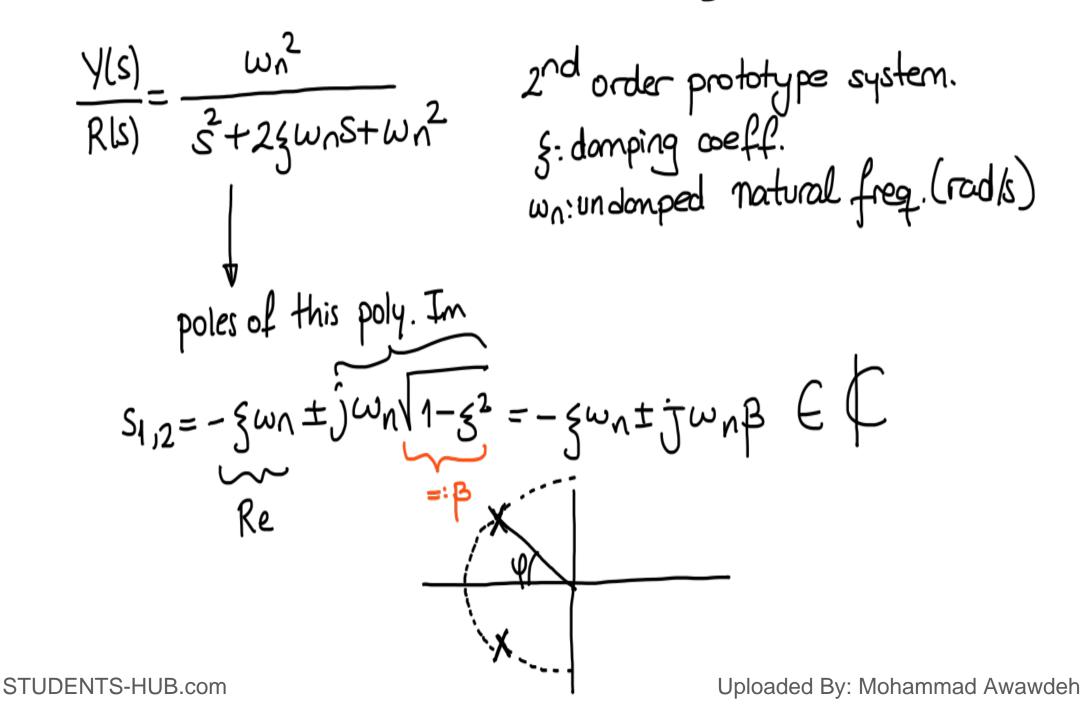
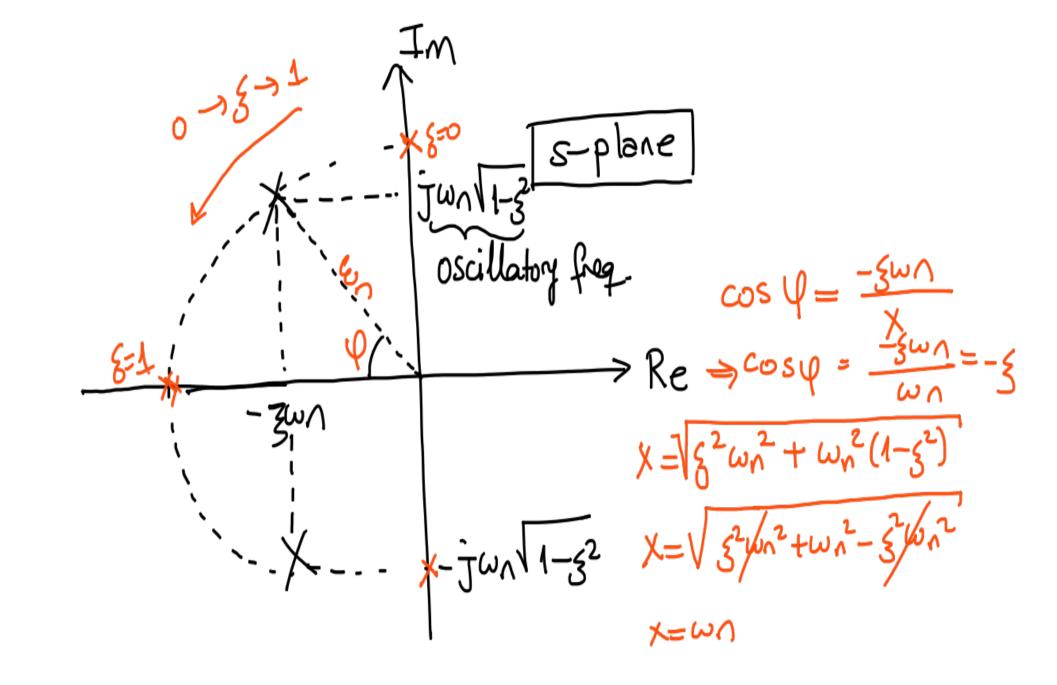
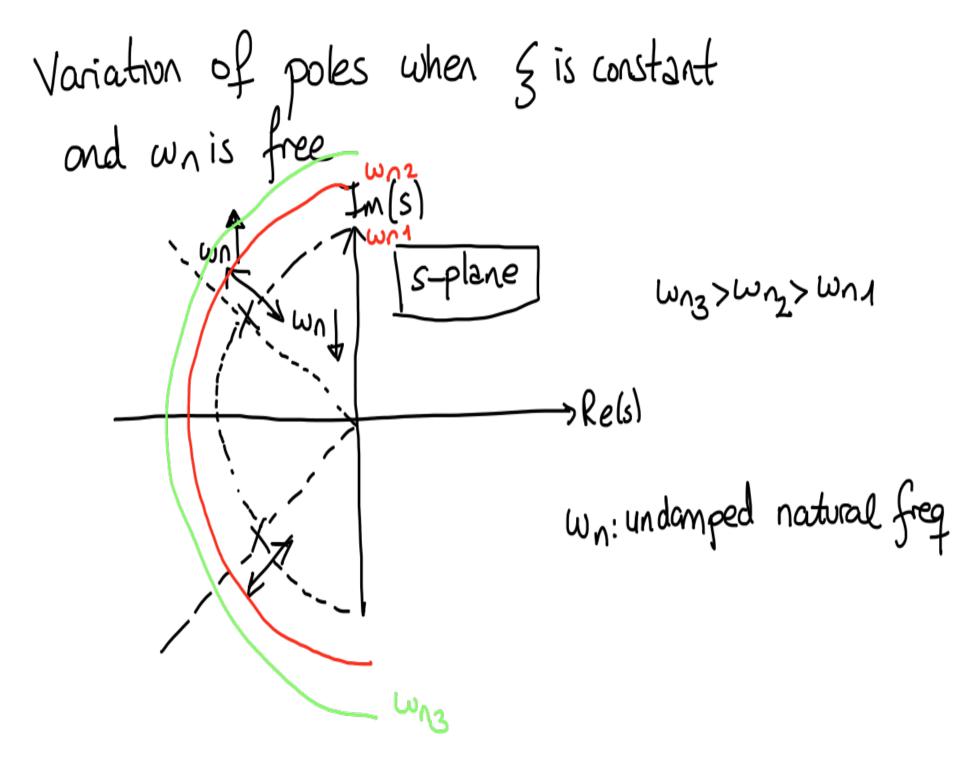
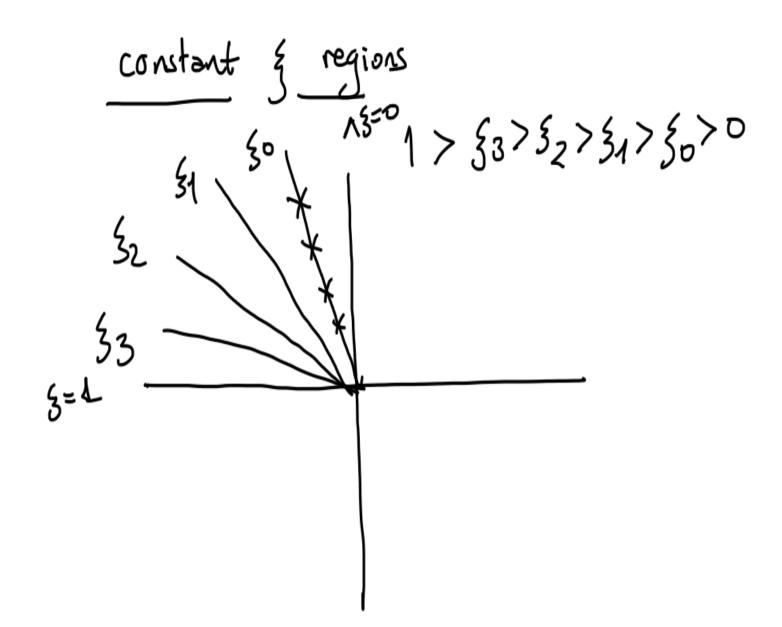
Underdamped Case (O<<<1)





