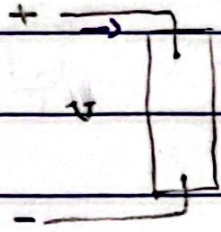


chapter 11:-

passive sign convention:-

current
- direction



$$p = \frac{dw}{dt}$$

$$p = Vi \text{ or } -Vi$$

→ can be positive or negative

- if $p > 0$ the element is

"absorbing power"

"absorbed power by the element"

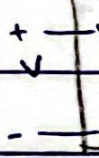
- if $p < 0$ the element

"delivering power"

"delivered power by the element"

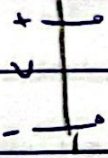
⇒ → i

①



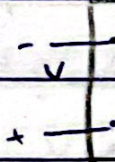
← i

②



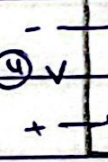
→ i

③



← i

④



1, 4

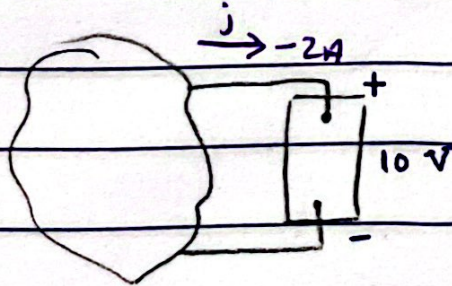
$$p = Vi$$

2, 3

$$p = -Vi$$

or +

Ex:-



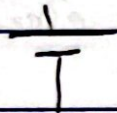
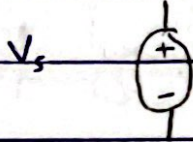
$$p = Vi$$

$$= (10)(-2)$$

$$= -20 \text{ W del. power}$$

Chapter (2): Voltage and Sources

Ideal Voltage source

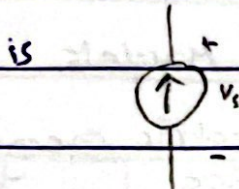


independent

• Voltage ثابتة

• التيار يتغير على الدارة

Ideal current source



Δ

independent

• Voltage على اقتران ال source

$V_s \rightarrow$ depends on the circuit

• يتغير على الدارة

$I_s \rightarrow$ constant

• التيار ثابت

dependent sources:-

• قيمة V_s or I_s voltage or current

same where in the circuit



$$V_s = A V_x$$

• ideal dependent voltage source
• voltage-controlled



$$V_s = A i_x$$

• ideal dep volt
• current controlled



$$I_s = A V_x$$

• ideal dep. curr. so
• Volt-cont.

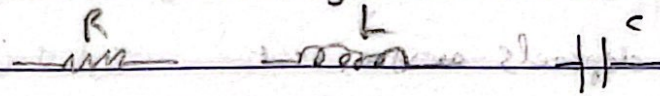


$$I_s = A i_x$$

• Ideal dep curr-so
• current-cont.

active element:- one that models a device capable of generating electric energy. \uparrow

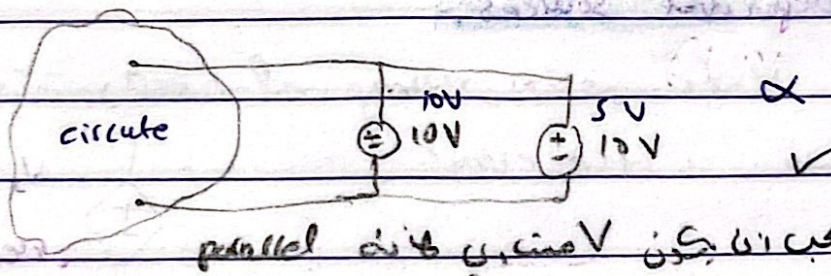
passive elements:- one that models a physical device that cannot generate electric energy



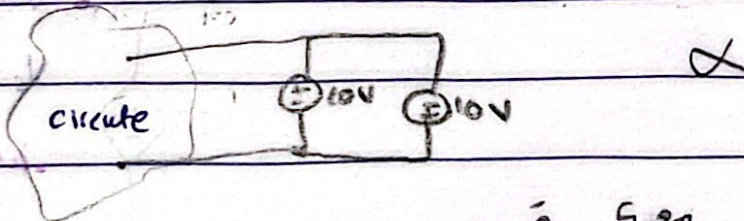
Ex:-

Voltage

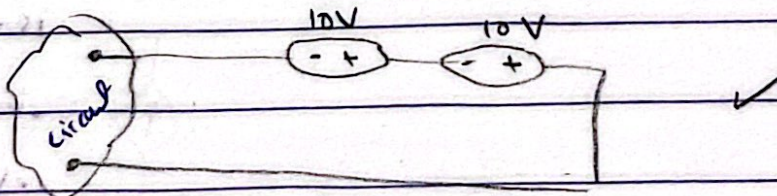
1, 3)



