but $v_0 = 2gt$ is not the same~~

~~$\Delta x_n = v_0 t - \frac{1}{2} g t^2$~~

~~$= 2gt^2 - \frac{1}{2} g t^2$~~

~~$\Delta x_n = \frac{3}{2} g t^2$~~

$\Delta x_n = v_0 t - \frac{1}{2} a_n t^2$

$\Delta x_n = v_0 t - \frac{1}{2} g t^2$ where $a_n = 2g$

$\Delta x_n = v_0 t - \frac{1}{2} g t^2$

السنه

في الارض راجع يتبع احوال جاذبية من الكوكب انا

لا نه ساله

[58] $v_e^2 = v_i^2 - 2gx$

case 1 $0 = v_i^2 - 2(100)g$

① — $v_i^2 = 200g$

case 2

$v^2 = (2v_i)^2 - 2gx$

$0 = 4v_i^2 - 2gx$

$4v_i^2 = 2gx$

$x = \frac{4(200g)}{2g}$

$= 400m$

(E)

[59]

↑ 100m/s ↓ 10m/s

$v_f^2 = v_i^2 - 2gx$

~~0~~

$x = \frac{v_i^2}{2g}$

$x_1 = \frac{10000}{2g}$

$x_2 = \frac{100}{2g}$

$\frac{x_1}{x_2} = 100$

(B)

[60]

~~$v = \frac{dx}{dt}$~~

$dx = v dt$

$x = \int v dt$

displacement

[61]

(D) انتافس

[62]

$a = 3 m/s^2$

~~$a = \frac{dx}{dt}$~~

$dx = a dt$

$v = \int_0^t 3 dt$

$v = 3t$

but $v = \frac{dx}{dt}$

$x = \int_0^t v dt$

$= \int_0^t 3t dt$

$x = \frac{3}{2} t^2$

So it is increase with time

نفر فکریہ سوال [76]
[75]

میکرہ الجواب

کالو [C]

$v \propto t$
بہت زیادہ مع الہافن

[77] ↑

$$v = u + gt$$

When $t = 0$

$$v = u$$

والرکھ الوصیہ
ای مشر بیلہ

منا نقمہ الاصل

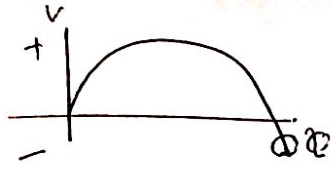
[C]

وصیہ

~~Handwritten scribbles~~

70

E



يكون الشارة \oplus باساره
عشان حيله بتتلا راسه ولان
بالا اتجاه العكس

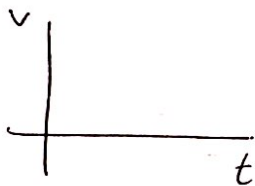
71

C

باتسارع

لان الميل موجب

72



$\Delta x = \int v \cdot dt$

= Area under the curve

$$= 3 \times 12 = 36 \text{ m}$$

D

73

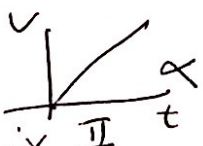
A

لان ميله متساوي

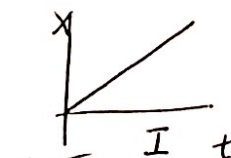
لعدة نفس بره شانه وبعدين بتساوي

$$a = \frac{dv}{dt} = \frac{12-0}{2-0} = 6 \text{ m/s}^2$$

74



لانو اسرعه
بتزداد مع الزمن



بتساوي وبعدين اسرعه تزداد

75

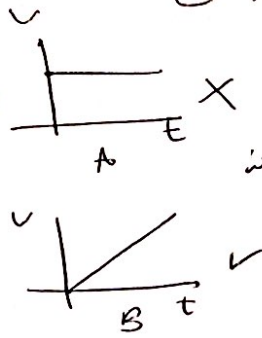
↓

$$v_i = 0$$

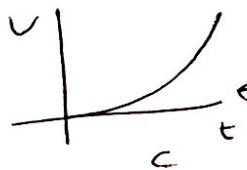
$$v = gt$$

$$y = \frac{1}{2}gt^2$$

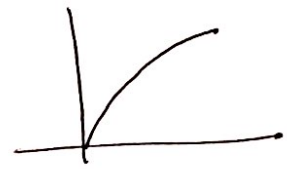
$$v^2 = 2gx$$



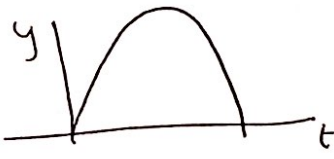
لان
 $v \propto t$
بتزداد مع الزمن



$v \propto t$
 ~~$v \propto t^2$~~
فنا



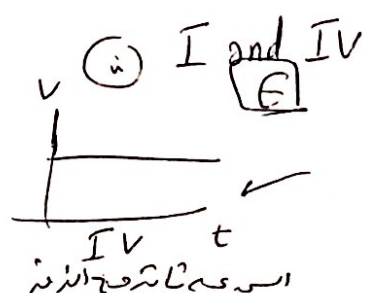
$\propto \sqrt{v \propto t}$



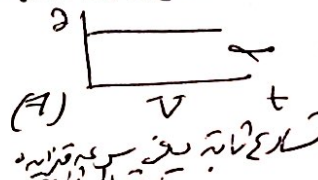
$$y = \frac{1}{2}gt^2$$

وبعانه
اشنا الاتجاه
اسرعه موجب اوله
يكون القطع المتكافئ
ورج يكون نفسه فقط

B



اسرعه ثابتة مع الزمن



تساوي ثابته يعني سرعه ثابته
بتساوي ثابته

By: Lara Sami

Chapter 3: Vectors

Test bank solutions

1 Ans: B

$\Rightarrow \infty$

2 Ans: D

3 Ans: A

$\Rightarrow \infty$

4 Ans: C

$\Rightarrow \infty$

The magnitude of the resultant must be somewhere between 5 and 45. Only 12 satisfy this.

5 Ans: A

Because

$$T + 6 > 12$$

$$\text{so } T > 6$$

$$\text{and } T - 6 < 12$$

$$\text{so } T < 18$$

6 Ans: D

7 Ans: ~~B~~ C

$$\vec{V}_1 + \vec{V}_3 = \vec{V}_2$$

$$\text{so } \vec{V}_3 = \vec{V}_2 - \vec{V}_1$$

8 Ans: E

9 Ans: A

10 Ans: B

11 Ans: B

"قوسا" apes

12 Ans: C

13 Ans: D

$$y = 12 \sin 30^\circ$$
$$\text{component} = -6$$

14

Ans: A

15 Ans: D

$$4 \times \sqrt{100} = 4 \times 10 = 40$$

$$16 \text{ Ans: B } \neq \sqrt{(10)^2 + (10)^2 + (5)^2}$$
$$\neq 15$$

17

$$\text{Magnitude} = \sqrt{(2)^2 + (6)^2 + (3)^2} = 7 \text{ Ans: C}$$

18

$$25 \cos \theta = 12 \Rightarrow \theta = 61^\circ \text{ Ans: C}$$

19

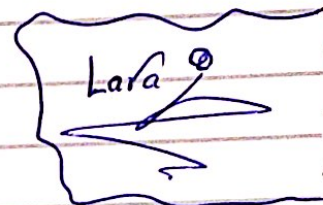
$$\theta = \tan^{-1} \frac{45}{25} = 61^\circ \text{ Ans: B}$$

20

$$\theta = \tan^{-1} \frac{45}{25} = 61^\circ \Rightarrow \theta = 180 - 61 = 119 \text{ Ans: C}$$

21) Ans: A $S = (2+4)\hat{i} + (6+2)\hat{j} + (-3+1)\hat{k}$

22) Ans: B $D = (2-4)\hat{i} + (6-2)\hat{j} + (-3-1)\hat{k}$
 $= -2\hat{i} + 4\hat{j} - 4\hat{k}$



23) Ans: A $= (2\hat{i} - 3\hat{j}) - (2(1)\hat{i} - 2(2)\hat{j})$
 $= 2\hat{i} - 3\hat{j} - 2\hat{i} + 4\hat{j} = +1\hat{j}$

24) Ans: C $(A+B)_x = A \cos \theta + B \cos \theta = 12(\cos 45) + B(\cos 60) \approx 12$

25) $A \cos \theta = 4 \quad \text{--- (1)} \quad \tan \theta = \frac{10}{4} \quad \theta = 68^\circ$
 $A \sin \theta = 10 \quad \text{--- (2)} \quad \text{Then } A = \frac{4}{\cos \theta} = 10.7$

Finally $A \cos \theta_2 = 8 \Rightarrow (10.7) \cos \theta_2 = 8 \Rightarrow \cos \theta = \frac{8}{10.7} \Rightarrow \theta_2 = 41.6$

So the y component $= A \sin \theta_2 = 10.6 \sin 41.6 \approx 7.2$

Ans: B

26) Ans: C $A \cdot B = |A| |B| \cos \theta = (L)(L) \left(\frac{\sqrt{3}}{2}\right) = \frac{\sqrt{3} L^2}{2}$

27) Ans: D $\vec{A} \cdot \vec{B} = (2)(4) + (6)(2) + (-3)(1) = 17 \text{ m}^2$

28) Ans: C $A \cdot B = (10)(15) \cos 65^\circ = 63 \text{ m}^2$

29) Ans: D $AB \cos \theta = A \cdot B$
 $(3)(5) \cos \theta = (1)(3) + (2)(4) = 11 \Rightarrow \cos \theta = \frac{11}{15}$
 $\theta = \cos^{-1} \frac{11}{15}$

30) Ans: D $\cos(B) = -\cos(B+20)$ so $B + B + 20 = 180$
 $2B = 160$
 $B = 80^\circ$

31 Ans: A 32 Ans: E 33 Ans: C $AB \sin \theta$

مع

34 Ans: B $\sin(\theta + 20) = 2 \sin \theta$

بتجربوا الخيارات بالآلة الحاسبة

والخيار اللي يربط بتختاروه وهون 18° الصح

ف

35 Ans: E

اجته بظهور

36
$$\begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 3 & -2 & 0 \\ 2 & 3 & -2 \end{vmatrix} = \hat{i}(4-0) + \hat{j}(-6-0) + \hat{k}(9-4)$$

$$= 4\hat{i} - 6\hat{j} + 5\hat{k}$$

Ans: A

منه

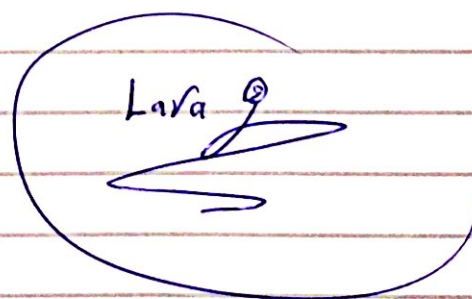
37 Ans: E

38 Ans: B

$\hat{i} \cdot (\hat{j} \times \hat{k}) = \hat{i} \cdot \hat{i} = 1$

39 Ans: A $\hat{k} \cdot (\hat{k} \times \hat{i}) = \hat{k} \cdot \hat{j} = 0$

لا تنسونا من دعائكم بفاهر الغيب



Chapter 4

اعداد: ونام: مكاوي

$$1. v = \frac{dx}{dt} = \frac{ax}{a}$$

معدل التغير في الارتفاع
بالنسبة لوقت

7



$$2. a = \frac{dv}{dt}$$

معدل التغير في السرعة
بالنسبة لوقت

C

3. speed (non vector
quantity) قياس

4. E ولة وحدة
كمية متجهة

5. E الحركة الانتقالية

المختزنات دائما يتكون

تغير السرعة والسرعة

اذن (السرعة)

$$a. r = -2\hat{i} + 3\hat{j} + 1\hat{k}$$

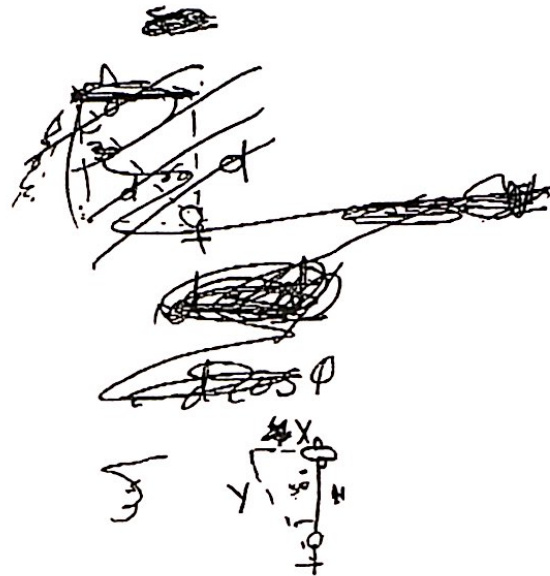
to

$$r = 3\hat{i} - 1\hat{j} + 4\hat{k}$$

$$\Delta r = r_2 - r_1$$

$$\Delta r = 5\hat{i} - 4\hat{j} + 3\hat{k}$$

B



$$\cos 30 = \frac{H}{Y}$$

Y it is the distance
that sound waves
have traveled

$$Y = \frac{H}{\cos 30}$$

$$Y = \frac{H}{\frac{\sqrt{3}}{2}}$$

$$Y = \frac{2}{\sqrt{3}} H$$

but

X is the distance that
plane have traveled

$$\tan 30 = \frac{X}{H}$$

$$X = \tan 30 H$$

معادله

$$\delta = \frac{d}{dt}$$

و قطع سرعت و الطیاره عند المسند
بمنظر الزمان

$$X = \frac{1}{\sqrt{3}} H$$

$$Y = \frac{2}{\sqrt{3}} H$$

$$\frac{X}{Y} = \frac{1}{2}$$

plane

$$X = \frac{1}{2} Y$$

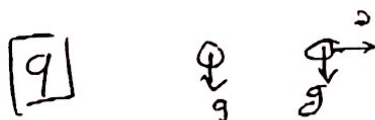
$$\frac{1}{\sqrt{3}} \div \frac{2}{\sqrt{3}} = \frac{1}{2}$$

[B] half the speed of sound.



$$\begin{aligned} \Delta V &= V_2 - V_1 \\ &= 200 - (-200) \\ &= 400 \text{ m/s south} \end{aligned}$$

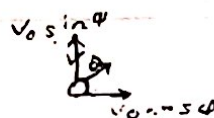
منه South به



بماند السارح الى اليمين
كان انقضى اذن ما بانر علوه
ضرب بالاربع فخرج يضربوا
المان

(A)

[10]



$$V_x = v_0 \cos \theta$$

$$V_y = v_0 \sin \theta$$

$$V_x = v_0 \cos \theta$$

$$V_y = v_0 \sin \theta$$

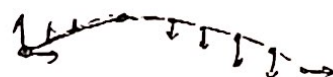
$$V_x = v_0 \cos \theta$$

$$V_y = v_0 \sin \theta$$

$$V_x = v_0 \cos \theta$$

$$V_y = v_0 \sin \theta$$

$$V_x = v_0 \cos \theta$$



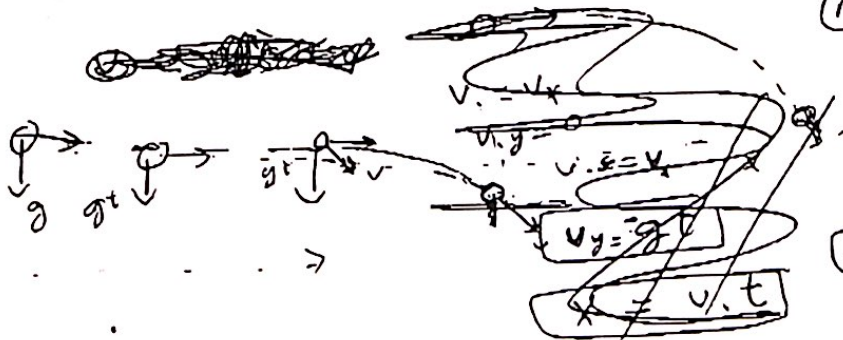
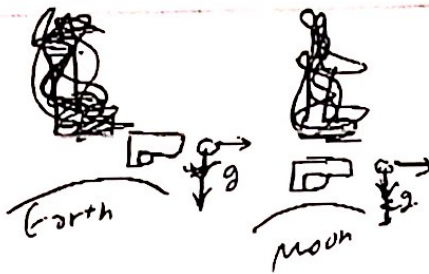
(D) constantly increasing downward velocity (gt)

- because the gravity will accelerate the object down which increase downward velocity. $V = U + gt$

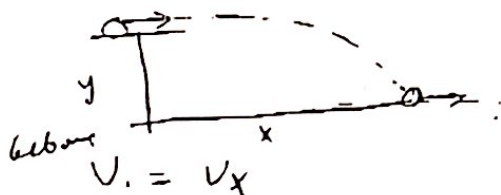
$$V = U + gt$$



(12)



المسألة عبارة عن الصمامات راجعاً أثروا
بجاذبية بتكون الجاذبية بالمر
اقتصر على الأرض من
إمكانه السياره يتطاعها الصمام
لأنه لا يكون الجاذبية
في الأرض والارتفاع أكثر
كان I and II



$$V_i = V_x$$

$$V_{y0} = 0$$

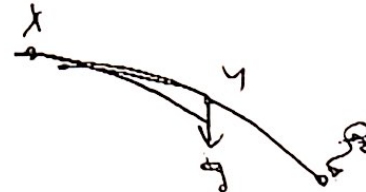
$$V_x = V_i$$

$$V_y = -gt$$

$$y = \frac{1}{2}gt^2$$

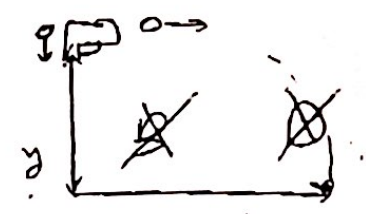
$$t = \sqrt{\frac{2y}{g}}$$

(13)



(A)

(14)



projectile
 $t = \sqrt{\frac{2y}{g}}$

dropped
 $y = \frac{1}{2}gt^2$
 $t = \sqrt{\frac{2y}{g}}$

(15)



CA
B ✓
D ✓
E ✓



$x = V_0 t = V_0 \sqrt{\frac{2y}{g}}$
 $t = \sqrt{\frac{2y}{g}}$

$V = V_0$

$x = V_0 t - \frac{1}{2}gt^2$

$x = V_0 \sqrt{\frac{2y}{g}}$

A ✓

C الجواب

(16)

$$y = v_0 \sqrt{\frac{2y}{g}}$$

$$x = \frac{1500}{36} \sqrt{\frac{2500}{10}}$$

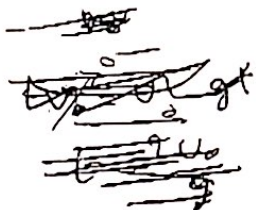
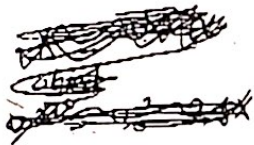
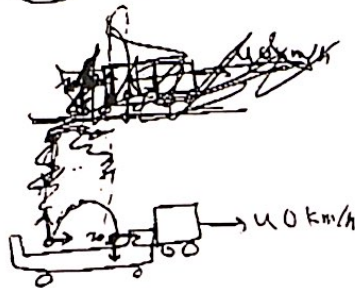
$$x = 41.7 \times 10$$

$$x = 417 \text{ m}$$

$$(C) \approx 420 \text{ m}$$

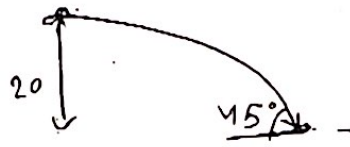
2/20

(17)



(C)

On the flatcar
because the object
has both horizontal
and vertical components
subject $\text{المركبة الأفقية لسرعة}$
 $\text{المركبة الرأسية لسرعة}$
اذن انما اعطينا سرعة ارتفاع وارتفاع
الارتفاع عليه



$$v_x = v_y$$

$$v \sin 45 = v \cos 45$$

$$v_x = v$$

I need to find (v_y)

$$v_{0y} = 0$$

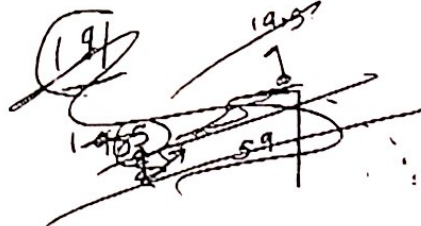
$$v_y^2 = v_{0y}^2 - 2gy$$

$$v_y^2 = 0 - 2g(20)$$

$$v_y^2 = -400$$

$$v_y = 20 \text{ m/s}$$

$$v_x = v_0 = 20 \text{ m/s}$$



$$v_y^2 = v_{0y}^2 + 2gy$$

$$v_y^2 = 38.03 + 118.88$$

$$v_y = 39.46$$

$$v_y = 39.46$$

$$39.46 = 19.5 - 10t$$

$$\frac{20}{10} = t$$

$$t = 2 \text{ s}$$

$$y = v_y t - \frac{1}{2} g t^2$$

$$y = 19.5 t - 5 t^2$$

$$-59.4 = 19.5 t - 5 t^2$$

$$5 t^2 - 19.5 t + 59.4 = 0$$

$$1 - 2 - 3.9 t + 11.8 = 0$$

$$3.9 \pm \sqrt{15.21 + 47.2}$$

$$3.9 \pm \sqrt{15.21 + 47.2}$$

2

$$\frac{3.9 \pm 7.9}{2}$$

$$t = 5.9$$

$$t = 6$$

$$20 \quad 80 \text{ m/s} \quad 30^\circ$$

$$v_x = 80 \times \cos 30^\circ = 848.7 \text{ m/s}$$

$$R = v_x t$$

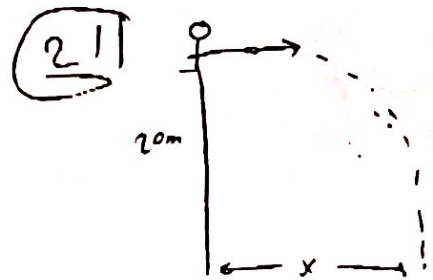
$$6 \text{ s}$$

$$0 = v_y \sin \theta - g t$$

$$t = \frac{80 \sin 30^\circ}{g} \Rightarrow t = 2 \times 50 = 100$$

$$t = 2 \times 50 = 100$$

(3)