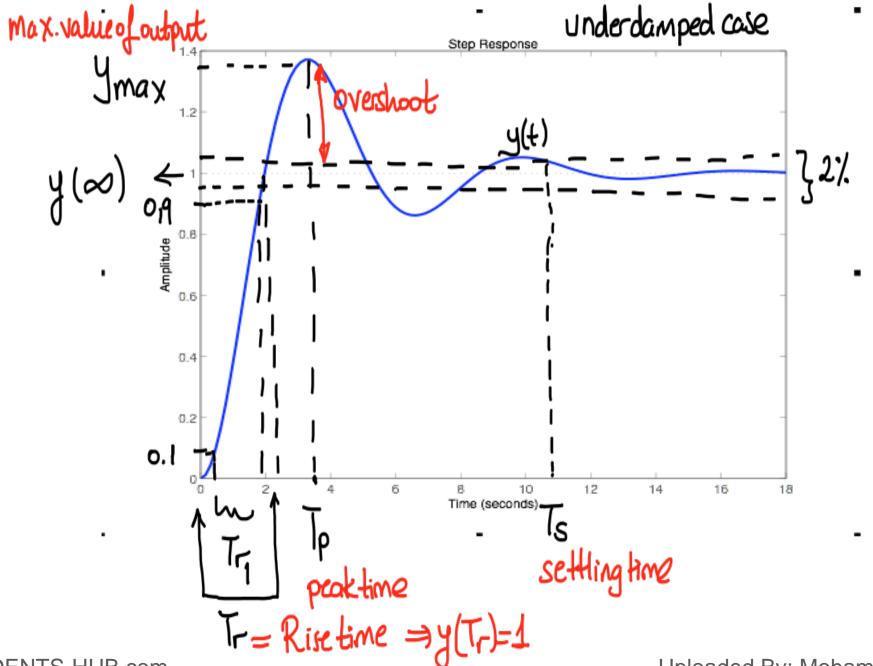




Definitions

$$g: d comping ratio$$

 $w_n: undomped natural freq. [rad lsec]$
 $wd = wn \sqrt{1-s^2} = d comped freq.$



$$T_{r_{4}} = (10 \text{ to } 90\% \text{ rise time}) = \text{Time required for the response} \\ \text{to rise to } 90\% \text{ of its steady-state value} (in this case=1) \\ \text{from 10\% of its steady-state value} \\ T_{r_{4}} \cong \frac{2.165 \pm 0.6}{\omega_{0}} \quad (0,3 \le 3 \le 0,8) \\ T_{r_{4}}(5,\omega_{0}) \end{cases}$$

$$T_{p} : \text{peak-time} \Rightarrow y(T_{p}) = Y_{mox}$$

$$y(t) = \frac{\omega_{n}}{B} e^{\frac{\omega_{n}t}{\sin(\omega_{n}Bt)}} = 0$$

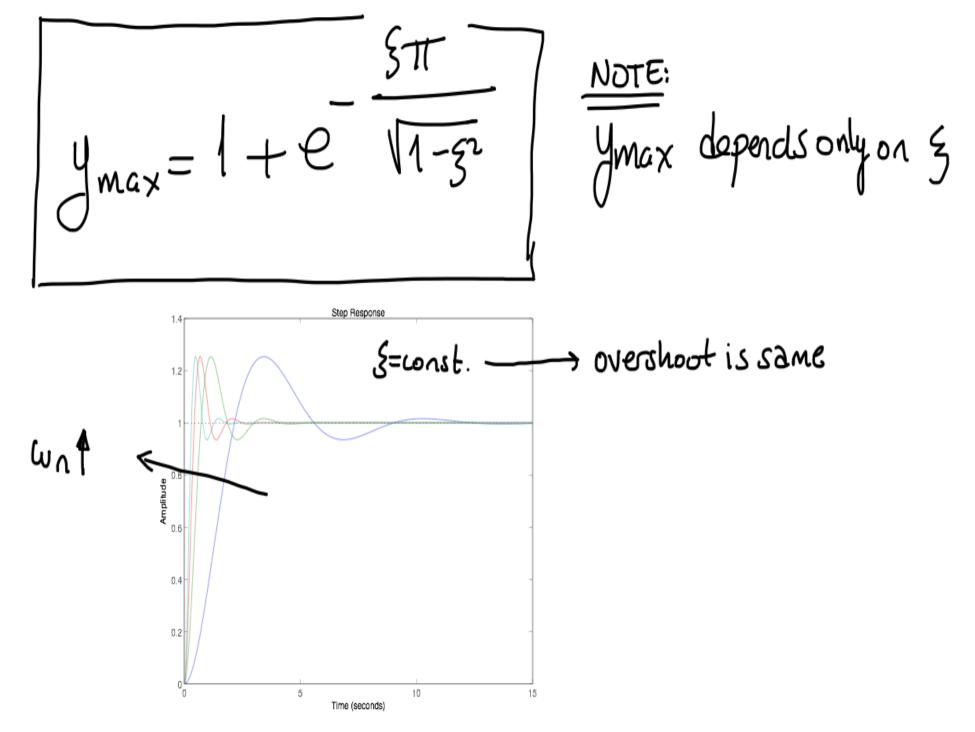
$$\Rightarrow t = T_{p} = \frac{T}{\omega_{n}B} = \frac{T}{\omega_{n}\sqrt{1-s^{2}}}$$