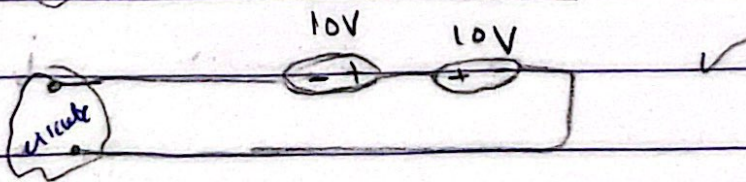
2)



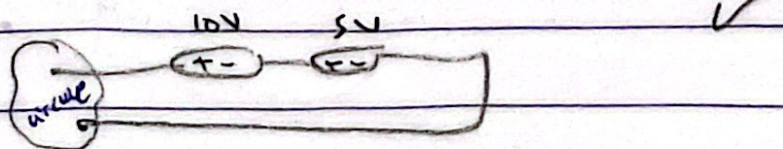
4)



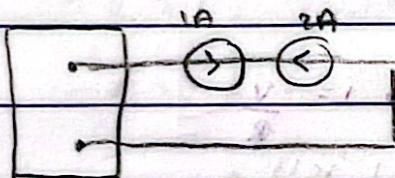
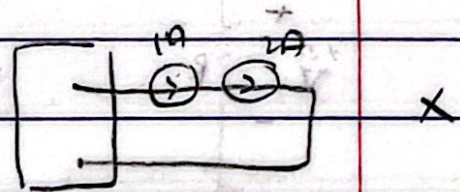
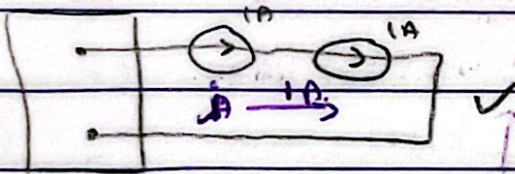
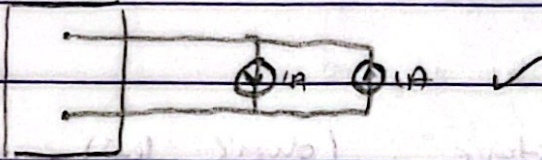
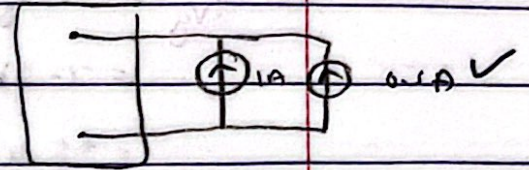
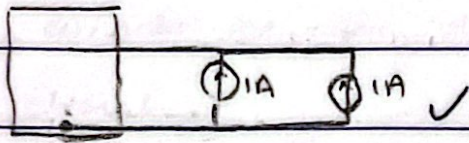
5)



6)



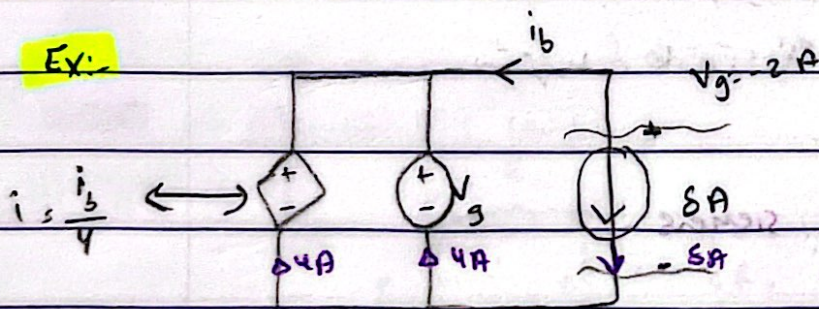
current:



يمكن التوصل بطريقتين مختلفتين، الأولى القياس

ملاحظة على power فترتبط بالطرف

Ex:



dependent source.

voltage source / current source

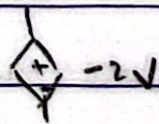
a) what value of V_g is required in order for the interconnection to be valid?

b) for this V_g find the power associated with the 8A source.

a $\Rightarrow i_b = -8A$

in $i = -\frac{8A}{4} = -2A$

in $V_g = -2V$



b $\Rightarrow P = V_i = (-2)(8) = -16W$ (del-power)