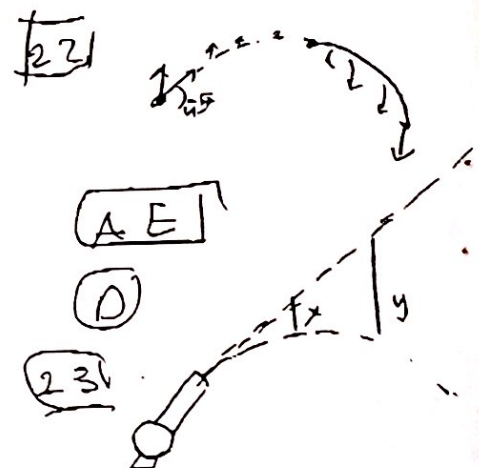
$$y = 20$$

$$y = v_y t - \frac{1}{2} g t^2$$

$$20 = \frac{1}{2} g t^2$$

$$t = 2 \text{ s}$$

$$x = v_0 t = 20 \times 2 = 40 \text{ m}$$



بجاء الكاز

$$v_x = v_0 \cos \theta$$

$$v_y = v_0 \sin \theta$$

بجاء الكاز

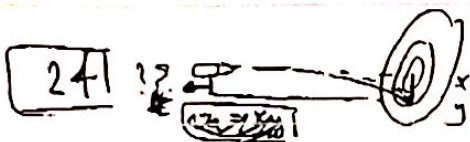
$$v_y = v_0 \sin \theta - g t$$

$$y = v_y t - \frac{1}{2} g t^2$$

$$y = \frac{1}{2} v_y t$$

$$v_{\text{net}} \cdot y = \frac{1}{2} g t^2$$

$$x = \frac{1}{2} \times 10 \times 5 \text{ m}$$

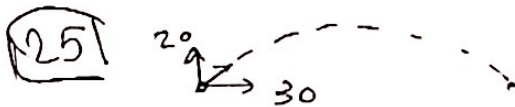


$$t = 1.5$$

$$y = \frac{1}{2} g t^2$$

$$y = \frac{1}{2} 10 (1.5)^2$$

$$y = 0.05 \text{ m}$$



$$v_y = v_{0y} - g t$$

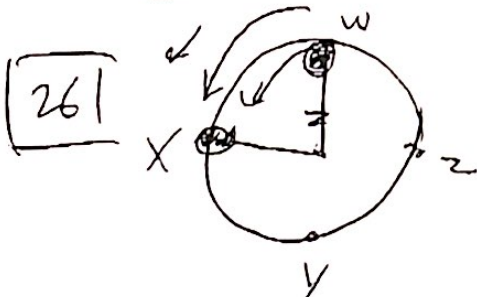
$$0 = 20 - 10 t$$

$$t = 2 \text{ s}$$

$$t_x = 2 \times 2 = 4 \text{ s}$$

$$x = v_x t$$

$$= 30 \times 4 = 120 \text{ m}$$



27

$$x = 0 \quad y = 3 \text{ m}$$

$$v = 6 \text{ m/s}$$

31

$$v = 6 \hat{j} \text{ m/s}$$

$$a = \frac{v^2}{r}$$

$$= \frac{6^2}{2} = 18 \text{ m/s}^2$$

28



$$v = 20 \text{ m/s}$$

$$a_y = \frac{v_2 - v_1}{\Delta t}$$

$$= \frac{20 \hat{j} + 20 \hat{j}}{\Delta t}$$

$$= \frac{20 \hat{j} + 20 \hat{j}}{\Delta t}$$

$$= \frac{\sqrt{240000}}{20}$$

$$= 14 \text{ m/s}^2$$



29

$$a_y = \frac{500 + 500}{40}$$

$$= \frac{1000}{40}$$

$$= 25 \text{ km/h}^2$$

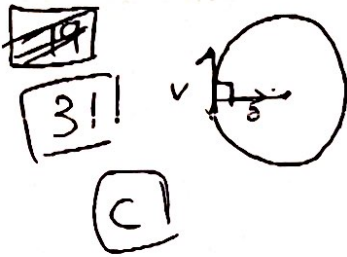
30



$$v = \frac{dx}{dt}$$

$$a_t = \frac{dv}{dt} = \frac{2\pi r}{t}$$

$$\Delta t = \frac{\pi^2}{2} \text{ s}$$



341



$$v = 4 \text{ m/s}$$

~~Range = 100~~

$$a = \frac{v^2}{R} = \frac{16}{25} = 32 \text{ m/s}^2 \text{ down}$$

32



$$v_2 = 2v_1$$

R same

$$a_1 = \frac{v_1^2}{R}$$

$$a_2 = \frac{v_2^2}{R}$$

$$\frac{a_1}{a_2} = \frac{v_1^2}{v_2^2}$$

$$4 a_1 = a_2$$

C1 ✓

33) a) how same 2

$$v_A = 2v_B$$

$$a_A = \frac{v_A^2}{R_A}$$

$$\frac{v_A^2}{R_A} = \frac{v_B^2}{R_B}$$

$$4 v_B^2 = v_A^2$$

$$\frac{4 v_B^2}{R_A} = \frac{v_B^2}{R_B}$$

$$4 R_B = R_A$$

35

$$a = \frac{v^2}{R} = \frac{16}{25} = 32 \text{ up m/s}^2$$

36

$$a = \frac{v^2}{R} = \frac{100}{20} = 5 \text{ m/s}^2$$

37



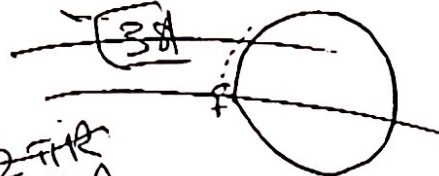
$$a = \frac{v^2}{R}$$

$$a = 28g$$

$$T = \frac{2\pi R}{v}$$

$$v^2 = aR$$

$$v = \sqrt{25g} = 16 \text{ m/s}$$



$$a = \frac{v^2}{R}$$

$$a = \frac{v^2}{R}$$

$$= 400$$

$$15.9$$

$$25 = \frac{v^2}{R}$$

$$25 = \frac{v^2}{R}$$

$$R = \frac{50}{v^2}$$

$$R = 15.9$$

$$T = \frac{2\pi R}{v}$$



39

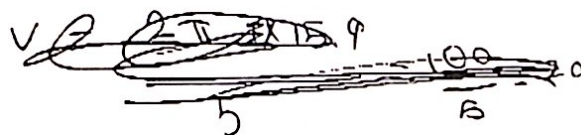


$$S = r\omega$$

$$\frac{\pi}{2} - \frac{3.14}{2} = 1.57 \text{ rad}$$

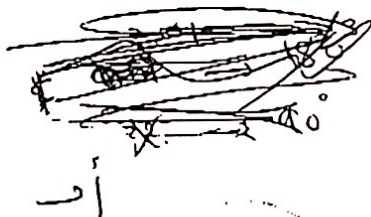


$$v = r\omega$$



$$\omega = \frac{\pi}{\frac{2}{7}} = \frac{\pi}{27} = 0.314 \text{ rad/s}$$

$$a = r\omega^2 = 15.9 (0.314)^2 = 1.57 \text{ m/s}^2$$



$$v = \frac{25}{5} = 5 \text{ m/s}$$

$$a = \frac{v^2}{r} = \frac{25}{15.9} = 1.57 \text{ m/s}^2$$

$$2\pi R = 25$$

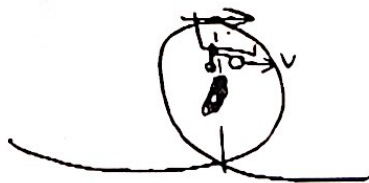
$$R = 15.9$$

40

$$R = 8$$

~~2.4 x 10^3~~

$$T = 10\text{ s}$$



$$T = \frac{2\pi R}{v}$$

$$v = \frac{2\pi R}{T}$$

$$= \frac{2 \times 3.14 \times 8}{10}$$

$$= 5 \text{ m/s}$$



$$R = vt$$

but

$$y = \frac{1}{2}gt^2$$

$$\frac{2 \times 16}{g} = t^2$$

$$t = 1.8 \text{ s}$$

$$R = 5 \times 1.8$$

$$= 9.1 \text{ m}$$

41



$$t_1 = \frac{x}{v}$$

$$t = \frac{3000}{(v_{\text{boat}} + v_r)}$$

$$\frac{3000}{25} = 120\text{ s}$$

$$t_2 = \frac{x}{v} = \frac{3000}{20.5}$$

$$t = t_1 + t_2 = 320\text{ s}$$

~~$$42 \quad v_{br} = 14 \text{ km/h}$$~~

~~$$v_{rb} = 6 \text{ km/h}$$~~

~~$$v_{mb} = 6 \text{ km/h}$$~~



~~$$v_{mb} = v_{rb} + v_{br}$$~~

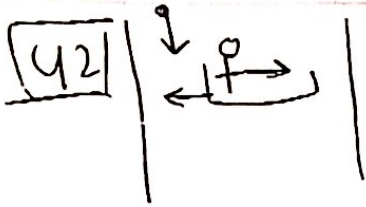
~~$$v_{mb} = v_{rb} + v_{br}$$~~

~~$$= 6 + 14$$~~

~~$$= 20 \text{ km/h}$$~~

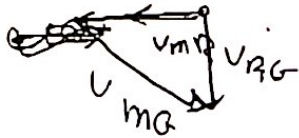
~~$$v_{mb} = v_{rb} + v_{br}$$~~

~~$$= 20 + 6 = 26 \text{ km/h}$$~~



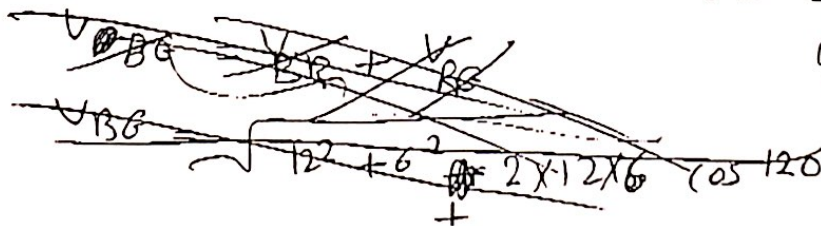
$$V_{MR} = V_{BR} - V_{MB}$$

$$V_{MR} = 14 - 6 = 8 \text{ km/h}$$

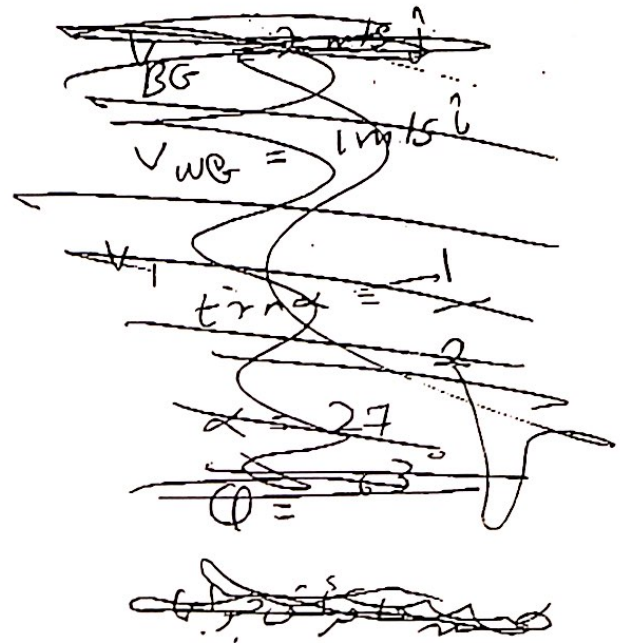
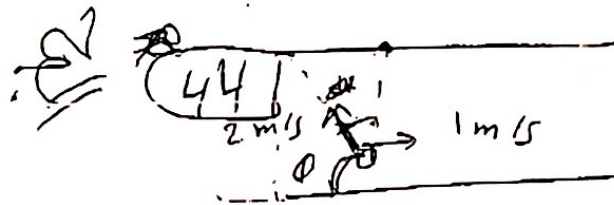


$$\begin{aligned} V_{MG} &= V_{RG} + V_{MB} \\ &= \sqrt{6^2 + 8^2} \\ &= 10 \text{ km/h} \end{aligned}$$

43

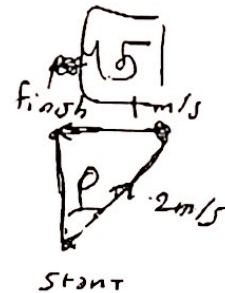


ازا كان القارب يح بصر 30°
من الناحية الخواص ازن هم
عم يقص منطه فراست
و عم برده صيرة كان
اسيار



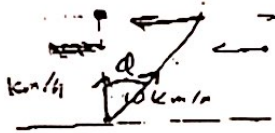
90° لائق

لما لاند وقتك
شتر بفرده (بوصه)
اسرر شير عنو
و مشر لما لاند طول الحانه
90° صير



$$\begin{aligned} \sin \phi &= \frac{1}{2} \\ \phi &= 30^\circ \end{aligned}$$

46



$$\tan \theta = \frac{5}{10} = \frac{1}{2}$$

$$\theta = 30^\circ$$

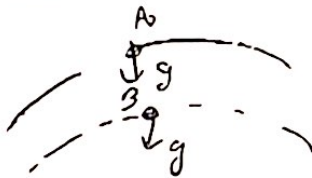
W of N

W of N



(B)

47



$$\theta_{AB} = \theta_{AO} - \theta_{BO}$$

$$= g - g = 0$$

تم بحال

وَأُضِرَّ كَمَا

إعداد: وائل عاوي



Chapter 5

[14] [B]

$$W = mg$$

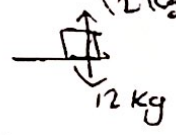
يعني

$$F = ma$$

[15] الكتلة تتحرك
وغير متساويةوهي ليست
free fall[16] 
 $W = 9.8 \text{ m}$

$$\frac{W}{m} = 9.8$$

وهي ليست

[E] الجسم
ليس في حالة سقوط
حرة فليس له تسارع[17] 
 $W = 120 \text{ kg}$
scale

$$m = \frac{W}{g} = \frac{120}{10} = 12$$

$$m = 12 \text{ kg}$$

$$W = mg$$

$$= 12 \times \frac{1}{6}$$

$$x = 2$$

[9] [D] net force

$$F_{\text{net}} = ma$$

تسارعت وقوة
F و a
same direction

[10] [B] الكتلة

التي تقيس مقاومة الجسم
Inertia القصور الذاتي لأنهاعند تسارع الجسم
تكون القوة

$$F = ma$$

تزداد مع m

لأن التسارع ثابت

عند تسارع الجسم

مساوي

[11] [C] التسارع

الذي يقيس

تغير السرعة مع الزمن

دلالة على

[12] [C] التسارع

مع التسارع

تسارع الجسم

بجهد أنه لو لم يكن

القوة رجبت التسارع

الخطي التسارع يكون

مساوي التسارع

$$1 \text{ kg} \rightarrow 5 \text{ m/s}^2$$

$$2 \text{ kg} \rightarrow 1 \text{ m/s}^2$$

[13]

$$F_1 = F_2$$

$$m_1 a_1 = m_2 a_2$$

[1] [B] التسارع

تسارعت الجسم

$$F = ma$$

اذن $a = 0$ وعليه لا يتحرك الجسم

ويفضل تسارع الجسم يتحرك

بسرعة ثابتة وفضل تسارع الجسم

وهو التسارع التسارعت القصور الذاتي

[2] التسارع

و a

D

$$F_{\text{net}} = 0$$

$$F = ma$$

so [D]

[4] [A] m/s

$$F = kg \frac{m}{s^2}$$

[6] و [7] تسارعت

~~[8]~~

$$F = ma$$

$$F = 5.6 \times 1$$

$$= 5.6 \text{ m/s}^2$$

(18) $m_1 < 3m_2$

$v = gt + u_0$
 الجواب: $v = gt$

(19) $a = \frac{F}{m} = \frac{10}{2} = 5$

$a = \frac{1}{2}g$

(B) the same

(20) $a = 0$
 $F \neq mg$

$F = 0$
 $5 - 3 - f = 0$

$f = 5 - 3$
 $f = 2N$
 left word

(B)

(21) (A)

$5 - 3 = 2$
 $f = 2N$

22: 1- $N = mg$
 2- $N \sin \theta + 10 \sin \theta = mg$
 3- $N + 10 = mg$

$3 < 2 < 1$

(23) $N_i = mg$

$N_{ii} = mg \cos \theta$

(C) (less)

(24) $m_B = 3m_A$

$F_B = F_A$

$m_B a_B = m_A a_A$

$3m a_B = m a_A$

$3a_B = a_A$

(A)

(25) zero
 $a = 0$

Friction $\rightarrow a$
 $F = 8N$

(26) u_s
 $16kg$

$\left(\frac{F}{m}\right)a = \frac{\Delta v}{\Delta t}$
 $(45) \frac{8}{16} = \Delta v$
 $\Delta v = 2 m/s$

$\Delta v = 0.5$

in this case

(27) $12N$

(A) $a = \frac{F}{m}$
 $= \frac{2}{1} m/s^2$
 North

(28) $W = 9000N$
 $F = 500N$

$F = ma$

$a = \frac{F}{m}$

$= \frac{500}{9000}$
 $= 0.055$ (B)

(29) $21W + 4S$

$F = ma$

$F_{app} - 0 = ma$

(30) $A = 25 + g$
 $f = 20N$ 20°

$a = \frac{F \cos 20^\circ}{m} = \frac{20 \cos 20^\circ}{25} = \frac{4}{5}$
 $= 0.8 m/s^2$

(31) $W = 1.5N$
 30°

$v_0 = 12 m/s$

$F = mg = 1.5N$
 down

(32) $5kg$

$8N$

$F_{net} = \sqrt{8^2 + 6^2}$

$= 10N$

على ان من سرعة الاجسام
 زادت ما مضى الزمان
 بسبب هي

(33)



$$T = 400 \text{ N}$$

$$T = mg = W = 400$$

(34)

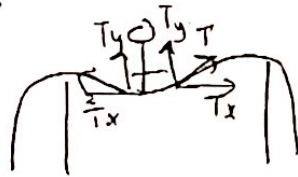
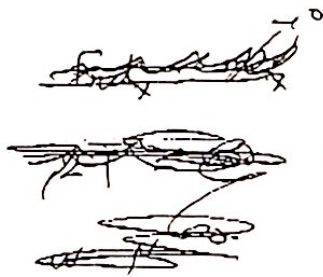
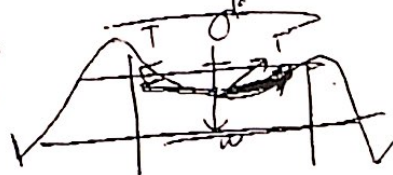
A = zero



لا شيء
التي لا عم ينزل

بمنزلة

(35)



ممكن لا تاتي

Component X

كيفية الف

$$T_y = mg$$

و ما لا كان X

Component فنان

بكون المبرند

(36)

$$1000 \text{ kg}$$

s ↑

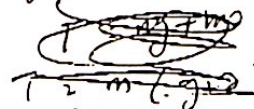
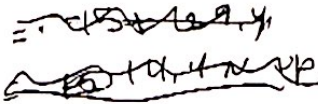
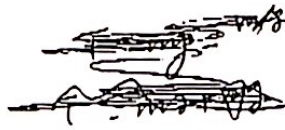
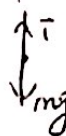
$$a = 3 \text{ m/s}^2$$

$$F_{\text{net}} = ma$$

$$- = ma$$



37



$$25(9.8 + 3)$$

$$= 64 \text{ N up}$$

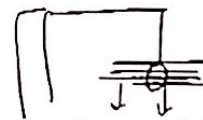
$$T = m_2 + m_1$$

$$T = m(2 + 9)$$

$$= m(2 + 9.8)$$

$$= 34 \text{ N}$$

(38)



$$3 \text{ m/s}^2 \quad 16000 \text{ N}$$

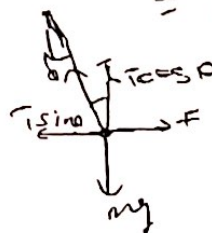
$$T - mg = -ma$$

$$T = mg - ma$$

$$T = 16000(9.8 - 3)$$

$$= 11000 \text{ N}$$

(39)