$$T_{p} = \frac{T}{\omega_{n}\sqrt{1-s^{2}}}$$

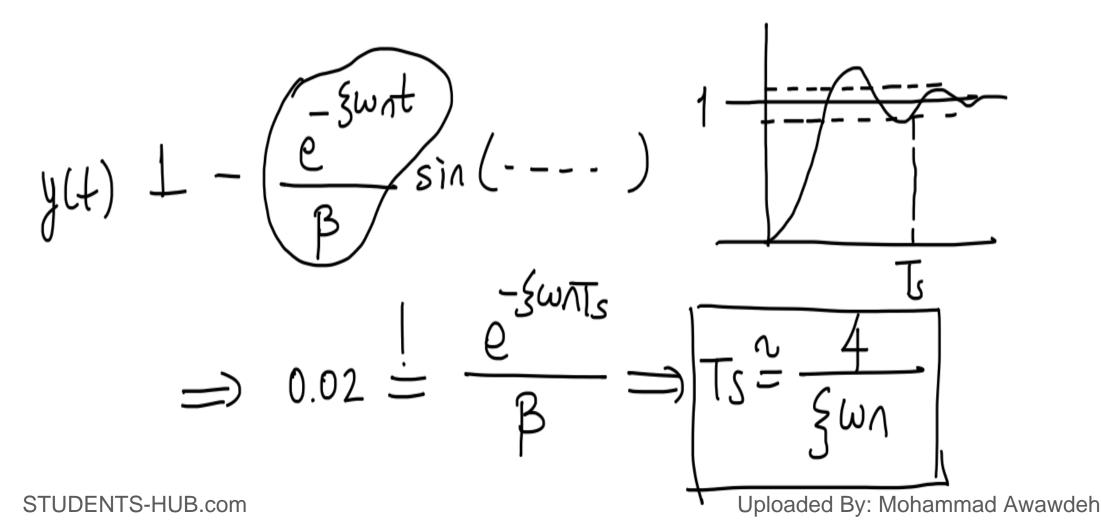
$$f \text{ vories in a small}$$

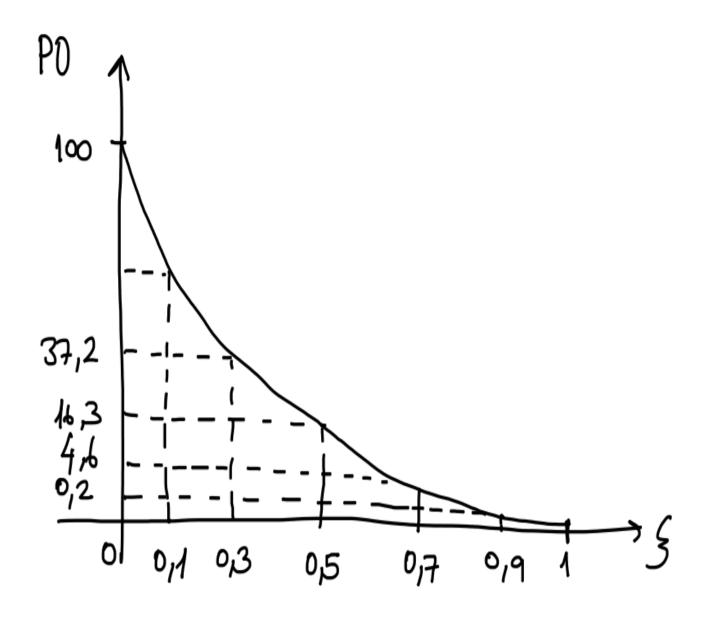
$$f \text{ interval} :: T_{p} :s \text{ makly controlled by } w_{n}$$

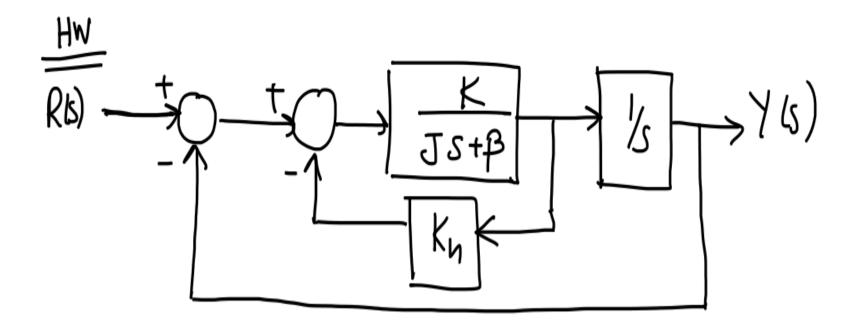
$$as w_{n}T_{u} = \frac{T_{u}}{T_{u}} = \frac{T_{u}}{T_{u}}$$



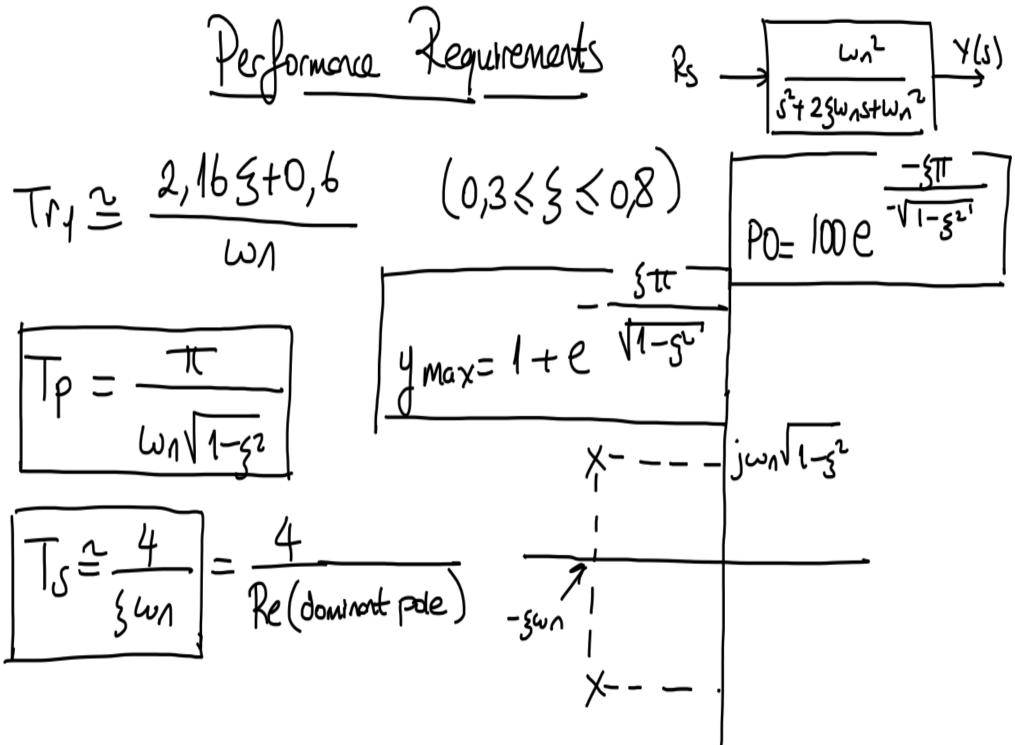
Ts: settling time: time after which response remains within 2% of its sleady-state value [sec]