← يعني طاقة

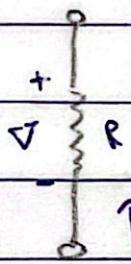
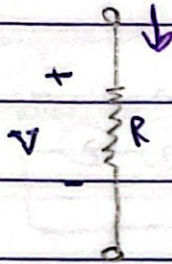
$$P_{Vg} = -V_g (1)$$

$$= -(1-2)(1.5)$$

$$= 1.5 \text{ W (abs. power)}$$

الطاقة الممتصة

(2.2) Electrical resistance (ohm's law)



$$P = Vi, \quad P = -Vi$$

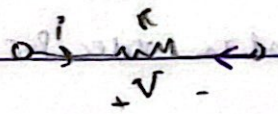
$$V = iR, \quad i = \frac{V}{R}, \quad V = -iR, \quad i = -\frac{V}{R}$$

• دالة الجوان النهائية +1 لأن المقاومة

ستكون طانة دالة

conductance G :-

$$G = \frac{1}{R} \quad \left[\frac{S}{\Omega} \right] \text{ siemens}$$



$$P = Vi, \quad P = -Vi$$

$$V = i^2 R, \quad i = \frac{V}{R}$$

$$= \frac{V^2}{R}, \quad V = \frac{V^2}{R}$$

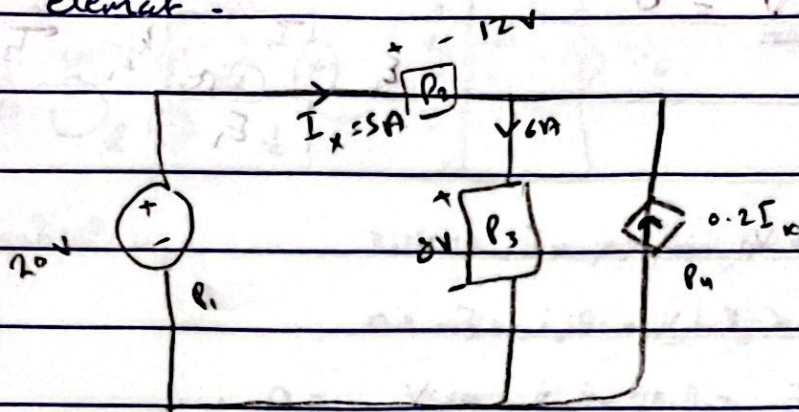
is V_p^+

- The algebraic sum of power in a circuit at any instant of time must be zero.

$$\sum P_{in} = 0$$

$$P_{abs} = P_{dep}$$

Ex:- calculate the power absorbed or delivered by each element.



$$P_1 = -VI \text{ (del)}$$

$$= -20(5) = -100 \text{ W}$$

$$P_2 = VI \text{ (abs)}$$

$$= 12(5) = 60 \text{ W}$$

$$P_3 = VI = 8 \times 5 = 40 \text{ W (abs)}$$

$$P_4 \rightarrow -100 + 60 + 40 = 0$$

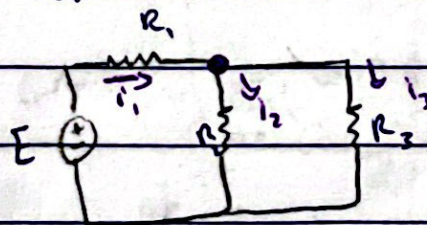
$$\text{or } P_4 = -VI = 8(0.5 \times 2) = -8 \text{ W}$$

$$\therefore P_4 = -8 \text{ W (del)}$$

$$= -8 \text{ W}$$

(2.4)

Kirchhoff's laws



KCL "Kirchhoff's current law". At any node, the sum of currents entering the node is equal to the sum of currents leaving the node.

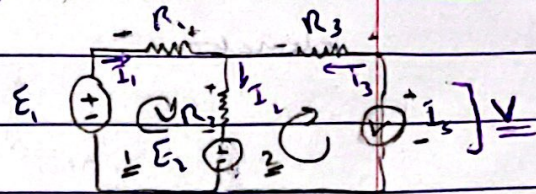
$$\sum I_{in} = \sum I_{out} \Rightarrow i_1 = i_2 + i_3$$

$$\sum I_{out} = 0 \Rightarrow -i_1 + i_2 + i_3 = 0$$

$$\sum I_{in} = 0 \Rightarrow i_1 - i_2 - i_3 = 0$$

• KVL:- "Kirchhoff's Voltage law".