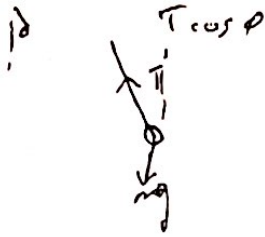
$$T^2 \cos^2 \theta = mg^2$$

$$T^2 \cos^2 \theta = 1$$

$$T \sin \theta = 4$$

$$T \sin \theta = 4$$

$$T \sin \theta = 4$$



$$F_{net} = ma$$

$$T \sin \phi = ma$$

$$T \cos \phi = mg$$

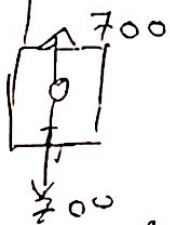
$$\frac{T \sin \phi}{T \cos \phi} = \frac{ma}{mg}$$

$$\tan \phi = 0.306$$

$$\phi = 17^\circ$$

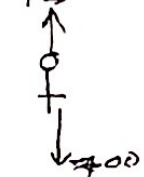
41

$$a = 4 \text{ m/s}^2$$



on a horizontal surface

is 700



$$N - 700 = ma$$

$$N = ma + 700$$

$$= 285.7 + 700$$

$$= 985.7$$

$$\approx 990 \text{ N}$$

42



(A) $T = m(g+a)$

(B) $T = m(g-a)$

(C) $T = mg$

(D) $T = m(g-a)$

(E) $T = mg$



(A) $N = m(g-a)$

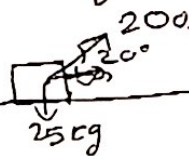
(B) $N = m(g+a)$

(C) $N = mg$

(D) $N = m(g-a)$

(E) $N = mg$

44



$$N = mg + 200 \sin 20^\circ$$

$$= 245 + 68.4$$

$$= 313$$

$$\approx 310 \text{ N}$$

45

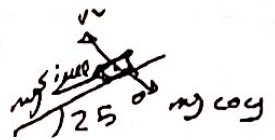


$$mg \sin \phi = ma$$

$$a = 4.9 \text{ m/s}^2$$

$$440 \text{ cm/s}^2$$

46



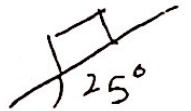
$$N = mg \cos \phi$$

$$= 25 \cos 25$$

$$= 22.6$$

$$= 23 \text{ N}$$

47



$$F - mg \sin \phi = 0$$

$$F = mg \sin \phi$$

$$= 25 \sin 25$$

$$= 10.5 \text{ N}$$

$$\approx 11 \text{ N}$$

48



$$N = mg \cos \phi$$

$$= 23 \text{ N}$$

49



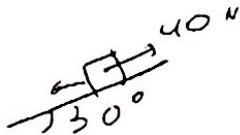
$$F - mg \sin \theta = ma$$

$$32 - 4.9m = 0$$

$$4.9m = 32$$

$$= 6.5 \text{ kg}$$

50



$$mg \sin \theta = F$$

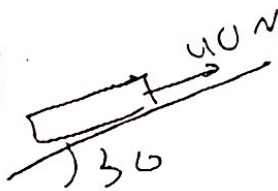
$$4.9m - 40 = 2m$$

$$2.9m = 40$$

$$m = 13.79$$

(E)

51



$$F - mg \sin \theta = ma$$

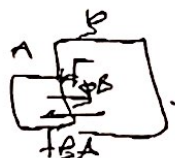
$$40 - 4.9m = 2m$$

$$40 = 6.9m$$

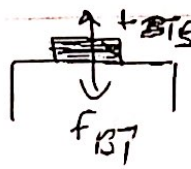
$$m = \frac{40}{6.9} = 5.8 \text{ kg}$$

52

B



53

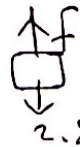


54



The block
on Earth

55



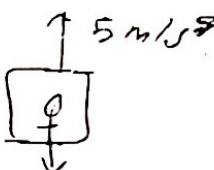
$$F - mg = ma$$

$$F = mg + ma$$

$$F = 35 \text{ N up}$$

$$F_B = 35 \text{ N down}$$

56



$$F = mg$$

$$= 90 \times 9.8$$

$$= 882 \text{ N}$$

57



$$F - mg = ma$$

$$F = m(g + a)$$

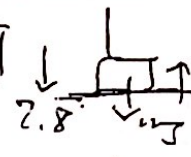
$$F = 90(10 + 1.1)$$

$$= 999$$

$$= 774$$

$$= 60 \text{ N}$$

58



$$F_B = mg$$

$$= 49 \text{ N}$$

$$F_C - F_B = 49 \text{ N}$$

59



$$W = 882$$

$$W = 107$$

$$107 - T = 110$$

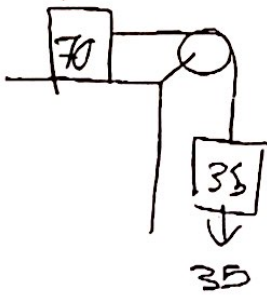
$$T - 882 = 9$$

$$107 - 882 = 9$$

$$a = 1.03$$

$$= 0.98 \text{ m/s}^2$$

(60)



$$35 - T = 3.82$$

$$T = 7.142$$

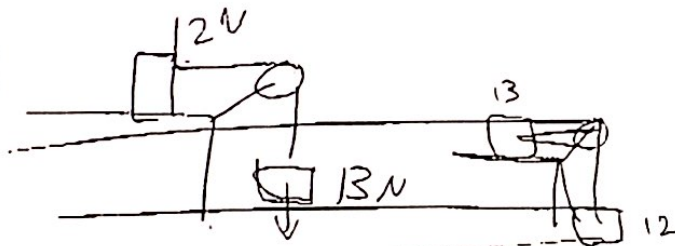
$$35 - 7.142 = 3.62$$

$$35 = 10.72$$

$$a = 3.25 \text{ m/s}^2$$

$$= 3.3$$

(61)



$$13 - T = 1.3$$

$$T = 1.22$$

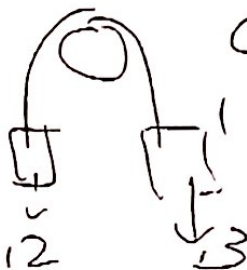
$$12 - 1.32 = 1.22$$

$$13 - 1.22 = 1.32$$

$$a = 2.52$$

$$a = 4.8$$

$$a = 2.52$$



$$13 - T = 1.32$$

$$T = 1.22$$

$$a = \frac{1}{2.5} = 0.4$$

(62)



$$5\text{kg} \quad 4\text{kg}$$

$$5g - T = 5a$$

$$T - 4g = 4a$$

$$1g = 9a$$

$$a = \frac{9}{9}$$

(63)

$$350 - T = 35a$$

$$T - 250 = 25a$$

$$100 = 60a$$

$$a = 1.66 \text{ m/s}^2$$

$$T = 41.7 + 250$$

$$= 291.7 \text{ N}$$

(64)



(65)

لا نولوكان

الذ فاع

يكون الوتار

تساوي مع توتر

لبس هو ثابت

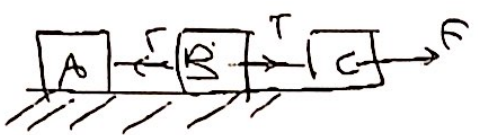


9

9 = 4 * 4

Uploaded By: anonymous

(66)



$$F - T_1 = Ma$$

$$T_1 - T_2 = Ma$$

$$T_2 = Ma$$

~~$a = \frac{F}{3M}$~~

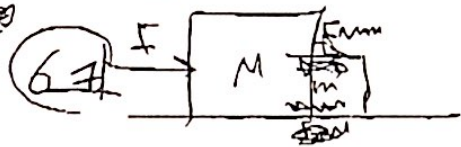
~~T_2~~

$$F = 3Ma$$

$a = 1.5$

$$F_{netB} = Ma$$

ii) $\left(\frac{F}{3}\right)$
(B)



~~$F - F_{fm} = Ma$~~

~~$F - F_{fm} = Ma$~~

~~$2F - 2F_{fm} = (m+M)a$~~

~~$F_{fm} = \frac{m}{m+M} F$~~

$$F - F_{fm} = Ma$$

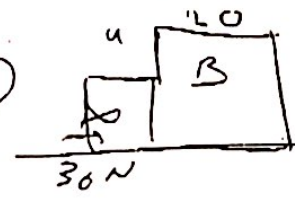
$$F_{fm} = ma$$

$$a = \frac{m}{m+M} F$$

$$F_{fm} = ma$$

$$F_{fm} = m \left(\frac{m}{m+M} F \right)$$

(68)



$$F - F_{AB} = ma$$

$$F_{AB} = Ma$$

~~a~~

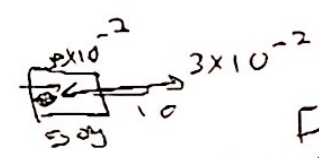
$$F = (m+M)a$$

$$36 = 24a$$

$$a = 1.5 \text{ m/s}^2$$

$$F_{AB} = 1.5 \times 20 = 30 \text{ N}$$

(69)



$$F = Ma$$

$$F - F_{ST} = ma$$

$$F_{ST} = F - ma$$

$$= 3 \times 10^{-2} - m \cdot a$$

$$= M \cdot a - m \cdot a$$

$$= (500 - 10) \cdot a$$

$$= 490 \cdot a$$

$$= 2.4 \times 10^{-2}$$

$$= 2.5 \times 10^{-2}$$

Ans

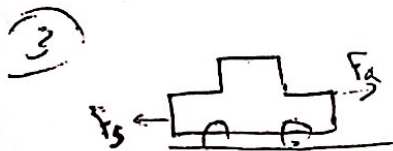
Chapter 6

① $F_s = \mu_s N = \mu_s mg$

نتائج زيادة الكتلة يؤدي إلى زيادة F_s

الاعداد: محمد
الهدل

② μ_k : ليس له وحدة
(2) ليس له اتجاه



The greatest retarding force $F_s = F_{s \max}$
وذلك قبل بدء الانزلاق



$F = \mu_k N$

$\mu_k = \frac{f}{N} = \frac{12}{240} = 0.05$



$F_s = ma$

$\mu_k N = ma$

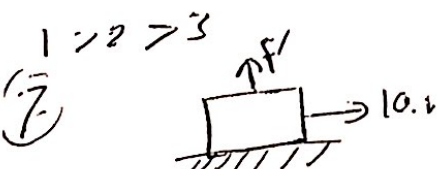
$\mu_k mg = ma$

$\mu_k = \frac{a}{g} = \frac{0.16}{9.8} = 0.01622$

⑥ $F_s = 10N$ في الحالة الأولى

$F_s = (10N) \cos 0$ في الحالة الثانية

$F_s = 20N$ في الحالة الثالثة



$F = \mu_s N = \mu_s (mg - F')$

$0 = (0.4)(50 - F')$

$F' = 50 - 25 = 25N$

⑧

إذا كانت $F > F_{s \max}$ تكون

$F_s = \mu_k N$

إذا كانت $F < F_{s \max}$ تكون

$F_s = F$

$F_{s \max} = \mu_s N = (0.5)(40) = 20N$
 $F_{s \max} > F$

$F_s = F = 12N$ يتالي

⑨

(نفس فكرة السؤال 8)

$F_{s \max} = \mu_s N = (0.5)(40) = 20N$

$F > F_{s \max}$

$F_s = \mu_k N = (0.4)(40) = 16N$

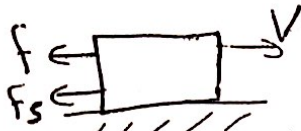
⑩

$F_{s \max} = 200N$

$\mu_s N = 200$

$\mu_s = \frac{200}{800} = 0.25$

(11) f f_{smax} (مطلوبات)



بما ان القوة اثرت باتجاه يمينها
الحركة يتألي سرعة الجسم سوف
تقل حتى تصبح صفر ثم تزداد بعد
ذلك

(12) $F = f_{smax} = \mu_s N = 0.5mg$

$F - f_k = ma$

$0.5mg - 0.4mg = ma$

$a = 0.1g = (0.1)(9.8)$

$a = 0.98$

(13) $v_f = v_i + at$

$0 = 15 + a(4)$

$a = \frac{-15}{4} = -3.75 \text{ m/s}^2$

$f_k = \mu_k N = \mu_k mg$

لحظة توقف الجولان عند الدوران

$f_k = ma$

$\mu_k mg = ma$

$\mu_k = \frac{a}{g} = \frac{3.75}{9.8} = 0.382$

(14) فيما ان السرعة ثابتة يتألي التسارع
ليسا صفر

$P - F = ma = 0$

$P = F$

$N - fg = 0$

$N = F_g$

(15) $P \cos \theta - f = ma = 0$

$P \cos \theta = f$

$-1 < \cos \theta < 1$

$P > F$

$P \sin \theta + N - fg = 0$

$N = fg - P \sin \theta$

بما ان الجسم يتحرك بسرعة ثابتة

(16)

$F \cos \theta - f_k = ma = 0$

$F \cos \theta = f_k$

$F \cos \theta = \mu_k N = \mu_k (mg - F \sin \theta)$

$(0.8)F = (0.4)(400 - (0.6)F)$

$(0.8)F = 160 - (0.6)(F)(0.4)$

$(0.8)F + (0.24)F = 160$

$(1.04)F = 160$

$F = \frac{160}{1.04} = 153.8 \approx 150 \text{ N}$

(17)

بما ان الجسم يتحرك بسرعة ثابتة

$T \cos \theta - f_k = ma = 0$

$f_k = T \cos \theta$

(18)

$T \sin \theta + N - mg = 0$

~~$T \sin \theta = mg$~~

~~$N = mg - T \sin \theta$~~

المطلوب (N) المركبة العمودية للقوة التي تؤثر

$N = mg - T \sin \theta$

(19)

اقل قوة تترك لتتألي الجسم

$F \cos \theta = f_{smax}$

$F \cos \theta = \mu_s N = \mu_s (mg + F \sin \theta)$

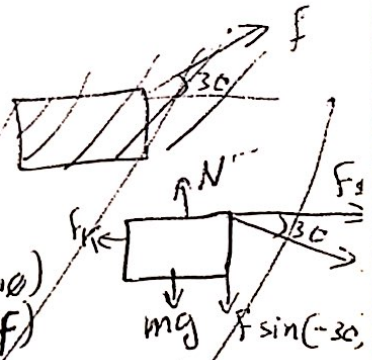
$F \cos(30) = (0.4)((12)(9.8) + (0.5)F)$

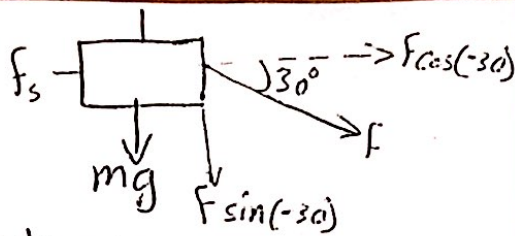
$F = \frac{47.04}{\cos 30 - 0.5 \sin 30} = 54.317 \text{ N} \approx 54$

$F \cos 30 = 47.04 + (0.5)F$

$F \cos 30 - (0.5)F = 47.04$

$F = \frac{47.04}{\cos 30 - \sin 30} =$





أقل قوة تلزم لتريك الجسم عن موضعه

تكون

$$F \cos(-30) = f_{s \max} = \mu_s N = \mu_s (mg + f \sin(-30))$$

$$F \cos 30 = (0.4)(12)(9.8) + (0.5)F$$

$$F \cos 30 = 47.04 + (0.5F)(0.4)$$

$$F' = \frac{47.04}{\cos 30 - 0.2} = \frac{47.04}{0.366}$$

$$F \cos 30 = 0.2F = 47.04$$

$$F = \frac{47.04}{\cos 30 - 0.2} = 70.627 \text{ N}$$

20) $\tan \theta = \mu_s$

$$\theta = \tan^{-1}(0.4) = 22^\circ$$

21) $\tan \theta = \mu_s$

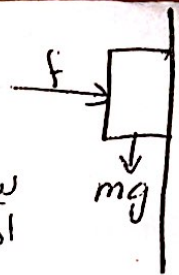
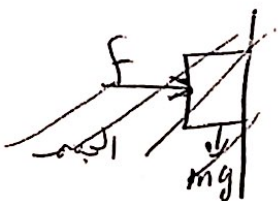
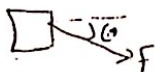
$$\theta = \tan^{-1}(0.5)$$

$$\theta = 26.6 \approx 27^\circ$$

عند هذه الزاوية تكون الكبرقوة و بتالي اقل يتسارع

22) نزال قوة الاحتكاك عند سحب الجسم بقوة تصلح زاوية تحت الاتجاه الافقي نتيجة زيادة N

$$f_s = \mu_s N$$



ليتحرك الجسم للأسفل
 اذا كانت
 $mg > f_{s \max}$

$$f_{s \max} = \mu_s N = \mu_s f = (0.6)(12) = 7.2$$

$$f_{s \max} > mg$$

بتالي:

$$f_s = mg = (0.5)(9.8) = 4.9$$

(24)

نبحث اذا كان الجسم قد تحرك
 للأسفل ام لا

$$mg = (0.5)(9.8) = 4.9 \text{ N}$$

$$f_{s \max} = \mu_s f = (0.6)(5) = 3 \text{ N}$$

$$mg > f_{s \max}$$

بتالي تحرك الجسم للأسفل

$$f_s = \mu_k N = \mu_k f = (0.8)(5) = 4 \text{ N}$$

(25)

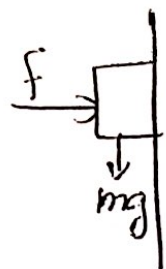
نبحث اذا كان الجسم قد تحرك
 ام لا

$$mg = (0.5)(9.8) = 4.9$$

$$f_{s \max} = \mu_s f = (0.6)(12) = 7.2$$

$$f_{s \max} > mg$$

و بتالي الجسم لم يتحرك
 التسارع يساوي صفر



(26)

$$mg = 4.9$$

$$f_{s\max} = (0.6)(5) = 3$$

$$mg > f_{s\max}$$

يتالي الجسم ترك لا سف

$$mg - f_k = ma$$

$$mg - \mu_k f = ma$$

$$4.9 - (0.8)(5) = (0.5)a$$

$$a = \frac{0.9}{0.5} = 1.8$$

(27)

$$F_1 = f_s + ma$$

من الحالة الأولى

من الحالة الثانية

$$F_2 = f_s + mg \sin \theta + ma$$

بما ان

$$f_1 = f_2$$

$$f_{s1} + ma = f_{s2} + mg \sin \theta + ma$$

$$f_{s1} = f_{s2} + mg \sin \theta$$

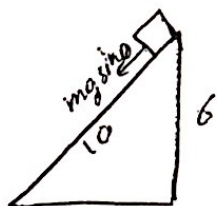
بما ان

$$mg \sin \theta > 0$$

يتالي

$$f_{s1} > f_{s2}$$

(28)

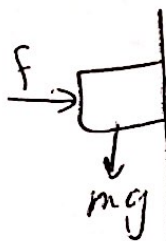


$$mg \sin \theta = f_s = \mu_s N$$

$$mg \sin \theta = \mu_s (mg \cos \theta)$$

$$\mu_s = \tan \theta$$

$$\mu_s = \tan(37^\circ) = 0.75$$



(30)

$$mg \sin \theta - f_k = 0$$

$$mg \sin \theta = (\mu_k)(mg \cos \theta)$$

$$\mu_k = \tan \theta = 0.577$$

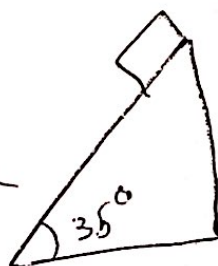


(31)

$$mg \sin \theta - f_k = ma$$

$$mg \sin \theta - \mu_k (mg \cos \theta) = ma$$

$$g \sin 35 - (0.4)(g)(\cos 35) = a$$



$$a = 2.409$$

(32)

نبحث اذا ترك الجسم للسف
ام لا

$$mg \sin \theta = (49)(\sin 25) = 20.7 \text{ N}$$

$$f_{s\max} = \mu_s N = \mu_s mg \cos \theta = (0.5)(44.4)$$

$$f_{s\max} = 22.2$$

$$f_{s\max} > mg \sin \theta$$

يتالي الجسم لا يتحرك

~~الاستاتيكي~~

$$f_s = mg \sin \theta = 20.7 \approx 21$$



(33)

نبحث اذا ترك الجسم
للا سف ام لا

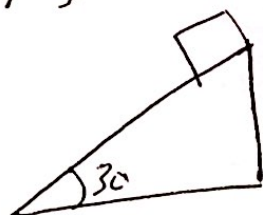
$$mg \sin \theta = 24.5 \text{ N}$$

$$f_{s\max} = (0.5)(49)(\cos 30) = 21.2$$

$$mg \sin \theta > f_{s\max}$$

يتالي الجسم ترك لا سف

$$f_k = \mu_k N = (0.4)(49)(\cos 30) = 17 \text{ N}$$



$$mg \sin \theta = 24.5 \text{ N}$$

$$f_{s \max} = 21.2 \text{ N}$$

$mg \sin \theta > f_{s \max}$
بالي الجسم يتحرك للأسفل
ولكني يشبه الجسم يجب ان
تؤثر القوة باتجاه يعاكس لاي
 $mg \sin \theta$

$$mg \sin \theta - f - f_s = ma = 0$$

$$= mg \sin \theta - \mu_s (mg \cos \theta)$$

$$= 24.5 - 21.2$$

$$f = 3.3 \text{ N}$$

$$(35) mg \sin \theta = 24.5 \text{ N}$$

$$f_{s \max} = 21.2$$

$$mg \sin \theta + f_s - F = ma = 0$$

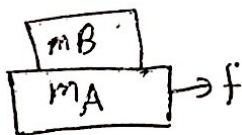
$$F = mg \sin \theta + f_{s \max}$$

$$= 24.5 + 21.2$$

$$= 45.7 \text{ N}$$

وصفتنا f باتجاه $mg \sin \theta$ لان ايس زياد
في قليلة في f سوف تؤدي الى حركة
الجسم للأعلى وبالتالي يكون الاحتكاك
باتجاه يعاكس لـ f

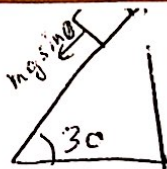
(36)



ملاحظة: اذا كانت
 $F \leq f_{s \max} \rightarrow$ يتحرك A و B
لا ينفصل الجسمان

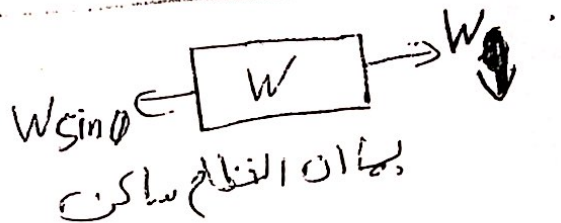
لذا ان كانت
 $F > f_{s \max}$
ينفصل الجسمان

$$f_{s \max} = \mu_s N = \mu_s (m_A + m_B)g$$



(37)

$$f_s = W \sin \theta$$



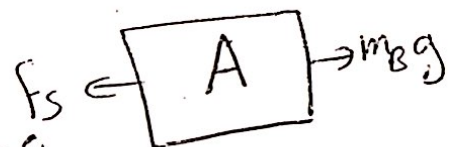
$$W \sin \theta + f_s = W = 0$$

$$f_s = W - W \sin 37$$

$$= 20 - 20 \left(\frac{3}{5} \right)$$

$$f_s = 8 \text{ N}$$

(38)



ليكون الجسم على وشك ان
يتحرك نحو اليمين

$$m_B g = f_{s \max}$$

$$f_{s \max} = \mu_s N = (0.4)(490) = 196$$

$$m_B g = f_{s \max} = 196$$

$$m_B = \frac{196}{9.8} = 20 \text{ kg}$$

(39)



$$m_A g \sin \theta - f_s - m_B g = 0$$

$$m_B = \frac{m_A g \sin \theta - f_s}{g} = \frac{m_A g \sin \theta - \mu_s m_A g \cos \theta}{g}$$

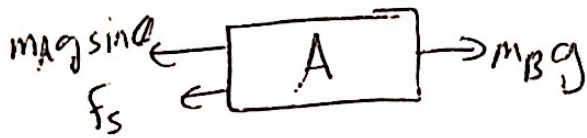
$$m_B = (10)(9.8)(\sin 35) - (0.4)(10)(9.8)(\cos 35)$$

$$= 20.75$$

$$m_B = 5.735 - 3.276$$

$$m_B = 2.458 \approx 2.5$$

(40)

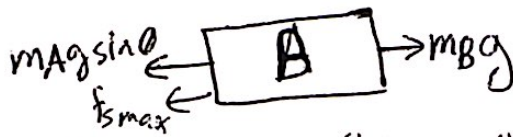


$$m_B g = m_A g \sin \theta + f_s = m_A g \sin \theta + \mu_k (m_A g \cos \theta)$$

$$m_B g = (10)(9.8)(\sin 35) + (0.4)(10)(9.8)(\cos 35) = 88.32$$

$$m_B = \frac{88.32}{9.8} = 9.01 \text{ Kg}$$

(41)



$$m_A g \sin \theta = 49 \text{ N}$$

$$m_B g = 78.4$$

$$f_{s \max} = f_k = \mu_k N = (0.2)(m g \cos 30)$$

$$f_k = (0.2)(98)(\cos 30) = 16.7 \text{ N}$$

$$m_B g - m_A g \sin \theta - f_k = m_{(A+B)} a$$

$$12.7 = (18) a$$

$$a = 0.69$$

$m_B g = 0$ بالجاه

(42) $m_A g \sin \theta = 49$ $m_B g = 29.4$

بما ان $m_A g \sin \theta$ اكبر من $m_B g$ بالجاه
بما ان تكون الحركة بالجاه $m_A g \sin \theta$ بالجاه
وتكون f_s بالجاه $m_B g$



$$m_A g \sin \theta - m_B g - f_k = m_{(A+B)} a$$

$$49 - 29.4 - 16.7 = (13) a$$

$$a = 20$$

$m_A g \sin \theta$ بالجاه

up

(43)

$f = ma$
بما ان السرعة ثابتة بتالي التسارع يساوي صفرا $f = 0$ بتالي

(44)



لان مقاومة الهواء لسقوط المطر تقل
الى قيمتها العظمى عند تسارع يساوي (mg)
ولا يمكن ان تزيد عن هذا المقدار.