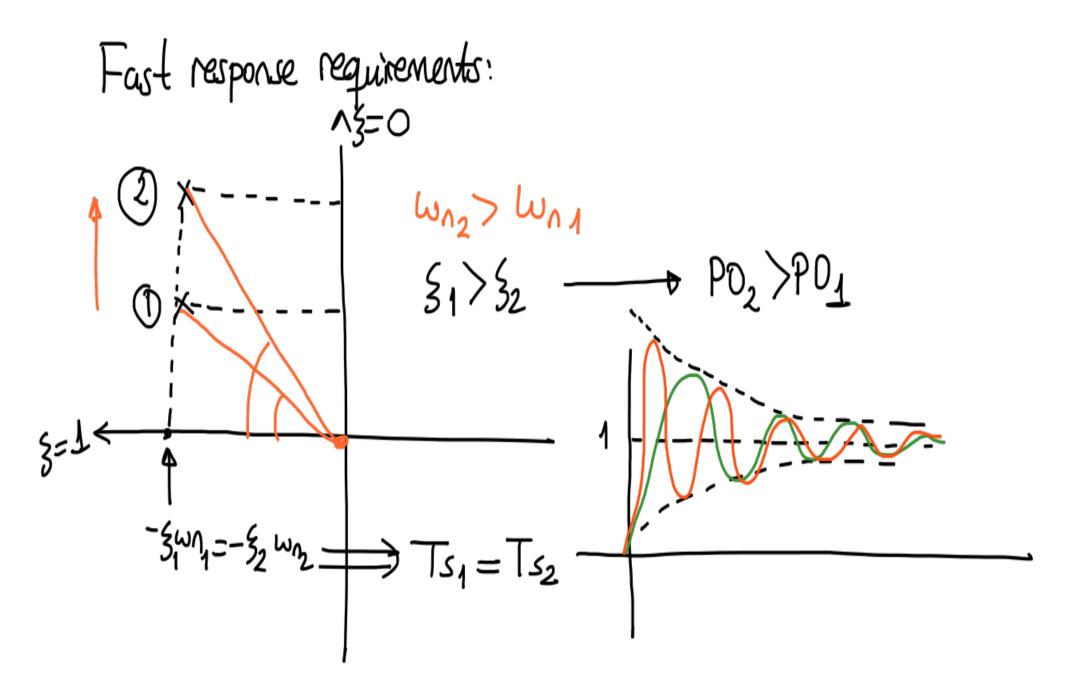




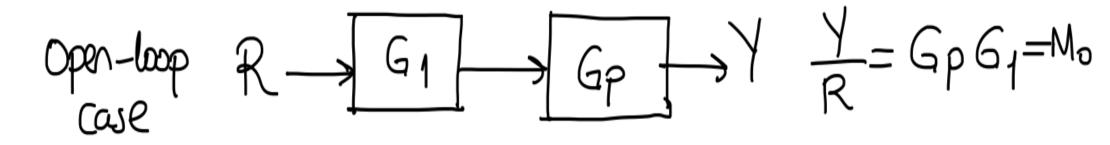
Determine K, Kh So that maximum overshoot for the unit step response is 0,2 and peak time is lsec. with the values of K, Kh, obtain rise-time and Ts assuming that J=1kgm², B=1Nmrad/sec UDENTS-HUB.com Uploaded By: Mohammad Awawdeh

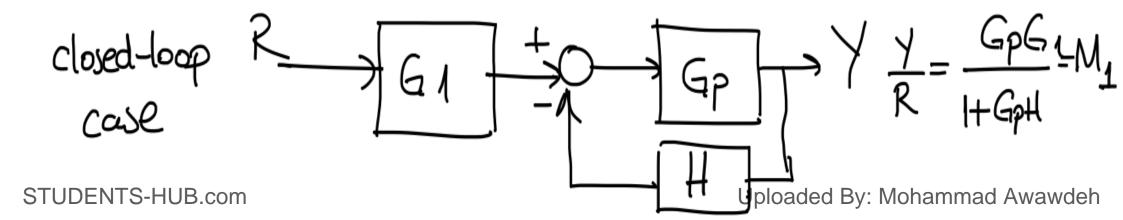


$$\frac{\text{Requirements}}{1. \text{ Fast response}: \text{ small Tr, Tp}} = \frac{1}{2} + \frac{1$$



Effects of Feedback





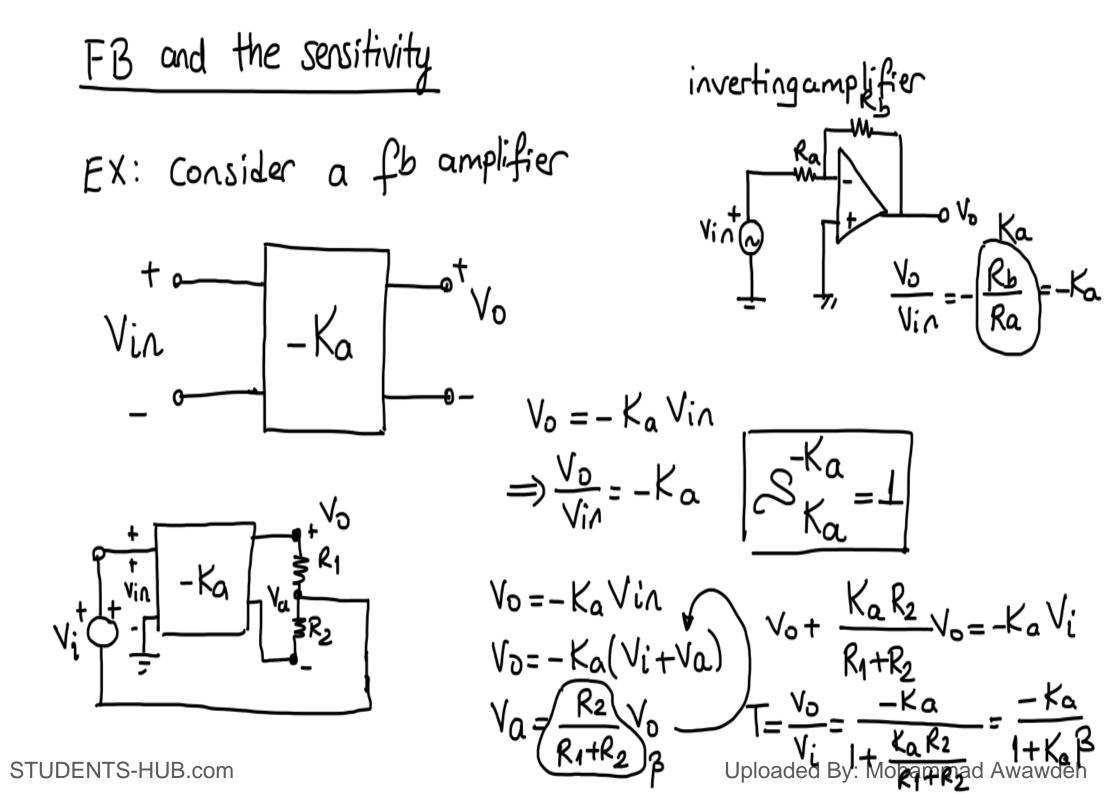
Let's define sensitivity :/ change in M R Y. change in X sensitivity M! gain of the system X: porameter