(45)

بما ان سرعته البدائية تساوي ثلاث اضعاف
 V_T بتالي فان لسرعته سوف تقل حتى تصبح
تساوي V_T ومن ثم تثبت وبما ان السرعة
تقل بتالي التسارع سالب حيث يكون اتجاهه
للأعلى وبما ان اتجاه التسارع للأعلى
 $a > g$

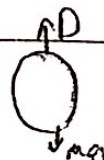
(46)

$V < V_T$ (قبل ان يحد
الارتفاع)


$$mg = D \quad V = V_T$$

$$mg > D$$

$$V > V_T$$



(1) $D=0$



$mg = D$
 $l = v_T$



$v < v_T$
 $mg > D$

$v > v_T$
 $mg > D$



$v = v_T$
 $mg = D$

(44) $a = \frac{v^2}{R}$

بما ان السرعة ثابتة وكذا ذلك
النصف قطر الدائرة ثابت
فان التسارع يتحرك بتسارع ثابت

(50) $a = \frac{v^2}{R}$

لا توجد عاكس كتلة الجسم

(51) $F = \frac{mv^2}{R}$

$F = \frac{(0.04)(0.0)^2}{1}$

$F = 0.0144 \text{ N}$

(52) $T = \frac{mv^2}{R}$

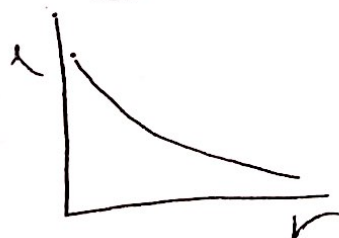
$V = 150 \text{ rev/min} = \frac{150(2\pi r)}{60} \text{ m/s}$

$V = 9.42$

$T = \frac{(0.2)(9.42)^2}{0.6} = 30 \text{ N}$

(53) $a = \frac{v^2}{R}$

بما ان السرعة ثابتة يتالي فان زيادة
تؤدي الى نقصان قيمة التسارع



(54) $T_1 = \frac{mv^2}{R}$

$T_2 = \frac{mv^2}{2R} = \frac{1}{2} \frac{mv^2}{R} = \frac{1}{2} T_1$

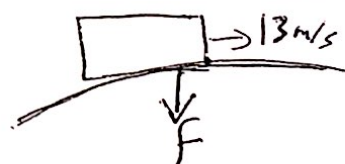
$T_2 = \frac{1}{2} T_1$

(55) $T_1 = \frac{mv^2}{R}$

$T_2 = \frac{(3m)(\frac{1}{2}v)^2}{R} = (3)(\frac{1}{4}) \frac{mv^2}{R} = \frac{3}{4} T_1$

(56) التسارع من الكسار الدائري يكون
دائماً باتجاه المركز

(57)



لكي يفتح الباب يجب ان تكون
السيارة تسير بسرعة 13 m/s

$F = \frac{mv^2}{R}$

$200 = \frac{(800)(13)^2}{R} \Rightarrow R = 67.6$

لكي يفتح الباب يجب ان تكون
800 N تساوي

$800 = \frac{(80)(v^2)}{67.6} \Rightarrow v = \sqrt{676} = 26$

$$(58) F = \frac{mv^2}{r}$$

$$r_1 = \frac{mv^2}{F}$$

$$r_2 = m \frac{(2v)^2}{F} = 4 \frac{mv^2}{F}$$

$$r_2 = 4r_1$$

$$(59) F_s = MBN = \frac{mv^2}{r}$$

$$(0.5) mg = \frac{mv^2}{30}$$

$$v^2 = 147$$

$$v = 12 \text{ m/s}$$

$$(60) F_s = \frac{m v_{\max}^2}{R}$$

$$v_{\max}^2 = \frac{(F_s)(R)}{m} = \frac{(400)(1000)}{1000} = 400$$

$$v_{\max} = \sqrt{400} = 20 \text{ m/s}$$

تبقى السيارة تتحرك على المنحنى بحداد
سرعتها أقل أو تساوي v_{\max} وبما أن
السيارة دخلت المنحنى بسرعة أكبر
من 20 m/s وهي 10 m/s يتأخر خروج
السيارة من المنحنى

$$(61) a = \frac{v^2}{R}$$

$$a = \frac{(18)^2}{75} = 4.32 \text{ m/s}^2$$

$$\tan \theta = \frac{a}{g} = \frac{4.32}{9.8} \frac{\Delta g}{a}$$

$$\theta = \tan^{-1} \left(\frac{4.32}{9.8} \right)$$

$$\theta = 23.788 \approx 24^\circ$$

(62)



$$\Sigma F = mg + N$$

$$N = mg$$

$$\Sigma F = 2mg$$

(63) من السؤال السابق

$$\Sigma F_{\text{net}} = 2mg = ma$$

$$a = (2)(9.8) = 19.6 \text{ m/s}^2$$

$$a = \frac{v^2}{R}$$

$$v^2 = (a)(R) = (19.6)(20) = 392$$

$$v = 19.8 \approx 20$$

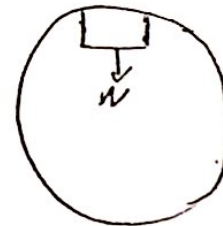
(64)

$$F_g = N = mg$$

$$F_b = 0 \rightarrow$$

تبقى منحنى بحداد
يدور

$$F_s = 0$$



دورات

(65)

$$T - mg = ma$$

$$T = mg + ma$$

$$= (2)(9.8) + (2) \left(\frac{v^2}{R} \right)$$

$$= 19.6 + 2 \left(\frac{16}{1} \right)$$

$$= 19.6 + 32$$

$$= 51.6 \approx 52$$



(33)

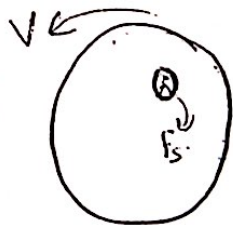
$$T - mg = ma$$

$$T = m\left(\frac{v^2}{R}\right) - mg$$

$$= 32 - 19.6$$

$$= 12.4 = 12 N$$

(7)



$$N = mg = \text{constant}$$

$$s_{\max} = \mu_s N$$

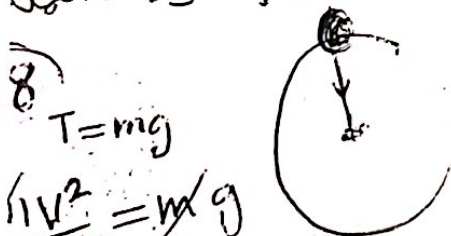
بجانب N ثابت بتاي

$$s_{\max} = \text{ثابت}$$

$$s = ma = m \frac{v^2}{R}$$

بتاي f تزيد حتى تصبح صفر

ف s_{\max} و a زياد بعد
تكون في اثنائها العمل



$$T = mg$$

$$\frac{mv^2}{R} = mg$$

$$v^2 = (0.7)(9.8)$$

$$v^2 = 6.86$$

$$v = 2.61 \text{ m/s}$$

(64)

$$a = \frac{v}{R} = \frac{(22)^2}{45} = 10.755$$

$$\tan \theta = \frac{a}{g}$$

$$= \frac{10.755}{9.8}$$

$$\theta = 47.66$$



(70)

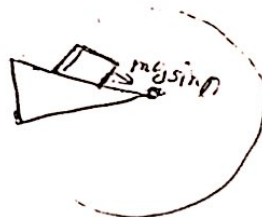
$$a = \frac{v^2}{R}$$

$$R = \frac{v^2}{a}$$

بما ان السرعة ~~تزداد~~ زادت الى

$$(2v)^2 = 4v^2$$

بتاي R تزداد اربع اضعاف



(71)

$$mg \sin \theta = ma$$

$$mg \sin \theta = \frac{mv^2}{R}$$

$$\theta = \sin^{-1} \frac{v^2}{(g)(R)}$$

$$\theta = 17^\circ$$

erg \checkmark الألف في الفيزياء
 $W = \Delta K.E$ \checkmark Δ \checkmark

ft lb \checkmark قدم رطل

Natt \times وحدة قياس القوة

$1, m \Rightarrow W = F \cdot d = N \cdot m$

Joule $\Rightarrow W = \Delta K.E = J$

(Scalar quantity)
 Power / speed

energy / distance
 time

scalar quantity

velocity force displacement

acceleration / force / sp

~~work~~ weight

3) $W = \vec{F} \cdot \vec{d}$
 هما ان الزاوية متساوية
 بيني الشكل يساوي

1) $W = F \cdot d = (10)(10) = 100$
 في الحالة الاولى
 في الحالة الثانية

$W = (F \cos 46)(10) < 100$
 في الحالة الثالثة

$W = (F)(d)(\cos 46) = 0$

$\theta > 90^\circ$

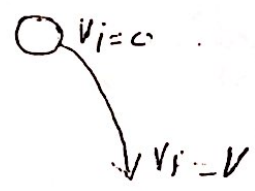


رسم القوة المركزية يساوي صفر
 لان الزاوية بين (r) و (v)
 دائما يساوي 90 و
 $\cos 90 = 0$
 $W = 0$

(6) $W = 0$ (نفس فكرة سوال 5)

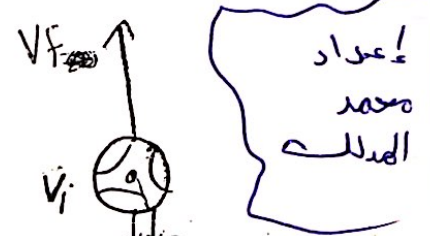
(7) $W_{mg} = \Delta K$

V_f دالة موجية كان
 V_i اكبر من

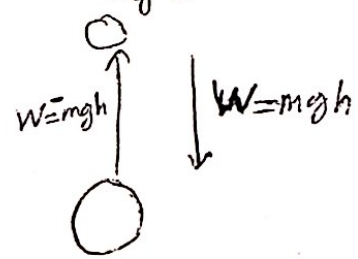


(8) ~~$W_{mg} = \Delta K$~~ $W = mgh$

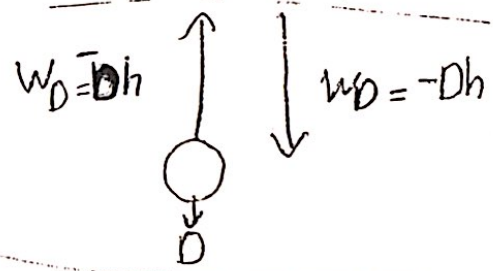
V_f اكبر من V_i
 تكون ΔK سالبة



(9) $W_{mg} = mgh - mgh = 0$

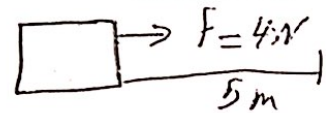


$W_D = -Dh - Dh = -2Dh$



(10)

$W_f = F \cdot d = (4)(5) = 20 J$

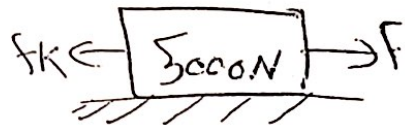


(11)

بما ان السرعة ثابتة بيني
 التسارع يساوي صفر

$F - f_k = ma = 0$

$F = f_k = \mu_k N = (0.05)(5000) = 250 N$



$W_f = F \cdot d = (250)(1000) = 2.5 \times 10^5 J$

(12) $f_k \leftarrow 6000 \rightarrow f$
 $F = f_k = \mu_k N = (0.05)(6000) = 300$
 $W_f = f \cdot d = (300)(1000) = 3 \times 10^5$

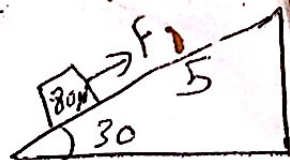
(13) $f_k \leftarrow 6000 \rightarrow f$
 $a = 0.2 \text{ m/s}^2$
 $F - f_k = ma$
 $F = f_k + ma = 300 + \left(\frac{6000}{10}\right)(0.2)$
 $F = 420 \text{ N}$
 $W_f = f \cdot d = (420)(1000) = 4.2 \times 10^5$

(14) $F_b = mg = (1)(10) = 10 \text{ N}$
 $W_b = f \cdot d = (10)(1) = 10 \text{ J}$

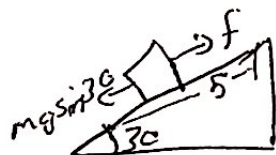
(15) $d = \text{one revolution}$
 $= 2\pi r = 15.7 \text{ m}$
 $W_f = f \cdot d = f d \cos 0$
 $= (3)(15.7) = 47.1$

(16) $mg \sin 30$
 $F_m - mg \sin 30 = 0$
 $F_m = mg \sin 30 = (100)(0.5) = 50 \text{ N}$
 $W_m = F_m \cdot d = (50)(10) = 500 \text{ J}$

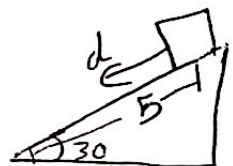
(17) $a = 1.5 \text{ m/s}^2$
 $F - mg \sin 30 = ma$
 $F = mg \sin 30 + ma = (80)(0.5) + \left(\frac{80}{10}\right)(1.5)$
 $F = 28 \text{ N}$
 $W_f = f \cdot d = (28)(5) = 140 \text{ J}$



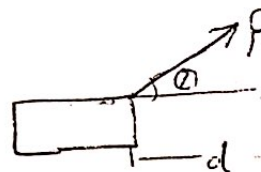
(18) $F - mg \sin 30 = 0$
 $F = (80)(0.5) = 40 \text{ N}$
 $W_f = (40)(5) = 200 \text{ J}$



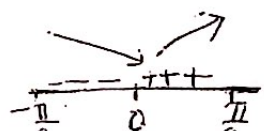
(19) $W_{mg} = mg \cdot d$
 $= (mg)(d)(\cos 90)$
 $= (mg)(d)(\sin 30)$
 $= (80)(5)(0.5)$
 $= 200 \text{ J}$



(20) $W = f d \cos \theta$



(21) $f_k = \mu_k N = \mu_k (mg + F \sin \theta)$
 $F \sin \theta = 0$
 $\sin \theta = 0$
 $\theta = 0$
 $W_f = F d \cos \theta$
 $dW = F d \sin \theta = 0$



نشفل مركبة القوة على زواياها وعلى
2-axis
الحالة تكون 90 بين F و d
وننتيجة لذلك يكون شغل F

$$W_f = F_x \cdot d = (4)(5)(1) = 20 \text{ J}$$

23) $W_s = \frac{1}{2} K (x_i^2 - x_f^2)$
يكون W_s موجب اذا كان
 $x_i^2 > x_f^2$

4) $F = -K \Delta x$
من الحالة الاولى

$$00 = -K(40 - x_0) \quad (1)$$

$$200 = -K(60 - x_0) \quad (2)$$

يحل (1) و (2) من خلال طرح (1) من (2)

$$100 = 4K$$

$$100 = 40K - Kx_0 + 6K - Kx_0$$

$$20 - 100 = K(60 - x_0) - K(40 - x_0)$$

$$100 = 60K - Kx_0 - 40K + Kx_0$$

$$100 = 20K$$

$$K = 5$$

بتعويض (1)

$$100 = 5(40 - x_0)$$

$$x_0 = 20$$

من الحالة الثانية

$$100 = K(30 - x_0)$$

$$= 5(30 - 20)$$

$$= 50$$

$$F = K \Delta x$$

$$-mg = -KX$$

من الحالة الاولى

$$(4)(10) = K(3 \text{ cm})$$

$$K = \frac{40}{3} \text{ N/cm}$$

من الحالة الثانية

$$60 = \left(\frac{40}{3}\right)(\Delta x)$$

$$\Delta x = 4.5 \text{ cm}$$

وبما انه يوجد زبرك Z وزبرك Y
فان كل منهما يتحرك بمقدار 4.5 cm

$$\Delta x = 4.5 + 4.5 = 9 \text{ cm}$$

26) $W = \int f dx = \int_0^L Kx dx$

$$W = \frac{Kx^2}{2} \Big|_0^L = \frac{KL^2}{2} - 0 = \frac{KL^2}{2}$$

27) $W = \int f dx = \int_0^L ax + bx^2$

$$= \frac{ax^2}{2} + \frac{bx^3}{3} \Big|_0^L = \frac{aL^2}{2} + \frac{bL^3}{3}$$

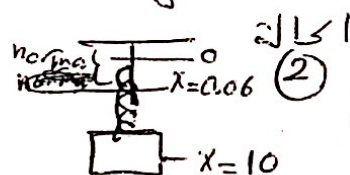
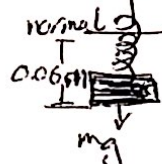
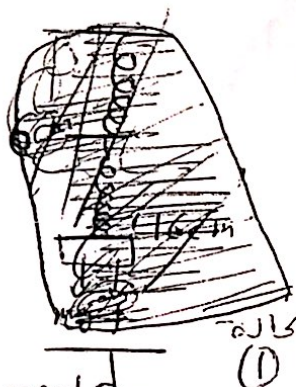
28) $mg = K \Delta x$

$$20 = K(0.06) \Rightarrow K = \frac{20}{0.06} \text{ N/m}$$

$$W = \frac{1}{2} K (x_i^2 - x_f^2)$$

$$= \frac{1}{2} \left(\frac{20}{0.06}\right) ((0.06)^2 - (0.16)^2)$$

$$= -3.66$$

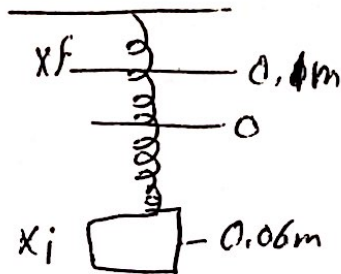


$$(29) K = \frac{20}{0.06}$$

$$W = \frac{1}{2} K (x_i^2 - x_f^2)$$

$$= \frac{1}{2} \left(\frac{20}{0.06} \right) (0.06^2 - 0.1^2)$$

$$= -1.06 \text{ J}$$



$$(34) T = \frac{mv^2}{R}$$

الجل ينقطع اذا زادت (T) عن (16M)
اكثر طاقة حركية يمكن الحصول عليها تكون
عند اكبر سرعة / واكثر سرعة يمكن الحصول
عليها بحيث لا ينقطع الجل عندما تكون

$$T = 16$$

$$T = 16 = \frac{mv^2}{0.5}$$

$$v^2 = \frac{8}{m} \quad (1)$$

$$K_{\max} = \frac{1}{2} m v^2 = \frac{1}{2} m \left(\frac{8}{m} \right) = \frac{8}{2} = 4 \text{ J}$$

(35) بما ان الطاقة الحركية لا تعتمد على
التسارع بتالي تكون متساوية للجسمين
لهما نفس الكتلة ويتحركان بنفس السرعة
في كوكبين مختلفين

$$K_{\text{moon}} = \frac{1}{2} m v^2$$

$$K_{\text{Earth}} = \frac{1}{2} m v^2$$

$$K_{\text{moon}} : K_{\text{Earth}} = 1 : 1$$

نظرة: الكتلة تختلف
كوكب اخر اختلاف في
الوزن لا يختلف من
ذات اخر

$$(36) \text{ الجواب C}$$

$$K = \frac{1}{2} m v^2 = K_g m^2 = \frac{M L^2}{s^2} \rightarrow \text{مسافة} \rightarrow \frac{M L^2}{T^2} \rightarrow \text{زمن}$$

$$(37)$$



$$W = \Delta K = K_f - K_i$$

$$W = K_f - K_i = 0 - K_i$$

$$W = -\frac{1}{2} m v^2 = \text{Kinetic energy of the object}$$

$$(30) \text{ الجسم : } K_1 = \frac{1}{2} m v^2 = \frac{1}{2} (3M) (v)^2 = \frac{3}{2} M v^2$$

$$\text{الجسم الثاني : } K_2 = \frac{1}{2} (3M) (2v)^2 = \frac{1}{2} (3M) (4v^2) = 6 M v^2$$

$$\text{الجسم الثالث : } K_3 = \frac{1}{2} (2M) (3v)^2 = 9 M v^2$$

$$\text{الجسم الرابع : } K_4 = \frac{1}{2} (M) (4v)^2 = 8 M v^2$$

$$\text{الجسم الخامس : } K_5 = \frac{1}{2} (M) (5v)^2 = 12.5 M v^2$$

الجسم الثالث له اكبر طاقة حركية

$$K_3 > K_4 > K_2 > K_1$$

$$(31) V_x = \frac{1}{2} m v_x^2 = \frac{1}{2} (500) v^2 = 250 v^2$$

$$V_y = \frac{1}{2} m v_y^2 = \frac{1}{2} (2000) v^2 = 1000 v^2$$

$$V_x = \frac{1}{4} V_y$$

$$V_y : V_x = 4 : 1$$

$$V_i = 12 \text{ m/s} \quad V_f = 0$$

$$(32)$$

$$\Delta K = K_f - K_i$$

$$= \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2$$

$$= 0 - \frac{1}{2} \left(\frac{8000}{9.8} \right) (12)^2$$

$$= -58775.5$$

$$= -5.9 \times 10^4 \text{ J}$$

$$(33) W = \Delta K = K_f - K_i$$

$$W = K_f - K_i$$

$$W = \frac{1}{2} m (v_f^2 - v_i^2)$$

يكون الشغل موجب عندما تكون

$$v_f^2 > v_i^2$$

$$38) W_{net} = \Delta K.E = K_f - K_i$$

$$= \frac{1}{2} m (v_f^2 - v_i^2)$$

$$= \frac{1}{2} (5) ((10)^2 - (6)^2)$$

$$= 160 \text{ J}$$

$$9) W = \Delta K.E = K_f - K_i = K_f - 0$$

$$W = \frac{1}{2} m v^2$$

$$W \propto v^2$$

الشفط يتناسب طردياً مع v^2



$$40) W = F_r \cdot d$$

نحتاج لمعرفة d كما ان F_r متغيرة تكون متغيرة حتى تصبح $V = V_t$ ومن ثم تثبت ونقيس مساهمة mg بتأثيرها الى منحنى F_r vs t

$$1) W = \Delta K = \frac{1}{2} m (v_f^2 - v_i^2)$$

$$= \frac{1}{2} (4) (0 - (3)^2)$$

$$= -18 \text{ J}$$

$$2) W = F \cdot d = \Delta K.E = K_f - K_i$$

$$(F_1)(d_1)(1) = 0 - K_{i1}$$

$$F_2(d_2)(1) = 0 - K_{i2}$$

$$F_1 = F_2$$

$$K_{i1} = K_{i2}$$

$$d_1 = d_2$$

$$43) W = f \cdot d = \Delta K = K_f - K_i$$

$$(F)(d)(-1) = 0 - \frac{1}{2} m v^2$$

$$f d = \frac{m v^2}{2} \Rightarrow f = \frac{m v^2}{2 \cdot d}$$

44

$$W = f \cdot d = \Delta K.E = K_f - K_i$$

$$(3)(2\pi R^2) = \frac{1}{2} m v^2 - 0$$

$$v = \sqrt{\frac{(3)(2\pi R^2)(2)}{m}}$$

$$= \sqrt{\frac{6(2\pi(2.5))}{0.5}}$$

$$v = \sqrt{188.5} = 13.7 \text{ m/s} \approx 14$$



45

المطلوب حساب قوة الشد

$$T = \frac{m v^2}{R} = \frac{(0.5)(13.7)^2}{2.5} = 37.7 \text{ J}$$

46

$$\Delta E_m = \Delta K + \Delta U = 0$$

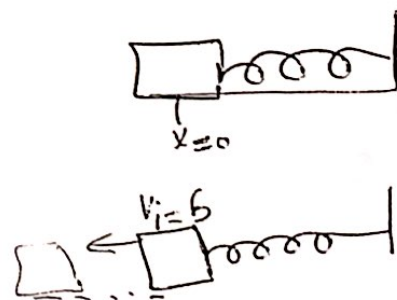
$$K_f - K_i + U_f - U_i = 0$$

$$0 - \frac{1}{2} m v_i^2 + \frac{1}{2} k x_f^2 - 0 = 0$$

$$\frac{1}{2} m v_i^2 = \frac{1}{2} k x_f^2$$

$$x_f = \sqrt{\frac{m v_i^2}{k}}$$

$$= \sqrt{\frac{(2)(25)}{200}} = \sqrt{0.25} = 0.5 \text{ m}$$



(47) ~~بما ان الطاقة الحركية تزداد~~
 لشكل منتظم مع مرور الوقت بتالي

$$K \cdot f(t) = C t$$

$$\frac{1}{2} m v^2 = C t \Rightarrow v = \sqrt{\frac{2 C t}{m}} = \sqrt{\frac{2 C}{m}} \sqrt{t}$$

$$a = \frac{dv}{dt} = \sqrt{\frac{2 C}{m}} \frac{1}{2 \sqrt{t}}$$

$$F = m a = \left(\frac{m}{2} \sqrt{\frac{2 C}{m}} \right) \frac{1}{\sqrt{t}}$$

$$F \propto \frac{1}{\sqrt{t}}$$

$$(48) v_i = \sqrt{(4)^2 + (3)^2} = 5$$

$$v_f^2 = (2)^2 + (3)^2 = 13$$

$$W = \Delta K = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2$$

$$= \frac{1}{2} (2) (13) - \frac{1}{2} (2) (25)$$

$$= 13 - 25 = -12 J$$

$$(49) f = c t$$

$$m a = c t$$

$$a = \frac{c t}{m}$$

$$v = \int_0^t a dt = \int_0^t \frac{c}{m} t dt$$

$$v = \frac{c}{2m} t^2$$

$$K.E = \frac{1}{2} m v^2 = \frac{1}{2} m \left(\frac{c}{2m} t^2 \right)^2$$

$$K.E = \left[\frac{c^2}{4m} \right] t^4$$

$$K.E \propto t^4$$

$$(50) \text{reading of scale} = f = k x$$

$$v_f^2 = v_i^2 + 2 g y$$

$$v_f^2 = 0 + (2)(10)(2)$$

$$v_f^2 = 40$$

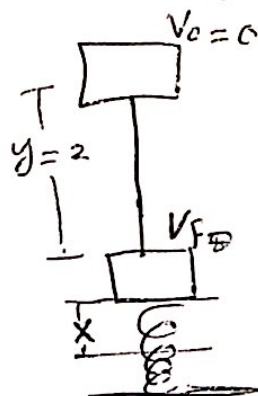
من قانون حفظ الطاقة الميكانيكية

$$\Delta K = \Delta U$$

$$\frac{1}{2} m v_f^2 = \frac{1}{2} k x^2$$

$$x = \sqrt{\frac{40}{105}} = 0.02$$

$$F = k x = (1.5 \times 10^5) (0.02) = 3 \times 10^3 N$$



$$(51) W = f \cdot d = \frac{1}{2} m v^2$$

$$F = \frac{m v^2}{2 d} = \frac{m}{L} \frac{L^2}{t^2} = \frac{m L}{t^2}$$

$$F = F_0 e^{-k x}$$

وبما ان

$$F_0 = \frac{m L}{t^2}$$

بتالي

$$k = \frac{1}{L}$$

$$k = \frac{1}{x} = \frac{1}{L}$$

$$k \cdot E = \frac{m L^2}{t^2}$$

يتبين ان الاجابة

$$(a) \frac{F_0}{k} = \frac{m L}{\frac{1}{L} t^2} = \frac{m L^2}{t^2} = K.E \quad \checkmark$$

$$(b) \frac{F_0}{e^{k x}} \quad \text{لا يجوز ان يكون } (e^{\frac{1}{L}})$$

$$(c) k F_0 = \left(\frac{1}{L} \right) \left(\frac{m L}{t^2} \right) = \frac{m}{t^2} \neq K.E \quad \times$$

$$(d) \frac{1}{2 (k F_0)^2} = \frac{1}{\left(\frac{m}{t^2} \right)^2} = \frac{t^4}{m^2} \neq K.E \quad \times$$

$$(e) k e^{k F_0} \quad \times \quad \text{لا يجوز ان يكون } (e^{\frac{1}{L}})$$

الشيء بين القوة التي بذلها الارتفاع إلى القوة التي تؤثر بها

بما أن الارتفاع المواد رفع الجسم (3) إليه يساوي من الخاليات بتالي فإن رفع الجسم بشكل عمودي يحتاج إلى قوة أكبر من القوة اللازمة لرفع في

Watt
وحدة قياس Power

$$= f \cdot v = (ma) \cdot v$$

$$= (kg) \left(\frac{m}{s^2} \right) \left(\frac{m}{s} \right)$$

$$= kg \cdot m^2/s^3$$

من السؤال السابق

$$= kg \cdot m^2/s^3$$

$$= mL^2/T^3$$

Watt → وحدة قياس القدرة
أما باقي الوحدات لطاقة

7) $ma = F = \text{Newton}$

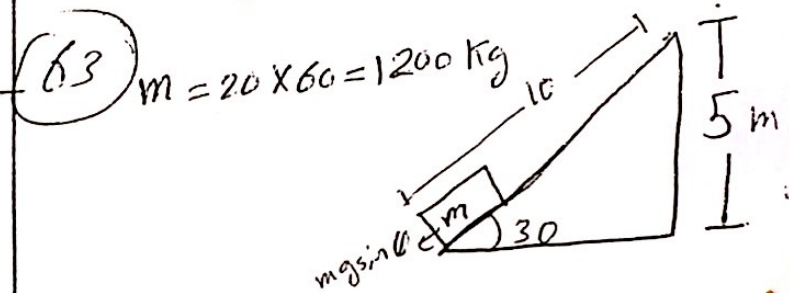
8) $\text{Watt} \cdot \text{second} = (P)(t) = \frac{W}{t}(t) = W$
= Energy

1) KiloWatt - hours
وحدة قياس الطاقة
Work

U1 $W = mgh$
 $h = 2R = 40 \text{ m}$
 $m = 0.01 \text{ kg}$
 $W = (0.01)(40)(40) = 4 \text{ J}$

ملاحظة: الشغل لا يعتمد على الوقت
و بتالي (0.75 min) لا فائدة منها
Power P فإنه يعتمد على الوقت
 $P = \frac{W}{\Delta t}$

62 الشغل لا يعتمد على الوقت والمبايعتم
على مقدار القوة ويعتمد أيضاً على نقطة
البداية ونقطة النهاية (الراحة)



$$P = f \cdot v = (mg \sin \theta) \left(\frac{10 \text{ m}}{60 \text{ s}} \right)$$

$$= (6000) \left(\frac{10}{60} \right) = 1000 \text{ watt}$$

64 $P = \frac{W}{\Delta t} = F \cdot v$

$$P = \frac{(80)(12)}{30} = 5.3 \text{ watt}$$

65 $F = ma$
 $v_0 = 0 \Rightarrow a = 25 \text{ m/s}^2$
 $2.1 \text{ kg} \Rightarrow f = 50 \text{ N}$

$$d = v_0 t + \frac{1}{2} a t^2$$

$$= 0 - \frac{1}{2} (25) (2)^2 = 50 \text{ m}$$

$$\text{Work} = f \cdot d = 50 \times 50 = 2500 \text{ J}$$

$$\text{rate of work } K \frac{\Delta W}{\Delta t} = \frac{2500}{2} = 1250 \text{ watt}$$

(66) $F = ma \Rightarrow a = \frac{F}{m}$
 $a = \frac{50}{2} = 25 \text{ m/s}^2$ $p = (v) \cdot b$
 $d = \cancel{v_0 t} + \frac{1}{2} a t^2$ $v^2 = v_0^2 + 2ax$
 $2 = 0 + \frac{1}{2} (25) t^2$ $v = \sqrt{\frac{1}{2} (25) (2)}$
 $t = \sqrt{0.16} = 0.4 \text{ s}$
 $w = f \cdot d = 50 \times 2 = 100$
the rate $\frac{w}{\Delta t} = \frac{100}{0.4} = 250 \text{ watt}$

(66) $F = ma$
 $a = \frac{F}{m} = \frac{50}{2} = 25 \text{ m/s}^2$
 $v^2 = v_0^2 + 2ax$
 $v^2 = 0 + 2(25)(2) = 100$
 $\boxed{v = 10}$
 $p = \frac{dw}{dt} = f \cdot v = (50)(10)(1)$
 $= 500 \text{ watt}$

(67) $\frac{w}{t} = ct$ $w = pt$
 $w = ct^2$ $w = \frac{1}{2} mv^2$
 $\frac{1}{2} mv^2 = ct^2$
 $v^2 = \frac{2c}{m} t^2$
 $v = \sqrt{\frac{2c}{m}} t$
 $v \propto t$

(67)

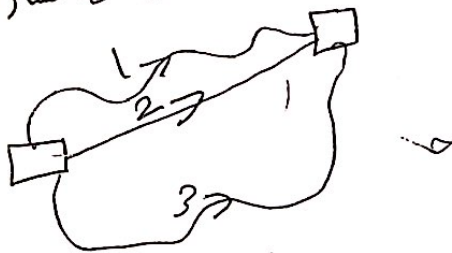
Chapter 8

إذا أثرت قوة محافظة على جسم فان مجموع الشغل لمسار متعلق بس

إعداد:

محمد الهدلح

إذا كانت القوة محافظة فان شغلها يعتمد على المسافة بين نقطة البداية والنهاية ولا يعتمد على المسار



$$W_1 = W_2 = W_3$$

بما ان كلا الجسمين عادا إلى نفس النقطة انطلقا منها فان طاقة الوضع تكون نفسها (لأنهما عادا إلى نفس الارتفاع)

$$L = -W_f = -f \cdot d$$

التغير في طاقة الوضع يساوي شغل القوة المؤثرة (يسبب العودة إلى نقطة البداية)

$$E_m = K + U$$

ولها ان سرعة كل من الجسمين قلتت يتالي الطاقة الحركية للجسم قلتت وبما ان $\Delta E_m \neq 0$ يتالي وجود تحول لطاقة أي أثرت قوة غير محافظة

$$E_m = K + U$$

$$E_m = K + U$$

$$E_m = K + U$$

$$E_m = K + U$$

السرعة كبيرة جداً فيها ان $K.E = \frac{1}{2} m v^2$ يتالي تكون الطاقة الحركية كبيرة جداً

8

في حالة الجسم الساكن تكون $v = 0$ فيها ان

$$K.E = \frac{1}{2} m v^2$$

$$K.E = 0$$

لا يوجد طاقة حركية

النار في الملقوف في الساعة ليملك طاقة حركية

10

الجسم الساكن في نظام بإمكانه ان يتحول لشغل إذا كان بإمكانه الحركة بحيث تقل طاقة الوضع الخاصة به إلى تزداد الطاقة الحركية له صبيح

$$W = \Delta K.E$$

$$U = -W_f = -f d \cos \theta$$

$$d = vt$$

$$U = fvt$$

$$U = FVT$$

13

$$U = -W_f = -\int f dx = -(مسافة)$$

$$مسافة 1 = \frac{1}{2} x_1 f_1 \Rightarrow U_1 = -\frac{1}{2} x_1 f_1$$

$$مسافة 2 = x_1 f_1 \Rightarrow U_2 = -x_1 f_2$$

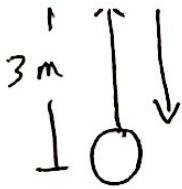
$$مسافة 3 = \frac{1}{2} x_1 f_1 \Rightarrow U_3 = \frac{1}{2} x_1 f_1$$

$$U_3 > U_2$$

الترتيب من الأكثر سالبية

$$2 > 1 > 3$$

(14)



أكبر طاقة وضع تكون عند أعلى ارتفاع حيث تكون الطاقة الحركية تساوي صفر ($V=0$) وذلك لأن

$$U = mgh$$

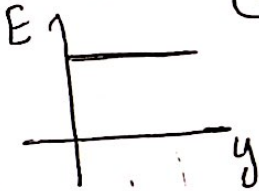
الحال ارتفاع ثابت

(15)

بما أن مقاومة الهواء يمكن تجاهلها يتالي

$$\Delta E_m = 0$$

أي أن الطاقة الميكانيكية محفوظة (تبقى ثابتة)



(16)

$$V_{60m}^2 = V_0^2 + 2gh$$

$$V^2 = 0 + (2)(10)(60) = 1200$$

$$V^2 = 1200$$

$$K.E = \frac{1}{2} m V^2 = \frac{1}{2} (6)(1200) = 3600$$

أو بطريقة أخرى

at height 80 m

$$E_m = U + K = U + 0 = mgh = (6)(10)(80) = 4800$$

at height 60

$$\Delta E_m = 0$$

$$E_m = E_m$$

$$4800 = U + K = mgh + K = (6)(10)(60) + K$$

$$K = 4800 - 1200 = 3600$$

(17)

المطلوب! متى تكون $\Delta U = 500 \text{ J}$

$$\Delta U = mgh = (2)(9.8)(20) = 392 \text{ J}$$

$$\Delta U = U_f - U_i = 500$$

$$mg(h_f - h_0) = 500$$

$$h_f - h_0 = \frac{500}{mg} = \frac{500}{19.6} = 25.5$$

$$h_f = h_0 + 25.5 = 20 + 25.5 = 45.5$$

(18)

بما أن المصعد يرتفع بسرعة ثابتة فان تسارعه يساوي صفر

$$a = \frac{v}{t} = 0$$

الطاقة الحركية له ثابتة

$$\Delta K = mg(V_f - V_i) = mg(0) = 0$$

وبما أن يترك بسرعة ثابتة فان القوة المؤثرة عليه تكون ثابتة

(19)

$$K.E (\text{vertical component}) =$$

$$= \frac{1}{2} m (V \sin 60) = \frac{1}{2} \left(\frac{1}{2}\right) (8.6)$$

$$= \frac{7.5}{4} = 18.75$$

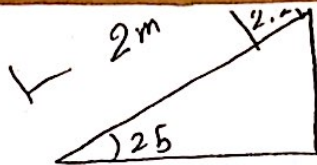
(20)

لكي يصل إلى ارتفاع (h)

يجب أن يمتلك على الأقل طاقة حركية تساوي طاقة الوضع عند ارتفاع h

$$K = U = mgh$$

1) $\mu_k = .25$



$$\Delta E_m + \Delta E_{bh} = 0$$

$$E_m = \Delta E_{bh} = W f_k = (\mu_k N) d \cos 180$$

$$= -\mu_k (mg \cos 25) (2)$$

$$= -(0.25)(2.2)(9.8)(\cos 25)(2)$$

$$= -9.8$$

2) $U = K$

$$mgh = \frac{1}{2} k v^2$$

$$v^2 = 2gh$$

$$v = \sqrt{2gh}$$

$$= \sqrt{(2)(9.8)(1.85)}$$

$$= 6.02 \text{ m/s}$$

3) $\Delta E_m = 0$

$$E_{mf} = E_{mi}$$

~~$$K_f + U_f = K_i + U_i$$~~

$$K_f + U_f = K_i + U_i$$

$$\frac{1}{2} m v_f^2 + 0 = \frac{1}{2} m v_i^2 + mgh$$

$$v_f^2 = \left(\frac{1}{2}\right)(3)^2 + (9.8)(0.5)$$

$$v_f^2 = 4.5 + 4.9 = 9.4$$

$$v = \sqrt{(2)(9.4)} = 4.3 \text{ m/s}$$

4) $f = -\frac{du}{dx} \Rightarrow du = -f dx$

$$\int du = \int f dx$$

$$U - U_0 = -\int 8x^3 dx = -2x^4$$

$$U - 0 = -2x^4$$

$$U = -2x^4$$

25) at $x=1 \Rightarrow U(1) = 80$

$$K(1) = \frac{1}{2} m v^2 = \frac{1}{2} (0.2) (5)^2 = 2.5$$

$$E_{at(x=1)} = E_m = U(1) + K(1) = 82.5$$

$$\Delta E_m = 0$$

$$E_{m0} = E_{m1}$$

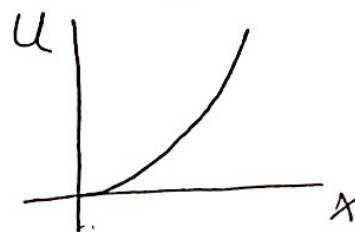
$$K_0 + U_0 = 82.5$$

$$\frac{1}{2} m v^2 + 0 = 82.5$$

$$v = \sqrt{125} = 11.1 \text{ m/s}$$

26) $U = \frac{1}{2} k x^2$

اقتران تربيعي



27) $U = \frac{1}{2} k x^2$

$$f = -\frac{du}{dx} = -kx$$

$$10 = -20x \Rightarrow x = -\frac{1}{2}$$

$$U = \frac{1}{2} (20) \left(-\frac{1}{2}\right)^2 = \frac{20}{8} = 2.5$$

28) طاقة الوضع تتحول الى طاقة حركية

$$U = K \quad x_0 = 0.07 \text{ m}$$

$$\frac{1}{2} k x^2 = \frac{1}{2} m v^2$$

$$\left(\frac{1}{2}\right)(20)(0.07)^2 = \frac{1}{2} (0.015) v^2$$

$$v = \sqrt{6.533} = 2.556$$

$$K.E = \frac{1}{2} m v^2 = \frac{1}{2} (0.015) (2.556)^2$$

$$= 0.049$$

(29) $E_m = U + K = U + 0$
 $0.12 = \frac{1}{2} K x^2$
 $x = \sqrt{\frac{(2)(0.12)}{80}} = 0.054$