$$\frac{\text{Open-loop case}}{M_0:GpG_1}: \int_{Gp}^{M_0} = \frac{Gp}{M_0} \cdot \frac{dN_0}{dGp}$$

$$\int_{Gp}^{M_0} = \frac{Gp}{GpG_1} \cdot G_1 = 1$$

$$\frac{\text{Closed-loop case}!}{M_1 = \frac{GpG_1}{1+GpH}}: \int_{Gp}^{M_1} \frac{Gp(1+GpH)}{GpG_1} \cdot \frac{G_1(1+GpH)-HGpG_1}{(1+GpH)^2}$$

$$\int_{Gp}^{M_1} = \frac{1}{1+GpH} \int_{Gp}^{Generally!} \frac{Generally!}{GpH > 1} = S_{Gp}^{M_1} << S_{Gp}^{M_0}$$



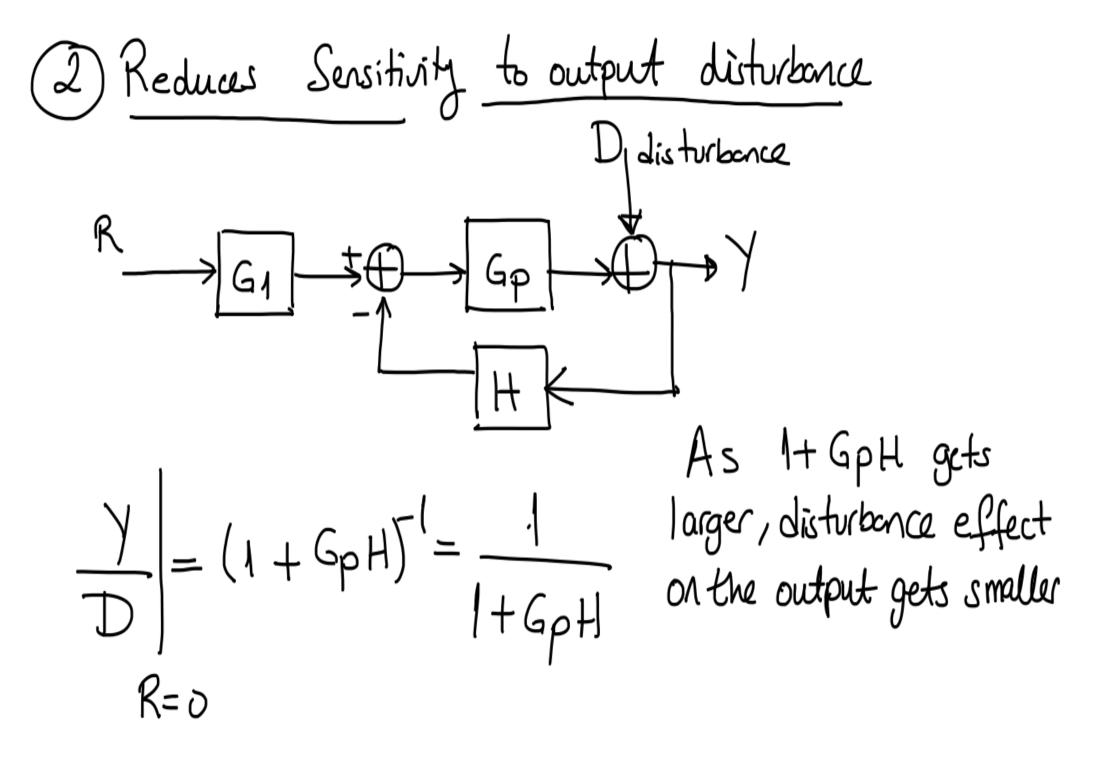
$$S_{Ka}^{T} = \frac{Ka}{T} \frac{dT}{dKa} = \frac{Ka}{-ka} \cdot \frac{-1 - \beta Ka + \beta Ka}{(1 + \beta Ka)^{2}} = \frac{1}{1 + \beta Ka}$$

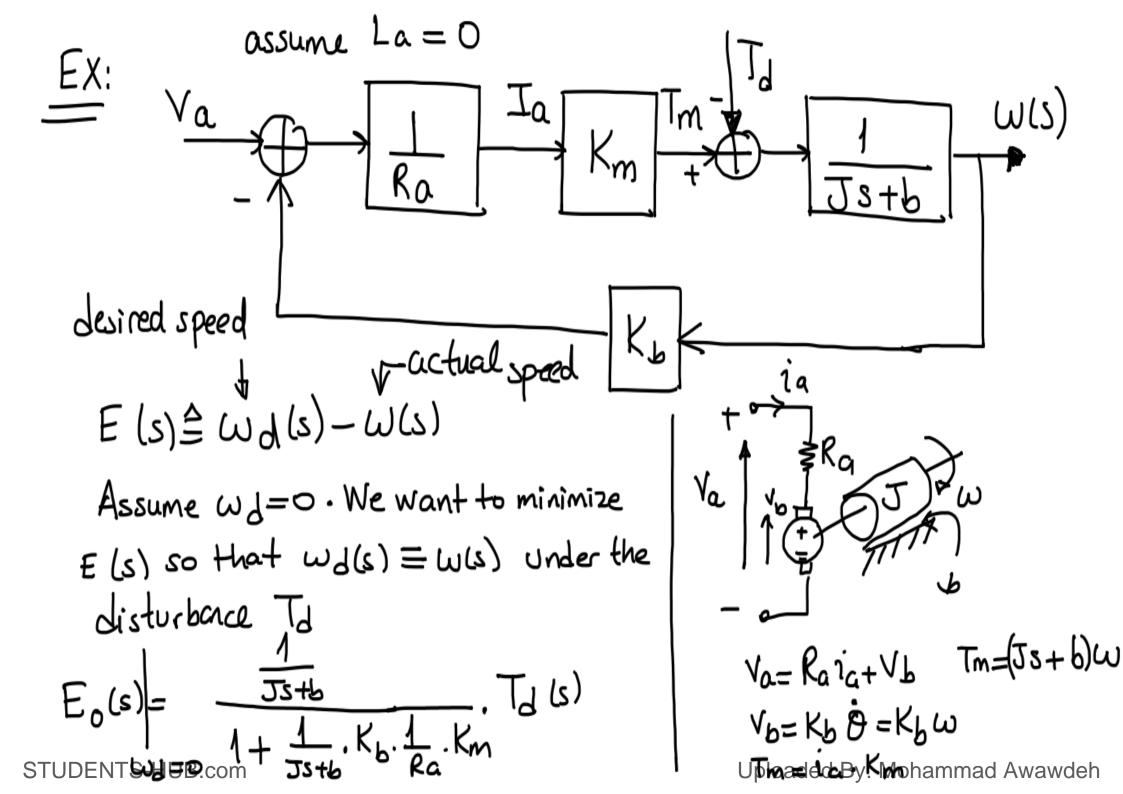
$$T = -\frac{Ka}{1 + \beta Ka} \qquad |1 + \beta Ka| \gg 1$$