(30) $E_m = U + K = 0 + K$
 $0.12 = \frac{1}{2} m v^2$
 $v = \sqrt{\frac{(2)(0.12)}{0.5}} = 0.692 \text{ m/s}$

(31) ~~When~~ when the spring is 4 cm
 $E_m = U + K = \frac{1}{2} K x^2 + \frac{1}{2} m v^2$
 $E_m = (\frac{1}{2})(80)(0.04)^2 + \frac{1}{2}(0.5)(0.5)^2$
 $E_m = 0.064 + 0.0625 = 0.1265 \text{ J}$
 $\Delta E_m = 0$
 $E_{m_i} = E_m$

$0.1265 = K + U = K + 0$

$0.1265 = \frac{1}{2} m v_{\max}^2$

$v_{\max} = \sqrt{\frac{(2)(0.1265)}{(0.5)}} = 0.71 \text{ m/s}$

(32) طاقة الحركة تتحول إلى
 طاقة وضع

$\frac{1}{2} m v^2 = \frac{1}{2} K x^2$

$(\frac{1}{2})(\frac{1}{2})(2)^2 = \frac{1}{2}(800)^2 x^2$

$x = \sqrt{\frac{1}{400}} = 0.05 \text{ m} = 5 \text{ cm}$

(33) $K E = U$
 $\frac{1}{2} m v^2 = \frac{1}{2} K x^2$

$x^2 = \frac{m v^2}{K} \Rightarrow x = v \sqrt{\frac{m}{K}}$

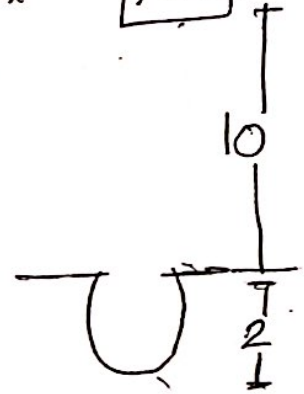
~~$\frac{1}{2} K x^2 = \frac{1}{2} K (\frac{m v^2}{K})$~~

(34) $mgh = \frac{1}{2} K x^2$

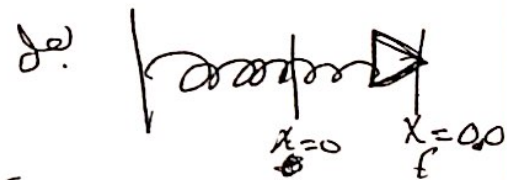
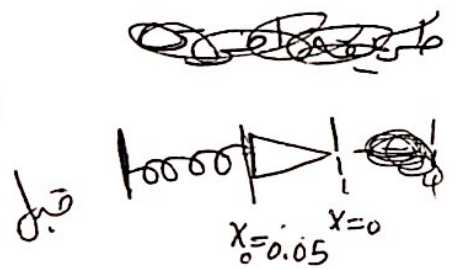
$(700)(12) = \frac{1}{2} K x^2$

$\frac{1}{2} K x^2 = 8400$

700 N



(35)



$\Delta E_m = 0$

$E_{m_i} = E_{m_f}$

$U_i + K_i = U_f + K_f$

$\frac{1}{2} K x_i^2 + 0 = \frac{1}{2} K x_f^2 + \frac{1}{2} m v^2$

$v^2 = \frac{K x_i^2 - K x_f^2}{m}$

$v^2 = \frac{(10)(0.05)^2 - (10)(0.01)^2}{(0.005)}$

$v^2 = 4$

$v = 2$

$$36) mgr = \frac{1}{2} mv^2$$

$$v^2 = 2gr$$

$$\sum F = ma = \frac{mv^2}{r} = \frac{m(2gr)}{r} = 2mg$$

$$\sum F = T - mg = 2mg$$

$$T = 3mg$$

$$37) mgh = \frac{1}{2} mv^2$$

$$h = r$$

$$v^2 = 2gr = 2(9.8)(0.5)$$

$$v = \sqrt{9.8} = 3.13 \text{ m/s}$$

$$38) \Delta E_m = 0 \quad E_{m1} = E_{m2}$$

$$mgh_1 = mgh_2 + \frac{1}{2} mv^2$$

$$= 2g(h_1 - h_2)$$

$$= \sqrt{2g(h_1 - h_2)}$$

$$1) \cancel{mgh(2r+h)} = \cancel{mg(2r)} + \frac{1}{2} mv^2$$

لا نأخذ الطاقة الكامنة صفرية السطح لتفقد

$$mg(2r+h) = mg(2r) + \frac{1}{2} mv^2$$

$$2mgr + mgh = 2mgr + \frac{1}{2} mv^2$$

$$gh = \frac{v^2}{2} \quad (1)$$

عند

$$\sum F = ma$$

$$mg = \frac{mv^2}{r}$$

$$v^2 = gr$$

$$1) \text{ لا يمكن أن } v$$

$$gh = \frac{gr}{2}$$

$$u = \frac{r}{2}$$

$$40) F = ma = \frac{mv^2}{r}$$

$$mg = \frac{mv^2}{r}$$

$$v = \sqrt{gr} = \sqrt{\left(\frac{3}{2}\right)(9.8)} = 3.8 \text{ m/s}$$

41) عند أعلى ارتفاع (Point 3) يكون
السرير يمتلك أقل طاقة حركية
وأكثر طاقة وضع وبما أن

$$\Delta E_m = 0$$

$$E_{m1} = E_{m2}$$

$$\cancel{K_1 + U_1} = \cancel{K_2 + U_2}$$

$$K_1 + U_1 = K_2 + U_2 = E_m$$

$$E_{m1} = K_2 + U_2$$

$$E_{m1} = E_{m2} = U + K$$

$$E_m = mgh + \frac{1}{2} mv^2$$

عند أعلى ارتفاع يكون هذا
السرير أكبر ما يمكن
وبما أن تكون الطاقة الحركية
أقل ما يمكن وبما أن
 $K.E = \frac{1}{2} mv^2$
تأخذ السرعة أقل ما يمكن

42) at the bottom of circle

$$\sum F = ma = \frac{mv^2}{L}$$

$$T - mg =$$



(42)

$$\Delta E_m = 0$$

$$E_{m_{top}} = E_{m_{bottom}}$$



$$K + U = K + U$$

$$\frac{1}{2} m v_{top}^2 + m g (2L) = \frac{1}{2} m v_{bottom}^2 + 0$$

$$\frac{v_{top}^2}{2} + 2gL = \frac{v_{bottom}^2}{2} \rightarrow (1)$$

at the top

$$\Sigma F = ma = m \frac{v^2}{r}$$

$$m g = m \frac{v^2}{L}$$

$$v^2 = gL$$

من المعادلة ①

$$\frac{gL}{2} + 2gL = \frac{v^2}{2}$$

$$v_{bottom}^2 = 5gL$$

$$v = \sqrt{5gL}$$

(44)

the limits of motion are

when $U = E_m$

when K.E = zero

$$8x^2 + 2x^4 = 9 \quad \text{J}$$

بالجريب

$$8(0.96)^2 + 2(0.96)^4 \stackrel{?}{=} 9$$

$$a = 9$$

بإلى الجواب

$$(-0.96 \text{ m}, 0.96 \text{ m})$$



$$-0.96 \quad 0 \quad 0.96$$

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(45)

$$K(1) = \frac{1}{2} m v^2 = \frac{1}{2} (0.2) (20)^2 = 20$$

$$U(1) = 8 + 2 = 10$$

$$E_{m1} = 10 + 20 = 30$$

~~when it stop~~

$$\Delta E_m = 0$$

$$E_m = E_m$$

$$K(1) + U(1) = K + U$$

when it stop

$$K(1) + U(1) = 0 + U$$

$$E_{m1} = U$$

$$8x^2 + 2x^4 = 30$$

بالجريب

$$8(1.1)^2 + 2(1.1)^4 \stackrel{?}{=} 30$$

$$30 = 30$$

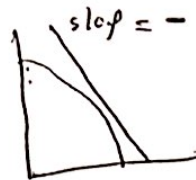
وبما انه كان يتحرك على محور السينات
الموجبة (مضطرب) بآلى قابل يسكن
عسا

$$x = +1.1$$

(46)

$$F = -\frac{du}{dt}$$

(F) is positive when

 $\frac{du}{dt}$ is ~~positive~~ negative $F = (-)(-) =$ that when U is ~~de~~creasing function

$$F = -\frac{du}{dx}$$

$$|F| = \left| \frac{du}{dx} \right|$$

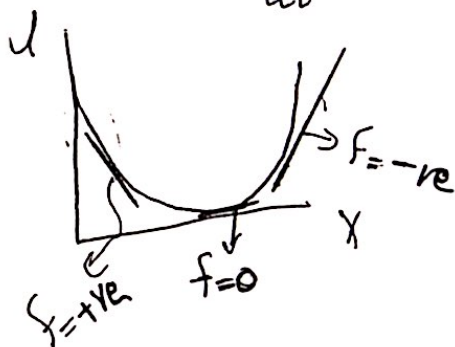
$$C = 0$$

$$AB < CD$$

بما ان (F) تزداد على القيمة المطلقة للميل

$$CD > AB > BC$$

$$(48) F = -\frac{du}{dx}$$

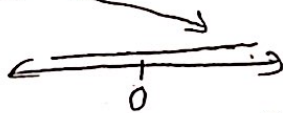


بما ان اقتران (U-x) يشبه الاقتران التربيعي

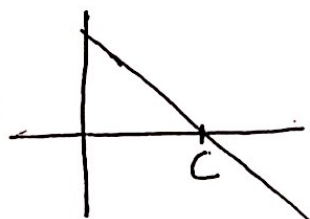
$$U = (x-c)^2$$

$$F = -\frac{du}{dx} = -2(x-c) \Rightarrow x=c$$

$$\frac{dF}{dx} = -2$$

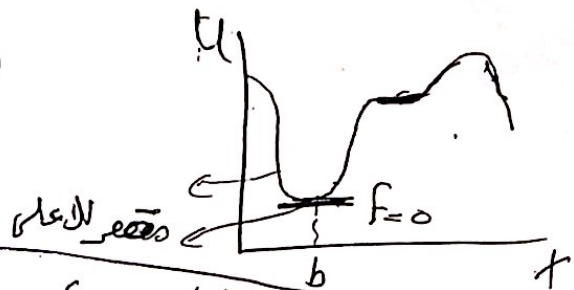


F decreasing (تقلو)



(49) The Point of stable equilibrium
 نقطة تكون عندها $F=0$ والاقتزان
 مقدار (U-x)

only b



(50) The Point of ~~stable~~ unstable equilibrium
 نقطة تكون عندها $F=0$ والاقتزان
 مقدار (U-x)

only d



(51) The Point of neutral equilibrium
 نقطة تكون عندها مقدار U ثابت
 مع تغير x



only c

$$(52) U = -mgx + \frac{1}{2}Kx^2$$

$$F = -\frac{du}{dx} = -(mg + Kx)$$

$$F = mg - Kx$$

(53) $f = ma_1 = -\frac{du}{dx}$

$\frac{du}{dx}|_{x=1} = 16x + 8x^3 = 16 + 8 = 24$

$F = -24 = m \cdot a$

$a = \frac{-24}{m} = \frac{-24}{0.2} = -120$

(53) لوجد خطأ من السؤال
الصحیح

$U(x) = 8x^2 - 2x^4$

$F = -\frac{du}{dx} = ma$

$\frac{du}{dx}|_{x=1} = 16x - 8x^3 = 16 - 8 = 8$

$F = -8 = ma$

$a = \frac{-8}{m} = \frac{-8}{0.2} = -40 \text{ m/s}^2$

(54) $U = Ax^{-12} - Bx^{-6}$

$F = -\frac{dU}{dx} = -\left(-\frac{12A}{x^{13}} + \frac{6B}{x^7}\right)$

$= 12A/x^{13} - 6B/x^7$

(56)

(57)

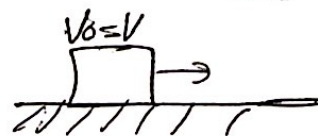
$\Delta E_m + \Delta E_{int} = 0$

$\Delta K + \Delta u + \Delta E_{th} = 0$

$\Delta K + 0 + \Delta E_{th} = 0$

$\Delta K + \Delta E_{th} = 0$

السؤال الذي يجب أن نغيره
الطاقة الحركية والطاقة الداخلية فقط



(58)

$\Delta E_m + \Delta E_{int} = 0$

$\Delta K + \Delta u + 15 = 0$

$K_f - 0 + 0 - U_i + 15 = 0$

$\frac{1}{2}mv^2 - mgh + 15 = 0$

$\frac{1}{2}mv^2 = mgh - 15 = 19.6 - 15 = 4.6$

$V^2 = \frac{(2)(4.6)}{0.025} = 368 \Rightarrow V = 19.1 \text{ m/s}$

$V_0 = 0.025$

(60)

$\Delta E_m + \Delta E_{th} = 0 \Rightarrow \Delta E_{th} = -\Delta E_m$

$\Delta E_{th} = \Delta E_m = -\Delta K + \Delta U = -\Delta K +$

$\Delta E_{th} = -\Delta K = \frac{1}{2}m(V_i^2 - V_f^2) = \frac{1}{2}(5)(200^2 - 15^2)$

$\Delta E_{th} = 44000 \text{ J}$

(61)

$\Delta E_m + \Delta E_{int} = 0 \Rightarrow \Delta E_{int} = -\Delta K + \Delta U$

$\Delta E_{int} = K_i - K_f + U_i - U_f = \frac{1}{2}mv^2 = 0 + 0 - \frac{1}{2}Kx^2$

$\Delta E_{int} = -\left(\frac{1}{2}(0.75)(3.5)^2 - \frac{1}{2}(1200)(0.057)^2\right) = -2.0$

CHAPTER 9

1) **Ans: E** "None of these"

2) **Ans: C** $6 \text{ kg}(1,3) \text{ m} / 4 \text{ kg}(0,0) \text{ m} / 5 \text{ kg}(3,2) \text{ m}$

$$X_{\text{com}} = \frac{m_1 x_1 + m_2 x_2 + m_3 x_3}{\Sigma M}$$

$$= \frac{4(0) + 6(1) + 5(3)}{15} = 1.4$$

Y_{com} the same 1.9
 $Y_{\text{com}} = 1.9 \text{ m}$
 Com (1.4, 1.9)

3) **Ans: E** the center of the circle

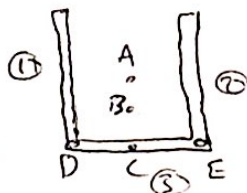


4) **Ans: B** Closer to the sun than the Earth or Mars
 bcz the mass of the sun is very large
 $M_{\text{sun}} \gg (M_{\text{Earth}} + M_{\text{Mars}})$

5) **Ans: D** "near the center of Earth"

6) **Ans: B**

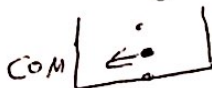
The center of 1, 2, 3 is in the midway between the ends across the thickness



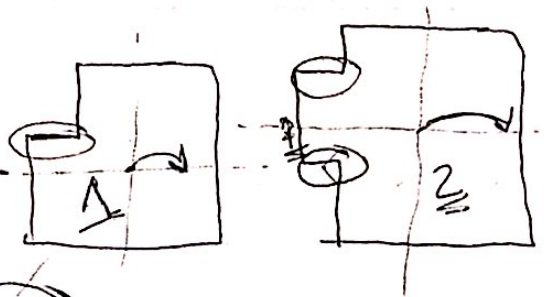
the center between 1, 2 in the mid way between



the center "1, 2" and "3" then is in the midway between them



7) **Ans: E**



the loss in X in 1 is the same as 3 bcz in 3 there is cuts from both right and left sides. But in 2 the loss is greater bcz there is 2 cuts from the left side only.

8) **Ans: B**
 $V_{\text{com}} = \frac{V_1 m_1 + V_2 m_2}{M}$

$$= \frac{(4)(2) + (8)(3)}{12} = 7.3 \text{ m/s}$$

9) **Ans: D** we find the height of the two balls after 2 s by $y = v_0 t + \frac{1}{2} a t^2$

$$H_1 = 25 - y_1 \Rightarrow H_1 = 25 - 19.6 = 5.4 \text{ m}$$

$$H_2 = y_2 = 10.4 \text{ m}$$

$$H_{\text{com}} = \frac{m_1 h_1 + m_2 h_2}{M} = \frac{(5.4)(0.5) + (10.4)(0.25)}{0.75}$$

$$\approx 7.1 \text{ m}$$

10) **Ans: C** we first find V after 2 sec.

$$\text{by } V_2 = v_0 + at \Rightarrow V_1 = 19.6 / V_2 = 4.6$$

$$V_{\text{com}} = \frac{V_1 m_1 + V_2 m_2}{M} = \frac{(19.6)(0.5) + (0.25)(4.6)}{0.75}$$

$$= 15.026 \approx 15 \text{ m/s}$$

11) **Ans: D** $a=g$ the acceleration never changes when the particles moves within the range of the Earth

12) **Ans: E** None of these

13) **Ans: B** since the two objects are the same with the same initial conditions the center of mass of displacement is the displacement of one of them.

In this question we are considered in vertical D, as the v_y at "L" is zero, the question is free fall: $y = v_y t + \frac{1}{2} a t^2 \Rightarrow 0 + \frac{1}{2} (10)(4) = 20$

14) **Ans: B** $\sum F_{ext} = 0$

15) **Ans: A** $v=0$ & $\sum F_{ext} = 0$

16) **Ans: E** is rearward of its original place & not moving.

17) **Ans: B** since the bear will move $\frac{1}{5} \times 20 = 3.3 \text{ m}$

18) **Ans: A** the same as 17 the 60 kg boy will move $\frac{10}{2.5} = 4 \text{ m}$

19) **Ans: C** $\vec{F} = \sum \vec{F}_{ext} / m = m_{system}$

20) **Ans: B** the same as 17 & 18 so $v_1 = 2v_2$ for the Hz comp. $v_2 = \frac{6}{2} = 3 \text{ m/s}$

21) **Ans: D** the motion was started with at least one of masses moving

22) **Ans: B** $E = \frac{1}{2} k x^2 = \frac{1}{2} (100) (0.1)^2 = 0.5$
 $E_{mg} = \frac{1}{2} m v^2 = \frac{1}{2} (2) (0.3)^2 = 0.18$
 $\Delta E_m = 0.18 - 0.5 = -0.32$

23) **Ans: C** $dp = J \Rightarrow J = \Delta p = F \cdot t$

24) **Ans: E** acceleration

25) **Ans: D** $p = \sqrt{2} \text{ km}$ $m_g = 9 \text{ mb}$

$\frac{P_a}{P_b} = \frac{\sqrt{2} \text{ kg ma}}{\sqrt{2} \text{ kg mb}} \Rightarrow \frac{P_a}{P_b} = \frac{\sqrt{9 \text{ mb}}}{\sqrt{20}}$

$\frac{P_a}{P_b} = \frac{3}{1}$

26) **Ans: B** "is moving faster"

27) **Ans: B** F is the slope in P_V vs t graph

28) **Ans: D** $dp = m \Delta v = 1(1.5 - 2) = -0.5$

29) **Ans: D** $\sum F_{ext} \neq 0$

30) **Ans: B** "the force of friction of the wire"

31) **Ans: A** $V = v_0 + at \Rightarrow v = 39.2$
 $P = mv = (39.2)(2.5) = 98$

41) **Ans: D** $P_b = P_a \Rightarrow m_1 v_1 = (m_1 + m_2) v$
 $2000 \times 3 = (2000 + 500) v \Rightarrow v = 2.4 \text{ m/s}$

32) **Ans: B** $m_1 v_{1b} + m_2 v_{2b} = m_1 v_{1a} + m_2 v_{2a}$
 $0 = (84)(0.0017) + 0.1 v_{2a}$
 $v_{2a} = -1.1$

42) **Ans: E** "Zero"

43) **Ans: B** "the force of the existing fuel gases"

33) **Ans: C** the same as 32 $V = 8.3 \times 10^{-2}$ 44) **Ans: C** Thrust $= V_{rel} \frac{dM}{dt} = (1500)(100) = 1.5 \times 10^5$

34) **Ans: B** the same as 32, 33 $V = 0.38 \text{ m/s}$ 45) **Ans: B** $v_f - v_i = V_{rel} \ln \left(\frac{M_i}{M_f} \right)$
 $\Rightarrow v_f = 1500 \ln \left(\frac{1}{0.2} \right) = 2414 \approx 2400 \text{ m/s}$

35) **Ans: A** P is conserved in explosion

36) **Ans: C** $\frac{P_b}{P_a} = P_a \Rightarrow 0 = M v_1 + m_2 v_2$
 $V = \frac{-m_2 v_2}{M}$

46) **Ans: B** $v_f - v_i = V_{rel} \ln \left(\frac{M_i}{M_f} \right)$
 $\frac{70}{1500} = \ln \left(\frac{M_i}{M_f} \right) \Rightarrow 1.004 = \ln \left(\frac{M_i}{M_f} \right)$

$M_f = \frac{1000}{1.004} = 996 \Rightarrow 1000 - 996 = 4 \text{ kg}$

37) **Ans: C** $\frac{P_b}{P_a} = P_a \Rightarrow 0 = M v_1 + m_2 v_2$
 $\frac{P_{G1}}{P_{G2}} = \frac{m_{bullet1} v_1}{m_{bullet2} v_2} = \frac{2m_1}{m_2} = \frac{2}{1} (2001)$

47) **Ans: D** $J = \Delta p$

48) **Ans: D** $J_{ext} = 0 \Rightarrow F_{ext} = 0$

38) **Ans: A** Area under $(F vs t)$ graph $= J$
 $\Rightarrow J = \Delta p \Rightarrow \left(\frac{1}{2} \right) (4) (2) = m \Delta v$
 $\frac{4}{5} = v = 0.8$

49) **Ans: E** $J_{xy} = -J_{yx}$

50) **Ans: E** the same momentum for the other

39) **Ans: D** $F = \frac{\Delta p}{\Delta t}$

40) **Ans: B** $V_{comb} = V_{com after}$
 $V_{com} = \frac{m_1 v_1 + m_2 v_2}{M} = \frac{0.2 \times 3 + 0.4 \times 2}{0.6}$

51) **Ans: A** $J = \Delta p = m \Delta v$
 $= 0.2(20 - -30) = 10 \text{ upward}$

52) **Ans: C** $F_{ext} = \Delta p \Rightarrow 1 \times 1 = P_f - P_i$
 $P_f = +1 \text{ kg} \cdot \text{m/s}$

≈ 0.33

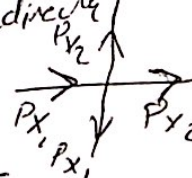
Ans: C

53) (Ans: C) ~ max in straight line

54) (Ans: C) $J = p p = +50$

55) (Ans: D) the airbags make it larger ~~and~~
so ~~J will be smaller~~ will be smaller
"exerts a much smaller force"

56) (Ans: C) $0P_x = P_{x1} - P_{x2} = 0$ same direction
 $0P_y = P_{y1} - P_{y2} = 2P_y > 0$



57) (Ans: B) $J = F \cdot t \Rightarrow F = \frac{J}{t}$
 $F = \frac{mV}{t}$

58) (Ans: E) "Impossible to determine for given data"

59) (Ans: E) "None of the choices"

60) (Ans: D) "a force for which the total momentum of the two objects is zero"

61) (Ans: D) P is covered of K is Not

62) (Ans: A) $P_{\text{before}} = P_{\text{after}}$
 $m_1 v_1 = (m_1 + m_2) V$
 $V = \frac{1.2}{1.2} = 1 \text{ m/s}$

63) (Ans: B) the same as 62
 $V = \frac{m_1 v_1}{(m_1 + m_2)} = \frac{0.399}{1.2} = 0.4$

64) (Ans: B) $P_b = P_{\text{after}} \Rightarrow m_1 v_1 = (m_1 + m_2) V$
 $V = 1.8$ $J = 0 P$
 $0P_2 = (1)(4) = 4 \text{ N.s}$

65) (Ans: B) $m_1 v_1 = (m_1 + m_2) V \rightarrow \sqrt{2gh}$
 $V = 0.245$ $V_1 = \frac{2.450}{0.003} = 816 \approx 8 \times 10^2$

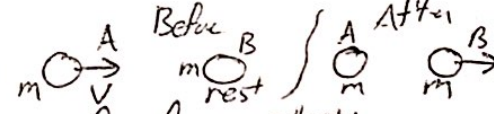
66) (Ans: C) $K = \frac{1}{2} m v^2$
 $40 = \frac{1}{2} (5) v^2$
 $V = 4 \text{ m/s}$

67) (Ans: C) $m_1 v_1 + m_2 v_2 = (m_1 + m_2) V_f$
 $V_f = 0 \Rightarrow 0K = K_f - K_i$
 $0K = \frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2 = 3750 \text{ J}$


68) (Ans: C) $\frac{1}{2} M_{\text{total}} V_{\text{com}}$

69) (Ans: D) $(m_1 + m_2) V_f = m_2 v_2$
 $V_f = \frac{(105)(2)}{30} = 7$ $0V = 7 - 2 = 5 \text{ m/s}$

70) (Ans: C) P & K are conserved

71) (Ans: E) 
the whole speed of elastic
A goes to B for elastic \Rightarrow proved by
 $(P_b = P_a) \& \left(\frac{v_2 - v_1}{v_1 - v_2} = 1 \right) \Rightarrow$ for B to have

the greatest K $m_B v_B = m_A$

72) (Ans: C) "A  elastic" it likes when
a ball strikes a wall in an elastic collision so
the ball will rebound with same speed &
the opposite direction $V_{\text{after}} = -5 \text{ m/s}$

$$V_{1a} = \frac{m_1 - m_2}{m_1 + m_2} (V_{1b}) + \frac{2m_2}{m_1 + m_2} (V_{2b})$$

73) (Ans: D)

$$SS = 0 + \frac{2m_2}{m_2} 10 = 20 \text{ m/s}$$



$$P_{\text{before}} = P_{\text{after}}$$

$$m_A V = m_A V_A + m_B V_B \Rightarrow mV = mV_A + 2mV_B$$

$$V = V_A + 2V_B \quad (1)$$

$$\Rightarrow \frac{V - 0}{V_B - V_A} = 1 \Rightarrow V = V_B - V_A \quad (2)$$

$$V_B - V_A = V_A + 2V_B \Rightarrow -V_B = 2V_A \quad \text{so} \quad \frac{V_A}{V_B} = \frac{1}{2}$$

$$\Rightarrow V_A = -\frac{V}{2} \quad | \quad V_B = \frac{2V}{3}$$

75) (Ans: A) By using $\Delta P = 0$ $V_{2a} - V_{1a} = V_{1b} - V_{2b}$

76

76) (Ans: E) "the incident and target particle have the same mass" the same as 71

77) (Ans: D) $x = \frac{2}{5}y \Rightarrow K = \frac{1}{2}mv^2 \Rightarrow K(x) = 50$ so $K(y) = 50 \times \frac{5}{2} = 125 \text{ J}$

78) (Ans: E) "the kinetic energy of the system is at a minimum"

79) (Ans: B) "if some other form of energy were changed to kinetic during the collision the report could be true" Because the K_{after} is larger than K_{before} and that impossible is if there is no other source of energy.

80) (Ans: A) $p_b = p_a \Rightarrow m v_0 = m v_1 + m v_2 \Rightarrow \boxed{v_0 = v_1 + v_2}$

$2K_b = K_a \Rightarrow 2\left(\frac{1}{2} m v_0^2\right) = \frac{1}{2} m v_1^2 + \frac{1}{2} m v_2^2 \Rightarrow \boxed{2v_0^2 = v_1^2 + v_2^2}$

$\Rightarrow \overset{①}{(5 = v_1 + v_2)} \quad \overset{②}{(50 = v_1^2 + v_2^2)} \quad \text{By solving these simultaneously}$

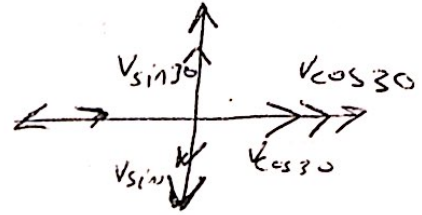
$\Rightarrow v_1 = 1.83 \text{ m/s}$

81) (Ans: B)



the same as [56] $\Rightarrow \underline{dp_x = 0} \quad \underline{dp_y = 2py}$

$= 2mv \sin 30$



عدد: 10 (اساتيف من ربيعه)

Chapter 10: Rotation

Test bank Answers

1 $\pi \rightarrow 180^\circ$
 $1 \rightarrow ??^\circ$

$X = \frac{180^\circ}{3.14} = 57.3^\circ$ ans: D

2 ans: E } 3 $\frac{1 \text{ rev}}{\text{min}} = \frac{2\pi \text{ rad}}{1 \times 60 \text{ s}} = 0.105 \text{ rad/s}$ ans: B

4 ans: C } 5 $T = \frac{2\pi}{\omega} = \frac{2\pi}{3} \approx 2.09 \approx 2.1 \text{ s}$ ans: E

6 $\omega = \frac{100 \times 2\pi}{10} \approx 63 \text{ rad/s}$ ans: E } 7 The second hand complete 1 rev/min
so $\omega = \frac{2\pi}{60} \text{ rad/s} = \pi/30 \text{ rad/s}$
ans: C

8 $\Delta\theta = \omega_i t + \frac{1}{2} \alpha t^2 \Rightarrow \alpha = \frac{2(\Delta\theta - \omega_i t)}{t^2} = \frac{2(450 - 20 \times 9)}{81} \approx 6.7 \text{ rad/s}^2$
ans: D

9 The min hand complete one rev/hour so $\omega = \frac{2\pi}{60 \times 60} = \left(\frac{\pi}{1800}\right) \text{ rad/s}$
ans: D

10 $\alpha_{\text{Avg}} = \frac{\Delta\omega}{\Delta t} = \frac{300(2\pi)}{60 \times 10} = 3.14 \text{ rad/s}^2$ ans: A

11 $\omega_f^2 = \omega_i^2 + 2\alpha \Delta\theta \Rightarrow \omega_i = \sqrt{4\pi^2 - 2\pi^2} = \sqrt{2} \pi \text{ rad/s}$
ans: D

12 $\alpha_{\text{Avg}} = \frac{\Delta\omega}{\Delta t} = \frac{0 - 24\pi}{6} = -4\pi \text{ rad/s}^2$ ans: D

$$13 \quad \alpha_{avg} = \frac{\Delta \omega}{\Delta t} = \frac{0 - 0.75 \times 2\pi}{30} = \frac{-1.5\pi}{30} = \frac{-\pi}{20} \quad \text{ans: D}$$

$$14 \quad \text{Given that the time taken is } t = 1 \text{ min} = 60 \text{ s} \quad \omega_i = 0 \quad \omega_f = 4\pi \text{ rad/s}$$

$$\alpha_{avg} = \frac{\Delta \omega}{\Delta t} = \frac{4\pi}{60} = \frac{\pi}{15} \text{ rad/s}^2 \quad \text{ans: D}$$

$$15 \quad \text{The time taken for angular velocity 18 rad/s to zero is } \omega_f = \omega_i + \alpha t$$

$$0 = 18 - 2t \Rightarrow t = 9 \text{ s} \quad \text{and the time for angular velocity zero to 18 is also 9 s}$$

$$\text{Total time is } t = 9 + 9 = 18 \text{ s} \quad \text{Hence we get by it ans: D}$$

$$16 \quad \alpha = \frac{\omega_f - \omega_i}{t} = \frac{+24 - 36}{6} = -2 \text{ rad/s}^2 \quad \text{Ans: B}$$

$$17 \quad \alpha = \frac{\omega_f - \omega_i}{t} = \frac{-24 + 36}{6} = 2 \text{ rad/s}^2 \quad \text{Ans: A}$$

$$18 \quad \omega_f^2 = \omega_i^2 + 2\alpha\Delta\theta \Rightarrow 0 = (18)^2 + 2(-2)\Delta\theta \Rightarrow \Delta\theta = 81 \quad \text{Ans: A}$$

$$19 \quad \omega_f^2 = 0 + 2(4)(20\pi) \Rightarrow \omega_f = 2\pi \text{ rad/s} \quad \text{ans: B}$$

$$20 \quad \Delta\theta = \omega_i t + \frac{1}{2} \alpha t^2 \Rightarrow t^2 = \frac{2(20\pi - 0)}{4} = 10\pi \quad t = \sqrt{10\pi} = 5.6 \text{ s} \quad \text{Ans: E}$$

$$21 \quad \alpha(t) = (6t^2) \quad \frac{d\omega}{dt} = 6t^2 \Rightarrow \omega = \int 6t^2 dt = \frac{6t^3}{3} = 2t^3 + C$$

$$\Rightarrow \frac{d\theta}{dt} = 2t^3 \Rightarrow \theta = \int 2t^3 dt = \frac{1}{2}t^4 = \left(\frac{1}{2}t^4\right) \text{ rad} \quad \text{ans: C}$$

$$22 \quad \text{from Q21 we found that } \theta = \frac{1}{2}t^4 \Rightarrow 10 \times 2\pi = \frac{1}{2}t^4$$

$$t = \sqrt[4]{125.6} = 3.3$$

ملاحظة استخدمنا العلاقة من الدائرة السابقة فقط لأنه الساري البطل هو نفسه أي أن هذه العلاقة ليست علاقة تامة لايجاد الزمن.

ans: B

$$23 \quad \text{Using Q21 and Q22 } \omega = 2t^3 \Rightarrow \text{when } \theta = 10 \text{ rev } t = 3.3$$

$$\text{So } \omega = 2(3.3)^3 \approx 75 \text{ rad/s} \quad \text{ans: B}$$

$$24 \quad \int d\omega = \int -3t^2 \Rightarrow \omega = -t^3 + C \quad \text{but } \omega(0) = 27 \Rightarrow 27 = 0 + C \Rightarrow C = 27$$

$$\omega = -t^3 + 27 \quad \text{when } \omega = 0 \quad t = 3 \text{ second} \quad \text{Ans: C}$$

25 ans: B



26 Ans A (دائرة جديّة)

27 $\theta = \frac{s}{r} = \frac{3000}{20} = 150 \text{ rad}$ ans: C

28 $v = \omega r = 0.7(10) = 7$ Ans A 29 Ans: D

30 $\Delta\theta = \omega t + \frac{1}{2} \alpha t^2$ But $\Delta\theta = \frac{s}{r} = \frac{4}{0.015} = 266$

$266 = 0 + \frac{1}{2} (2) t^2$

$t = \sqrt{266} \approx 16 \text{ s}$ ans: D

$r = \frac{0.03}{2} = 0.015$

31 Because ω is constant the particle has a_r and doesn't have a_t so $a = a_r = \omega^2 r = (5(2\pi))^2 (0.1) = 10\pi^2 \text{ m/s}^2$ ans: E

32 ans: A دائرة متساوية

33 to find how many revolutions/s the tube made $r = 0.05 \text{ m}$
~~so the tube complete one revolution~~ so the tube complete one revolution when
 and the tube circumference $= 2\pi r = 2\pi(0.05) = 0.1\pi$

الأنبوب يكمل 10 سم كل ثانية ولذا يكتمل 10 سم في 10 سم
 ويكون ذلك بعد الدورات في الثانية
 to make one revolution

$\frac{10 \times 10^{-2}}{0.1\pi} = 0.31847$ revolution the tube made every second

so $\omega = 0.318 \text{ rev/s} = 0.318(2\pi) \text{ rad/s} = 2 \text{ rad/s}$ Ans: A

34 From Question 33 we notice that $\omega = 2 \text{ rad/s}$
 here $a = a_r = \omega^2 r = (2)^2 (0.05) = 0.2 \text{ m/s}^2$

35 $a_t = \alpha r = 5 \times 0.6 = 3$ ans B

36 $v_1 = \omega r_1 = \omega r$ $v_2 = \omega \frac{r}{2} \Rightarrow \frac{v_1}{v_2} = \frac{\omega r}{\omega \frac{r}{2}} = 2$ (ans: B)
 point 1 $\left(\frac{r}{2}\right)$ point 2

37) 360° في ω $\Rightarrow a_{t1} = \alpha r$ $a_{t2} = \alpha \frac{r}{2}$ $\frac{a_{t1}}{a_{t2}} = 2$
ans: B

38) $37, 36^\circ$ في ω $a_{r1} = \omega^2 r$ $a_{r2} = \omega^2 \frac{r}{2}$ $\frac{a_{r1}}{a_{r2}} = 2$
Ans B

39) $\omega_B = 2\omega_A$ $a_{rA} = \omega_A^2 r$ $a_{rB} = 4\omega_A^2 r$ $\frac{a_{rB}}{a_{rA}} = 4$
Ans D

40) Ans: D $\omega_f = \omega_i + \alpha t$ $\Rightarrow \omega_f = \alpha t$ (constant) $\Rightarrow \omega_f$ increases
 $a_t = \alpha r$ (constant) $a_r = \omega^2 r$ (increases) \Rightarrow So \vec{a} increases in magnitude and becomes more radial
 Vector $|\vec{a}| = \sqrt{(a_r)^2 + (a_t)^2}$ (increasing constant)

41) $|\vec{a}| = \sqrt{(a_t)^2 + (a_r)^2}$ $|\vec{a}_f| = \sqrt{(a_t)^2 + (a_r)^2}$ ~~$\sqrt{(4a_t)^2 + (4a_r)^2}$~~

$a_{t \text{ final}} = 4 a_{ti}$
 $\alpha_{f \text{ final}} = 4 \alpha_i$
 $\alpha_f = 4 \alpha_i$

$|\vec{a}_f| = 4 \sqrt{(a_t)^2 + (a_r)^2}$
 $= \sqrt{16(a_t)^2 + 16(a_r)^2}$
 $= \sqrt{(4a_t)^2 + (4a_r)^2}$
 $= \sqrt{(4\alpha_i r)^2 + (4\omega_i^2 r)^2}$

$a_{r \text{ final}} = 4 a_{ri}$
 $\omega_f^2 r = 4 \omega_i^2 r$
 $\omega_f = 2 \omega_i$

answer is E

42 $I_1 = m(1)^2 = m$
 $I_2 = m(2)^2 = 4m$
 $I_3 = m(3)^2 = 9m$
 $I_1 < I_2 < I_3$
Ans: A

43 $I = 2(0)^2 + 2(0)^2 + 2(1)^2 + 2(1)^2 = 4$ $12 \text{ kg} \cdot \text{m}^2$

المسافة r في الاحداثي
السياري

44 $I = 3(0)^2 + 2\left(\frac{L}{2}\right)^2 + m(L)^2$

$= \frac{1^m L^2}{2} + \frac{2ML^2}{2} = \frac{3ML^2}{2}$ Answer is C

منه عارفة ليس بال Test Bank معلومة E لـ متأكدة من الجواب

45 Ans: D thin كلفة
Hoop نصف بفسله معلومة ان

46 Ans: D

47 $I_1 = \frac{2}{5} MR^2$ $I_2 = \frac{2}{3} MR^2$ $I_3 = \frac{MR^2}{2}$ $I_4 = MR^2$

suppose that $X = MR^2$

the $I_4 > I_2 > I_3 > I_1$

\Rightarrow ~~1, 2, 3, 4~~

Ans: C



بصراحة سؤاله مستفز ! لازم نحفظ القوانين

48 $I = \frac{1}{2} MR^2$

~~Mass = \rho V~~

Mass = ρV

$V_A = \pi r^2 L$

$V_B = \pi (2r)^2 2L = 8 V_A$

$I_A = \frac{1}{2} \rho \pi r^2 L R^2$

$I_B = \left(\frac{1}{2} \rho \pi (2r)^2 L (4R^2) \right) = 32 I_A$

$\frac{I_B}{I_A} = 32$

Answer is: E

49 ans A

سؤال بسيط

50

$$V = \frac{m}{\rho} \leftarrow \text{constant}$$

Lava



الحجم يزداد عندما تقل الكثافة ويقل عندما تزداد

I (بقليل الكثافة) عندما يزداد الحجم تزداد أبعاد الشكل بالتالي تزداد

I (بزيادة الكثافة) عندما يقل الحجم تقل أبعاد الشكل بالتالي تقل

50

عنه نفسه مبدأ سؤال 49

لما كانت كثافة الـ lead < من كثافة الـ Wood

$$I_{\text{wood}} > I_{\text{lead}}$$

ملعباً "بخبوطه العتلة"

51

ans B



عنده رجلاً "تركة عجباً"

52

$$I_{\text{new}} = I_{\text{disk}} + Mr^2$$

$$= 0.7 + 0.32 = 1.02 \quad \text{ans: E}$$

53

$$I = I_{\text{cm}} + Mh^2 = \frac{1}{12} ML^2 + M\left(\frac{1}{2}L\right)^2 = \frac{1}{3} ML^2 \quad \text{ans: C}$$

54

$$I = \frac{2}{5} MR^2 + MR^2 = \frac{7}{5} MR^2$$

answer: E

55

$$I = I_{\text{cm}} + Mh^2 = \frac{2}{5} MR^2 + M(4R)^2$$

$$= \frac{2}{5} MR^2 + 16MR^2 = \frac{2}{5} MR^2 + \frac{16 \times 5}{5} MR^2$$

$$= \frac{82}{5} MR^2$$

where $h = 4R$

is the distance between the center of the sphere and the point of suspension

56

ans: D

57

Ans: E

$$\text{Torque} = FR \sin \theta$$

$$\sum \vec{F}_2 = \sum \vec{F}_5 = 0$$

$$r=0 \quad \theta=180$$

$$\left. \begin{array}{l} F_4 \sin \theta \\ \text{التي هي} \\ \sin 90 \end{array} \right\}$$

$$\sum \vec{F}_1 = \sum \vec{F}_3$$

58: $\tau_1 = F_1 \times r_1 = F_1 r_1 \sin \theta_1 = 5(4)(\sin 150) = 10 \text{ N.m}$

$\tau_2 = F_2 \times r_2 = F_2 r_2 \sin \theta_2 = 5(2)(\sin 150) = 5 \text{ N.m}$

$\tau_{\text{total}} = \tau_1 + \tau_2 = 10 + 5 = 15$

Ans: D

59 ans: D 60 ans: A

61 $\tau = r \times F = I \alpha$

$\alpha = \frac{r F \sin \theta}{I}$

$I_{\text{Disk}} = \frac{1}{2} M r^2$, $I_{\text{Hoop}} = M r^2$, $I_{\text{sphere}} = \frac{2}{5} M r^2$

$\alpha_{\text{Hoop}} < \alpha_{\text{disk}} < \alpha_{\frac{2}{5} M r^2}$ Ans: D

62 Ans: B 63 $\alpha = \frac{(0.1)(1)}{0.020} = 5$ Ans: B

64 $\alpha = \frac{(5)(0.4)}{2} = 1$ ans: C

65 ans: A Because the force is applied along the rotation axis
 $\tau = 0$ so $\alpha = 0$