$$\implies S_{Ka}^{-Ka} \gg S_{Ka}^{T}$$

$$\implies S_{Ka}^{-Ka} \gg S_{Ka}^{T}$$

$$if Ka \text{ is large } \Rightarrow \text{ Sensificity is feduced.}$$



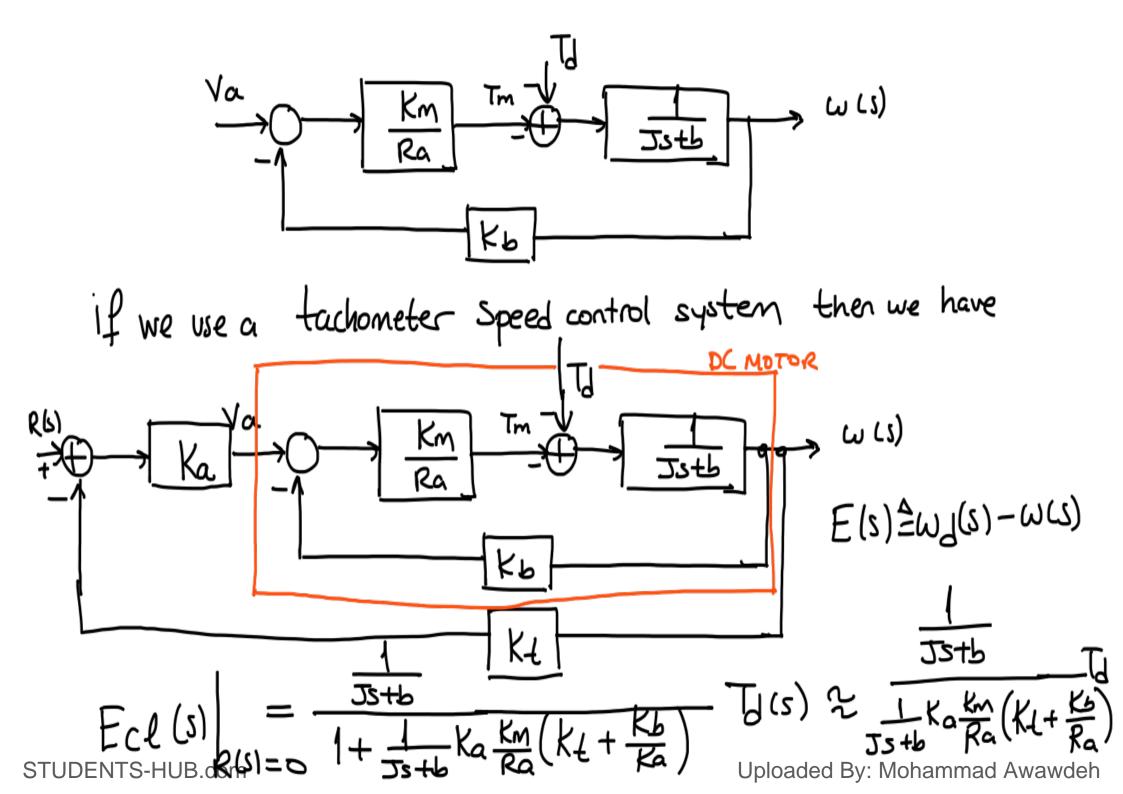


$$E_{o}(s) = \frac{1}{Js+b+\frac{K_{b}K_{m}}{Ra}} \cdot T_{J}(s) = \frac{1}{\sqrt{t}} \cdot \frac{T_{J}(s)}{t}$$

$$\omega_{J}=0 \quad \text{Arrow} \quad R_{a}$$
assume our disturbance effect is constant $\left(T_{J}(s)=\frac{D}{s}\right)$

$$\text{Lim } e(t) = \text{Lim } s E(s) = \frac{D}{b+\frac{K_{b}K_{m}}{Ra}} = e_{o}(\omega)$$

$$t \to \omega \quad s \to 0 \quad b+\frac{K_{b}K_{m}}{Ra}$$

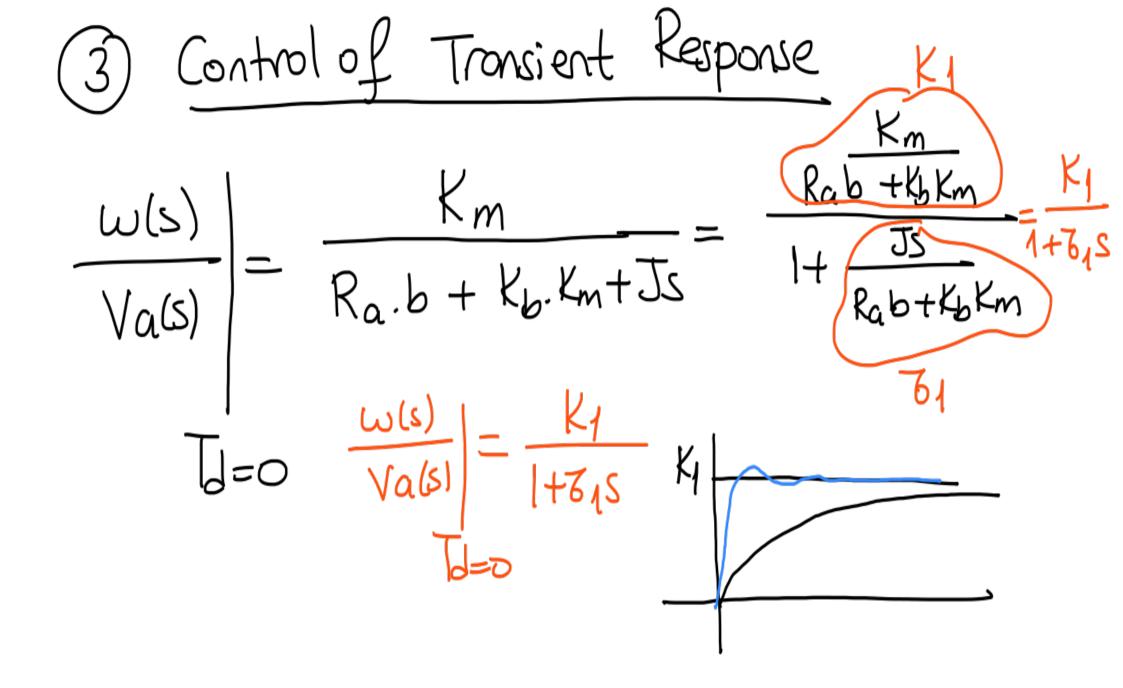


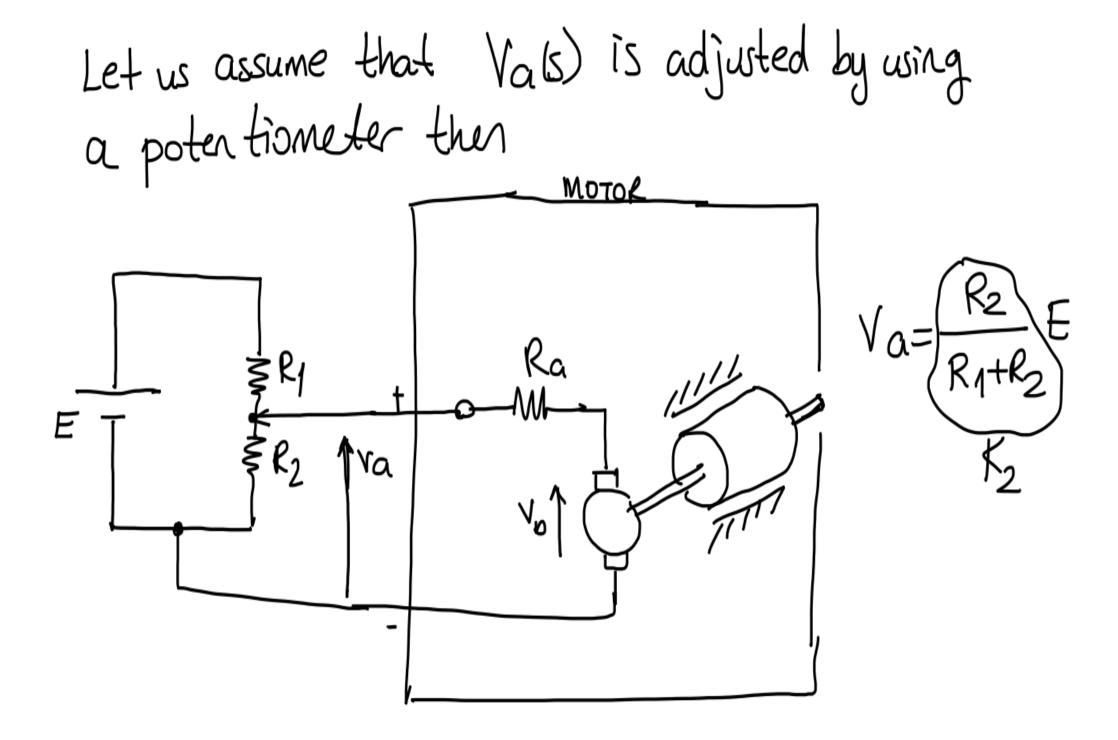
$$e_{ce}(\omega) = \lim_{s \to 0} s \in ce(s) = \frac{D}{\frac{K_a K_m}{R_a} \left(K_t + \frac{K_b}{R_a} \right)}$$