66 $\tau = F \times r = I \alpha$

$F r \sin \theta = I \alpha$

$\frac{(8)(0.25)(1)}{5} = \alpha$

$\Rightarrow \alpha = 0.4 \text{ rad/s}^2$

then:

$\omega_f^2 = \omega_i^2 + 2 \alpha \Delta \theta$

$\omega_f^2 = 0 + 2(0.4)\pi$

$\omega_f = \sqrt{0.8\pi} \approx 1.6$

$\Delta \theta = \text{half revolution} = \frac{1}{2} \cdot 2\pi = \pi$

Ans: D

67 $I_{\text{Hoop}} = M r^2 = 1(2)^2 = 4 \text{ kg.m}^2$

$\tau = \alpha I = (7)(4) = 28 \text{ N.m}$ Ans: C

page 7

68

$$W_f^2 = W_i^2 + 2\alpha \Delta\theta \quad \leftarrow \text{torque constant and } I \text{ constant so } \alpha \text{ is constant}$$

$$(6)^2 = (5)^2 + 2\alpha(10\pi)$$

$$\alpha = 0.175 \Rightarrow \tau = I\alpha = 12(0.175) = 2.1$$

Ans: D

69

$$I = 0.5 \text{ kg} \cdot \text{m}^2$$

القوة السحب

We know that $\tau = I\alpha = Fx\vec{r}$

$$\tau = I\alpha = \text{Tension } r(1)$$

$$\text{so Tension} = \frac{I\alpha}{r}$$

$$\text{And } F_{\text{net}} = W - T$$

$$ma = mg - \left(\frac{I\alpha}{r}\right) \quad \dots (1)$$

$$\text{But we know that } a = \alpha r \Rightarrow \alpha = \frac{a}{r} \quad \dots (2)$$

By substituting (2) in (1)

$$ma = mg - \frac{Ia}{r^2} \Rightarrow \text{now we must solve for } a \text{ so}$$

$$ma + \frac{Ia}{r^2} = mg$$

$$a = \frac{(mg)}{\left(m + \frac{I}{r^2}\right)} \Rightarrow a = \frac{16 \text{ g}}{16 + \frac{0.5}{(0.2)^2}} = 0.56 \text{ g}$$

Ans is B

70

$$R = 8.0 \text{ cm} = 8 \times 10^{-2} \text{ m} \quad \{ I = 0.12 \text{ kg} \cdot \text{m}^2 \quad \{ m = 10 \text{ kg} \quad \{ T = 9 \text{ N} \cdot \text{m}$$

$$\alpha = \frac{a}{R} \quad \dots (1)$$

$$\tau = I\alpha = \text{Tension } R(1)$$

$$\tau = \text{Tension } R$$

$$F - mg = ma \Rightarrow \tau_{\text{net}} = I\alpha$$

$$F = m(a + g) \quad \tau_1 - FR \sin \theta = I\alpha$$

$$\tau_1 - m(a + g)R = I\left(\frac{a}{R}\right)$$

$$a = \frac{(\tau_1 - mRg)}{\left(mR + \frac{I}{R}\right)} = \frac{9 - 10(8 \times 10^{-2})(9.8)}{10(8 \times 10^{-2}) + \frac{0.12}{(8 \times 10^{-2})}} = 0.5 \text{ m/s}^2$$

ans: A

71

The Ans is B. 9.8 N

~~The Ans is B. 9.8 N~~

The suspension holding the cylinder pulls up on the cylinder with a force of $T = m_g + M_{\text{block}}(g - a_{\text{block}})$ where a_{block} - the acceleration of 2 kg mass. At the same time that is the tangential acceleration of the disk. Let's find it.

$$\tau = I\alpha = F \times R = M_{\text{block}}(g - a_{\text{block}})R$$

$$\left(\frac{a}{R}\right) \frac{MR^2}{2} = M_{\text{block}}(g - a_{\text{block}})R$$

$$\frac{Ma_{\text{disk}}}{2} = M_{\text{block}}(g - a) \Rightarrow 2M_{\text{block}}(g - a) = m_{\text{disk}}a$$

$$a = \frac{2M_{\text{block}}g}{m_{\text{disk}} + 2M_{\text{block}}} = \frac{2(9.8)}{0.7 + 2} = 8.34 \text{ m/s}^2$$

$$2M_{\text{block}}g - 2M_{\text{block}}a = m_{\text{disk}}a \Rightarrow 2M_{\text{block}}g = a(m_{\text{disk}} + 2M_{\text{block}})$$

$$a = \frac{2M_{\text{block}}g}{m_{\text{disk}} + 2M_{\text{block}}} = 8.34 \text{ m/s}^2 \Rightarrow T = m_{\text{disk}}g + M_{\text{block}}(g - a) = (0.7)(9.8) + 2(9.8 - 8.34) = 9.8 \text{ N}$$

ans : B

$$\cancel{T = FR = TR_2 = I\alpha}$$

$$\cancel{T = FR_1 = I\alpha}$$

Then we use $T = ma$:

To find a : $a = \dots$

Continued

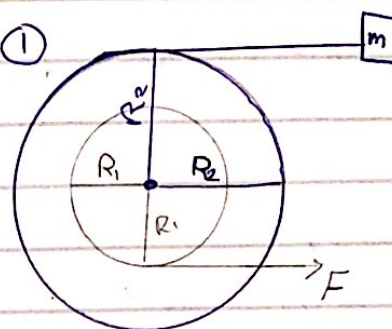
Page 9

72

$$\tau_{\text{net}} = \tau_{\text{by } F} - \tau_{\text{by } T} = I\alpha \quad \text{--- ①}$$

$$\tau_{\text{net}} = R_1 F_1 - T R_2 = I\alpha$$

The point here is that $\alpha = \frac{a}{R_2}$



So we can now find T from ①

$$T = -I \frac{a}{R_2^2} + \frac{F R_1 R_2}{R_2^2} = \frac{F R_1 R_2 - I a}{R_2^2}$$

Then we use T to find a : since $T = ma$

$$a = \frac{T}{m} = \frac{F R_1 R_2 - I a}{m R_2^2} \Rightarrow a m R_2^2 = F R_1 R_2 - I a$$

$$a(m R_2^2 + I) = F R_1 R_2$$

$$a = \frac{F R_1 R_2}{m R_2^2 + I}$$

ans: C

73

From problem 72 $T = am = \frac{m F R_1 R_2}{m R_2^2 + I}$

The ~~answer~~ answer is C

74

ans: A

75

$$\text{By } v = \omega r \Rightarrow \omega = \frac{v}{r} \Rightarrow \omega = \frac{2}{3 \times 10^{-2}} = 66.7 \text{ rad/s}$$

$$\text{Thus by KE (rotational)} = \frac{1}{2} I \omega^2$$

$$= \frac{1}{2} (45 \times 10^{-3}) (66.7)^2 = 10 \text{ J}$$

ans: D

76

ans: C

77

$$\text{Work done} = F \times \text{distance}$$

$$\text{distance} = \pi R = 3.14 (0.25) = 0.7854 \text{ m}$$

$$\text{Work done} = (2) (0.7854) = 1.6 \text{ J}$$

Ans: A

$$W = \tau \theta$$

$$= F R \pi = 1.6 \text{ J}$$

Page 10

constant $\omega \Rightarrow \alpha = 0$

78) $Work = \tau \cdot \theta$ ~~$\tau = 0.80$~~ $\theta = \omega t = 20 \times 60 = 1200 \text{ rad}$
 $= (0.80)(1200)$
 $= 960 \text{ J}$ ans: C

~~79~~

79) $\omega_f = \omega_i + \alpha t = 0 + 2(5) = 10 \text{ rad/s}$
 Work done by $\tau_{net} = \Delta K = \frac{1}{2} I (\omega_f^2 - \omega_i^2)$
 $= \frac{1}{2} (6) (10)^2 = 300 \text{ J}$
 ans: D

80) $\tau_{net} = I \alpha$ \rightarrow constant $\omega_f = \omega_i + \alpha t$
 \downarrow constant \downarrow constant $\omega(5) = \alpha 5$ $\omega(10) = 10\alpha$
 Work done by $\tau_{net} = \Delta K = \frac{1}{2} I (\omega_f^2 - \omega_i^2)$
 Work in first 5s = $\frac{1}{2} I 25\alpha$ --- (1) $\frac{(2)}{(1)} = 4$
 Work in second 5s = $\frac{1}{2} I 100\alpha$ --- (2)
 ans: D

81) ans: A



لا تنسوا من صالح دعائكم بظهر الغيب

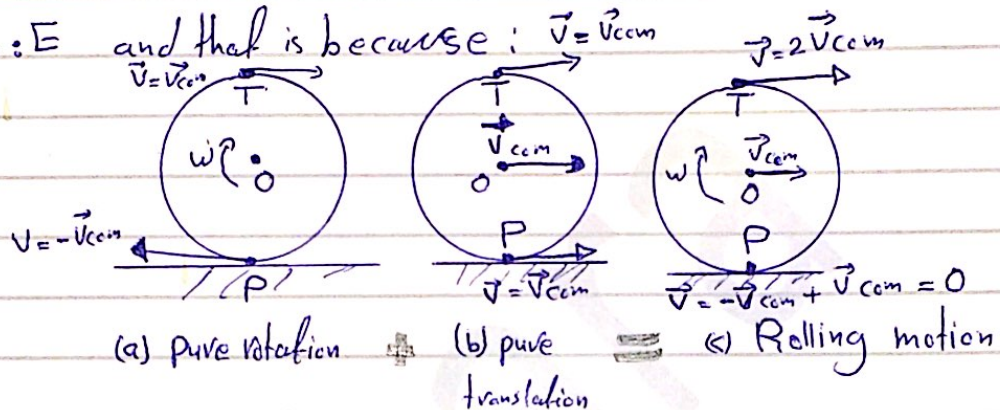
Chapter 11:

Rolling, Torque, and Angular Momentum

Test bank answers

1

ans: E and that is because: $\vec{v} = \vec{v}_{cm}$



راجعوا صفحة
276
بالكتاب

2

$$\Delta\theta = \omega t + \frac{1}{2} \alpha t^2$$

$$= 0 + \frac{1}{2} (6) (3)^2 = 27 \text{ rad}$$

ans: C

but $s = \theta R = 27 (0.5) = 13.5 \text{ m}$

3 $V = \omega R$ and if V is the same in the two cases and $R_2 = 2R_1$

then $\omega_1 = \frac{V}{R_1}$ $\omega_2 = \frac{V}{R_2} = \frac{V}{2R_1} = \frac{1}{2} \omega_1$ ans: C

A - 7

مطلوب

دوائر الاستكمال غير مطلوبة
سأورد بالفاينل

8

$$K_{rot} = \frac{1}{2} I_{cm} \omega^2$$

$$K_{translation} = \frac{1}{2} M V_{cm}^2$$

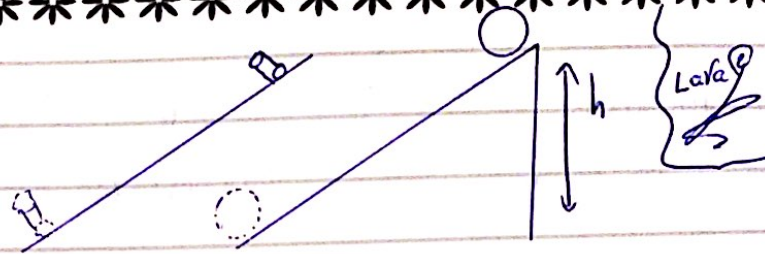
$$= \frac{1}{2} M R^2 \omega^2$$

$$= \frac{1}{2} M R^2 \left(\frac{V}{R} \right)^2 = \frac{1}{2} M V_{cm}^2$$

$$\text{so } \frac{K_{rot}}{K_{trans}} = 1$$

ans: A

9) ans: E



$$I_{\text{sphere}} = \frac{2}{5} MR^2$$

$$I_{\text{cylinder}} = \frac{1}{2} MR^2$$

* so the first option A is wrong because $I_{\text{cylinder}} > I_{\text{sphere}}$

$$K_{\text{rotational sphere}} = \frac{1}{2} I_{\text{sphere}} \omega^2 = \frac{1}{2} \left(\frac{2}{5} MR^2 \right) \frac{V^2}{R^2} = \frac{1}{5} MV^2 \quad (1)$$

$$K_{\text{rotational cylinder}} = \frac{1}{2} I_{\text{cylinder}} \omega^2 = \frac{1}{2} \left(\frac{1}{2} MR^2 \right) \frac{V^2}{R^2} = \frac{1}{4} MV^2 \quad (2)$$

here we will use the conservation of Energy

First for the sphere: $(K+U)_i = (K+U)_f$

$$Mgh = K_{\text{rot}} + K_{\text{trans}}$$

$$Mgh = \frac{1}{2} I \omega^2 + \frac{1}{2} MV^2$$

$$Mgh = \frac{1}{5} MV^2 + \frac{1}{2} MV^2 \Rightarrow Mgh = \frac{7}{10} MV^2_{\text{sphere}}$$

$$V_{\text{sphere}} = \sqrt{\frac{10}{7} gh} \Rightarrow \text{(it reaches first)}$$

$$\text{Second for the cylinder } Mgh = \frac{1}{4} MV^2 + \frac{1}{2} MV^2 = \frac{3}{4} MV^2_{\text{cylinder}}$$

$$V_{\text{cylinder}} = \sqrt{\frac{4}{3} gh} \Rightarrow V_{\text{sphere}} > V_{\text{cylinder}} \text{ (sphere reaches first)}$$

\Rightarrow The option B is wrong because the sphere reaches first

The option C is wrong because $K_{\text{rot sphere}} < K_{\text{rot cylinder}}$

The option D is wrong because They didn't reach the bottom together

So option E is correct

10) $I_{\text{cylinder}} = \frac{1}{2} MR^2$

$$I_{\text{sphere}} = \frac{2}{5} MR^2$$

$$I_{\text{ring}} = MR^2$$

for hoop:

$$\frac{1}{2} MV^2 + \frac{1}{2} MV^2 = Mgh$$

$$MV^2 = Mgh$$

for cylinder:

$$\frac{3}{4} MV^2 = Mgh$$

$$h = \frac{3}{4} \frac{V^2}{g}$$

for sphere:

$$\frac{7}{10} MV^2 = Mgh$$

$$h = \frac{7}{10} \frac{V^2}{g}$$

for disk:

$$\frac{8}{10} MV^2 = Mgh$$

$$h = \frac{8}{10} \frac{V^2}{g}$$

$$h_{\text{hoop}} > h_{\text{cylinder}} > h_{\text{sphere}}$$

So correct answer is

$$h_{\text{hoop}} > h_{\text{cylinder}} > h_{\text{sphere}}$$

11) Ans: B $k_{rot} = \frac{1}{2} I \omega^2 = \frac{1}{2} M R^2 \left(\frac{V^2}{R^2} \right) = \frac{1}{2} M V^2 = k_{trans}$

12) غير مطلوب 13) D 14) Ans: D

15) Ans: E السرعة لديه نقطة على العتلة وانما ستكون $V = \sqrt{\frac{4}{3} g h}$ بالتالي يصل الى $\frac{4}{3} g h$

16) Ans: A

As the bodies roll from rest down the inclined plane, the initially gravitational potential energy is converted to translational and rotational kinetic energies. Since the ball is bigger than the ball bearings, its moment of inertia is larger, so that the amount of gravitational potential energy converted to rotational kinetic energy $\frac{1}{2} I \omega^2$ is also larger, leaving a smaller amount for the translational kinetic energy $\frac{1}{2} m v^2$, so that its translational speed at the bottom is smaller.

For the block mounted on roller bearings, the ball bearings are smaller than the ball, so they also have smaller moments of inertia, converting less amount of the initial gravitational potential energy to rotational kinetic energy of the ball bearings, leaving behind a larger amount for the translational kinetic energy of the block, making its translational speed at the bottom higher.

17) غير مطلوب

18) ans: E

19) Ans: D

kg.m²/s

20) Ans: A

21) Ans: D

22) $L = I \omega = m R^2 \omega = 2 (0.5)^2 (12) = 6 \text{ kg.m}^2/\text{s}$ نفس السؤال السابق مختلفه

23) Ans: C

24) $L = r \times p = (12)(6)(4) \sin 30 = 144$ ans: C

25) $L_{ball 1} = (1)(6)(2) \sin 90 = 12$ $L_{ball 2} = (2)(3)(3) \sin 90 = 18$

$L_{total} = 12 + 18 = 30 \text{ kg.m}^2/\text{s}$ ans: D

26)

$v(2) = at = 4(2)i - 3(2)j = 8i - 6j \text{ m/s}$

$r(2) = v_0 t + \frac{1}{2} a t^2 + r_0 = 0 + \frac{1}{2} (4i - 3j) (2)^2 + 3i$
 $= 8i - 6j + 3i = 11i - 6j$

$L = r \times p = (11i - 6j) \times (16i - 12j)$
 $= -(36 \text{ kg.m}^2/\text{s}) \hat{k}$

Ans: B

27

~~$$L = I\omega = \frac{1}{2}MR^2\omega = \frac{1}{2}(18)(0.3)^2(3.3) = 4.7 \times 10^{-3}$$~~

$$L = I\omega = mR^2\omega = \left(\frac{18}{1000}\right)(0.3)^2(3.3) = 4.7 \times 10^{-3}$$

Ans: B

~~$$L = I\omega = mR^2\omega = (2)(0.5)^2(12) = 6 \text{ kg}\cdot\text{m}^2/\text{s}$$~~

28 + 29 + 30 :

يوجد خطأ في إرقام السؤال يجب أن نحوله 0.75 إلى 0.61

الهم فقرة البطل في التالي L لها مركبتين :

① The z component ② the xy plane component

بداية " دائرة 29 " قلبه الـ 2 component والى التالي

$$L_1 = I\omega = mR^2\omega = 2(0.5)^2(12) = 6 \text{ kg}\cdot\text{m}^2/\text{s} \quad \text{Ans: A}$$

و دائرة 30 " قلبه الـ The component in the xy plane

$$L_2 = I\omega = mR^2\omega = 2(0.61)^2(12) = 9 \quad \text{ans: C}$$

$$L_{\text{net}} = \sqrt{L_1^2 + L_2^2} \quad \text{دائرة 28 } L \text{ الـ}$$

$$= \sqrt{(6)^2 + (9)^2} \approx 11 \text{ kg}\cdot\text{m}^2/\text{s}$$

منه عارفة الارقام ما يتربط الا هيليه مستحيل ترتبط مع وجود 0.75
عصبة الهم الفكرة

31

using parallel axis theorem

$$I = I_{\text{com}} + mh^2$$

$$\text{so } L = (I_{\text{com}} + mh^2)\omega$$

Ans: B

32

~~$$L = m_1 v R$$~~

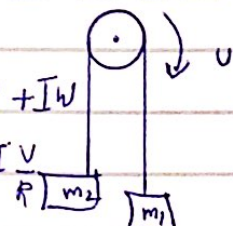
$$L_1 = m_1 v R$$

$$L_2 = m_2 v R \Rightarrow L_{\text{net}} = (m_1 + m_2) v R + I\omega$$

$$L_{\text{for the pulley}} = I\omega = \frac{1}{2} I \frac{v}{R} = (m_1 + m_2) v R + I \frac{v}{R}$$

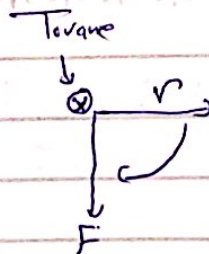
Ans: B

$$L_{\text{net}} = (m_1 + m_2) v R + I v / R$$



33

ans: B



34

Ans: C

35

Ans: A

36

$$F_{\text{centrifugal}} = m \omega^2 R = (2)(12)^2(0.5) = 144$$

The distance from the origin = 0.75

$$\tau = r F = 0.75 (144) = 108$$

Ans: E

$$\tau = \mathbf{r} \times \mathbf{F}$$

Force perpendicular component: since the 2kg mass is located 3m from the origin on the positive x-axis, only the y-component of the force cause torque. To determine the y-component of the force, we use the y-component of the acceleration $a = 4\hat{i} - 3\hat{j}$

$(-3\hat{j}) \text{ m/s}^2$ is the y-component

$$\text{Force} = (\text{mass})(\text{acceleration}) = -6\text{N}$$

$$\tau = \mathbf{r} \times \mathbf{F} = rF \sin 90 = (3)(-6) = -18 \text{ N.m}$$

Ans: B

38

ans: A

39

Ans: C

40

ans: A

41

$$I_{\text{new}} = I_{\text{old}}$$

$$I_F = \frac{I_0}{4}$$

ans: D

42

Ans: E

43

ans: B

44

ans: C

Internal forces are unable to change angular Momentum
The Answer is L

45

Ans: B

راجعوا سؤال 4.5

بالنسبة (acceleration)

46 Ans: C

47 $L_{\text{Before}} = L_{\text{After}}$

$$I\omega + 4I\omega = 3I\omega_f$$

$$\omega_f = \frac{5I\omega}{3I} = \frac{5}{3}\omega$$

Ans: A

Lara @

48 $L_{\text{Before}} = L_{\text{After}} \Rightarrow I\omega_0 = \omega_f(2I+I)$

$$\omega_f = \frac{\omega_0 I}{3I} = \omega_0/3$$

Ans: C

49 Ans: D

50 From the conservation law,

The total angular Momentum of the child before = $L_{\text{child + merry-go-round}}$
After

$$MRV = MRV' + I\omega$$

$$MRV = MR(\omega R) + I\omega \Rightarrow MRV = \omega(MR^2 + I)$$

$$\text{So } \omega = \frac{MRV}{I + MR^2}$$

Ans: E

* 51 $L_{\text{Before}} = L_{\text{After}}$

$$600(0.8) = 600\omega_f + 20(3)^2\omega_f$$

$$600(0.8) = (600 + 180)\omega_f$$

$$\omega_f \approx 0.62 \text{ Ans: A}$$

52 Ans: A

53 Ans: C

54 Ans: A

The End 