$$e_{oe}(\omega) = \frac{D}{b + \frac{K_b K_m}{R_a}}$$

$$e_{o}(\omega) \quad \text{for large} \quad \text{amplifier gain Ka}$$

$$\Rightarrow e_{ce}(\omega) \ll e_{o}(\omega)$$

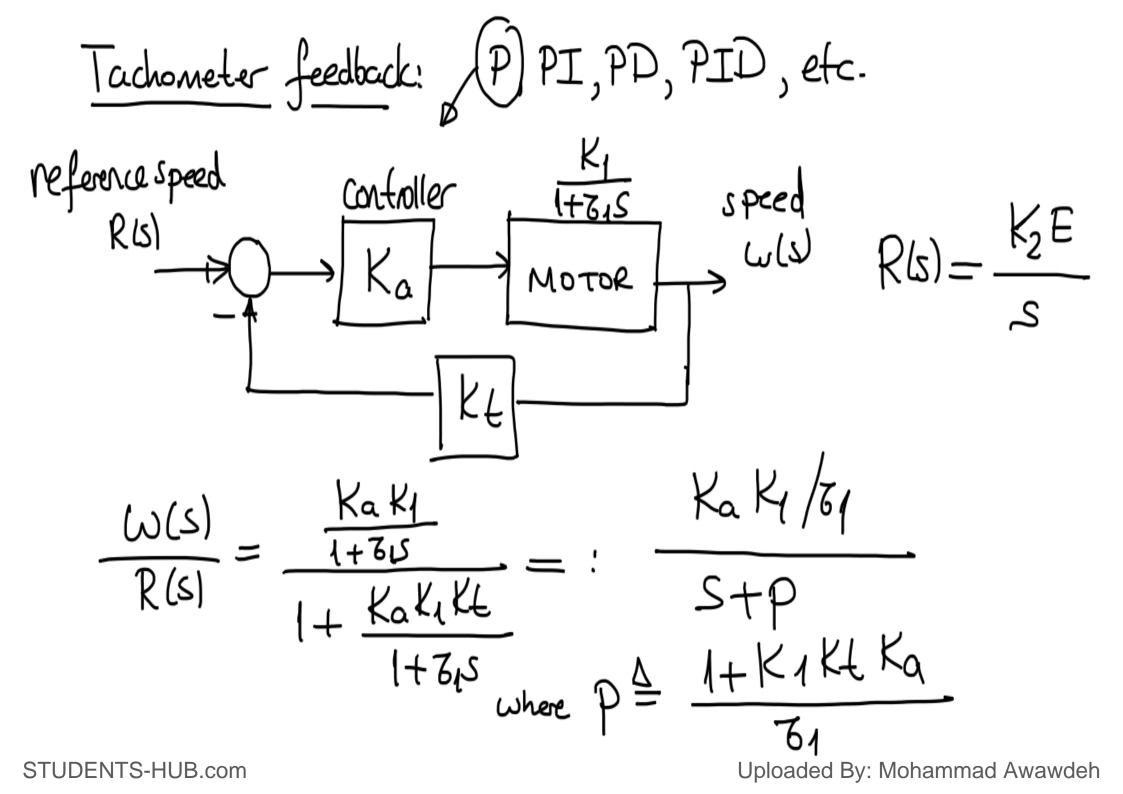


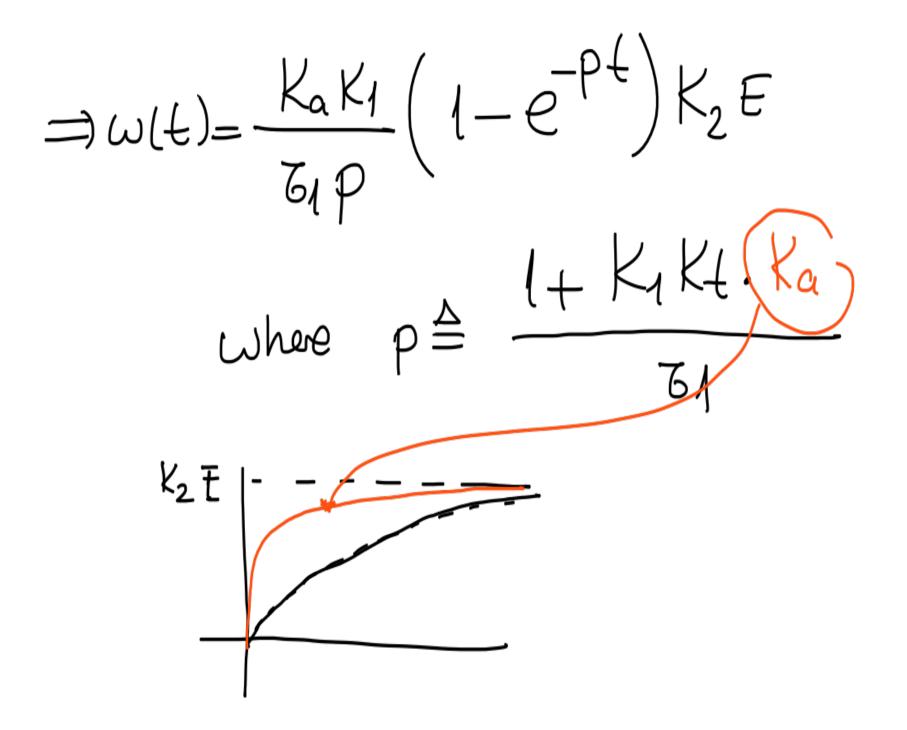


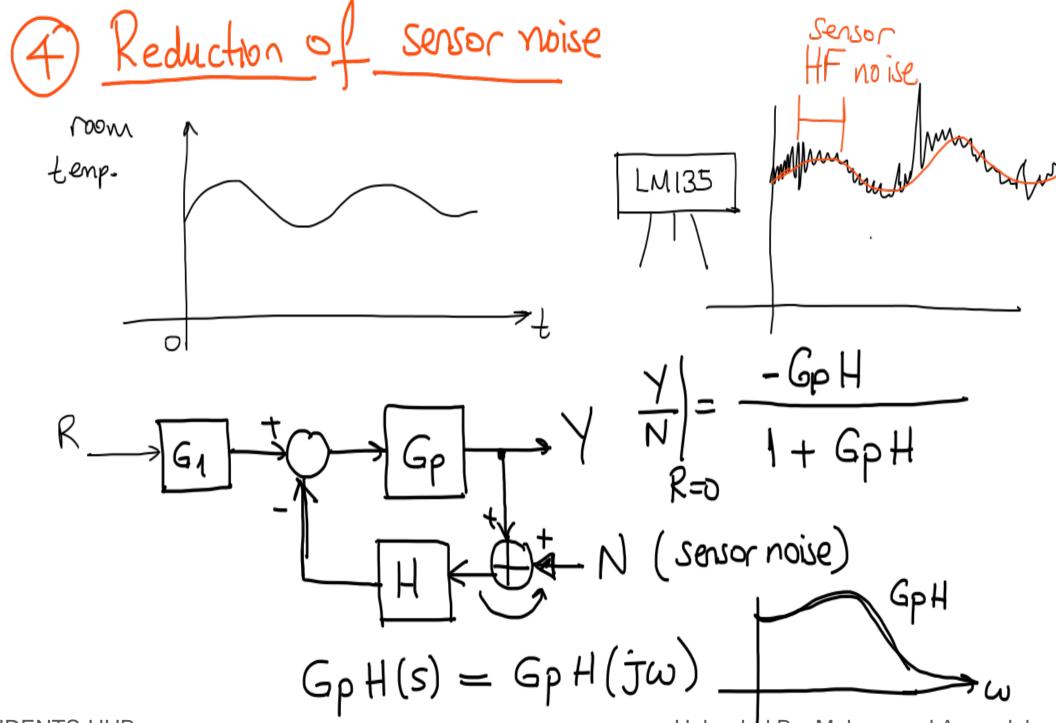
$$(\omega(s)) = \frac{K_1}{1+\overline{c_1}s} \cdot \frac{K_2 E}{s} = K_1 K_2 E \left(\frac{1}{s} - \frac{\overline{c_1}}{1+\overline{c_1}s}\right)$$
where $K_2 = \frac{R_2}{R_1+R_2}$ $\omega(t) = K_1 K_2 E \left(1 - \overline{e}^{-\frac{t}{\overline{c_1}}}\right)$

$$K_1 K_2 E \left(-\frac{1-\overline{e}^{-\frac{t}{\overline{c_1}}}}{1-\overline{e}^{-\frac{t}{\overline{c_1}}}}\right)$$

$$K_1 K_2 E \left(-\frac{1-\overline{e}^{-\frac{t}{\overline{c_1}}}}{1-\overline{e}^{-\frac{t}{\overline{c_1}}}}\right)$$







To attenuate sensor noise |GpH| must be low at frequencies of the sensor noise. (mostly at high freq.) (5) Reduction of Steady-State Error! $\frac{1}{5} = R \longrightarrow G \longrightarrow Y \xrightarrow{R=5} G \longrightarrow G \longrightarrow Y$ Open-loop syst. closed-loop syst. $E_{CL} = R - Y = R - \frac{G}{I+G}R$ $E_0 = R - Y = R - GR$ = R(I-G) $R \Rightarrow e_{\mathcal{C}}(\mathcal{M}) = -\frac{1}{1+G(\mathbf{o})}$ $I + G(\mathbf{o})$ $I + G(\mathbf{o})$ $I + G(\mathbf{o})$ $|\mathcal{C}_{o}(\infty)| = \lim_{s \to \infty} sE_{o}(s) = 1 - G(o) \cong G_{o}$