المجموع الجهد $\sum V = 0$



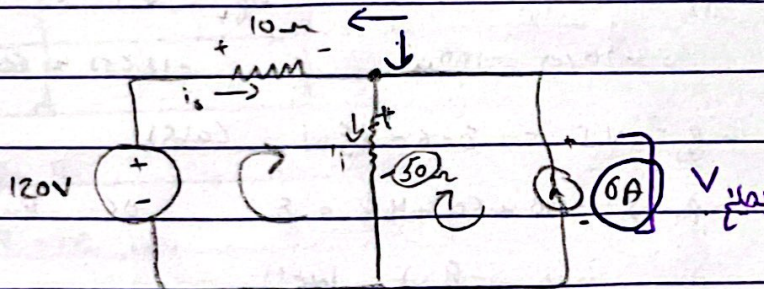
KVL \Rightarrow

$-E_1 - V_{R1} - R_2 i_2 + E_2 = 0$

$-E_1 - (-R_1 i_1) + R_2 i_2 + E_2 = 0$

KVL $\Rightarrow -E_1 - R_1 i_1 - R_2 i_2 + V_{\text{مخرج}} = 0$

EX:



a) find i_0 :

KVL $\Rightarrow -120 + 10i_0 + 50i_1 = 0$

KCL $\Rightarrow i_0 + 6 = i_1$

$\Rightarrow -120 + 10i_0 + 50(i_0 + 6) = 0$

$\Rightarrow i_0 = -3 \text{ A} \quad , \quad i_1 = 3 \text{ A}$

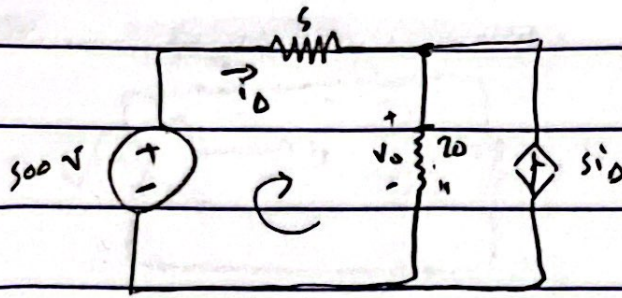
b) V :

KVL $\Rightarrow -50i_1 + V = 0$

$\Rightarrow -50(3) + V = 0 \quad \Rightarrow V = 150 \text{ V}$

Ex:-

(1)



\Rightarrow find V_o

$$KVL \Rightarrow -500 + 5i_o + V_o = 0$$

$$KCL \Rightarrow i_o = 5i_o + i_o = 6i_o$$

$$-500 + 5i_o + 20i_o = 0$$

$$-500 + 5i_o + 120i_o = 0$$

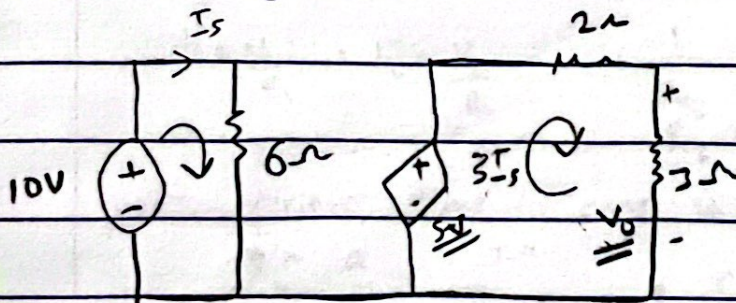
$$i_o = 4A \quad i_o = 24A$$

$$V_o = 20i_o$$

$$= 20(24) = 480V$$

(2)

Find V_o



$$KVL \Rightarrow 1) I_s 6 - 10 = 0$$

$$I_s = \frac{10}{6} A$$

$$KVL \Rightarrow 0 = -5 + 2i + 3i$$

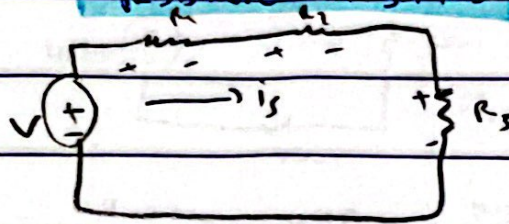
$$i = 1A$$

$$V_o = 3V$$

Ex (2.10)

chapter (CS):-

Resistor in series



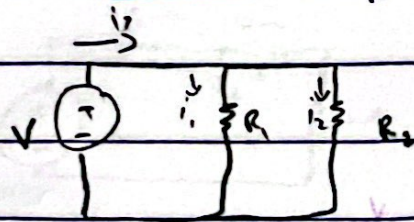
$$KVL \Rightarrow -V_s + R_1 i_s + R_2 i_s + R_3 i_s = 0$$

$$V_s = \underbrace{(R_1 + R_2 + R_3)}_{R_{eq}} i_s$$

$$R_{eq} = R_1 + R_2 + R_3 + \dots + R_n$$

series resistor have the same current.

Resistor in parallel



$$KCL \Rightarrow I_s = i_1 + i_2$$

$$= \frac{V}{R_1} + \frac{V}{R_2} = V \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$$

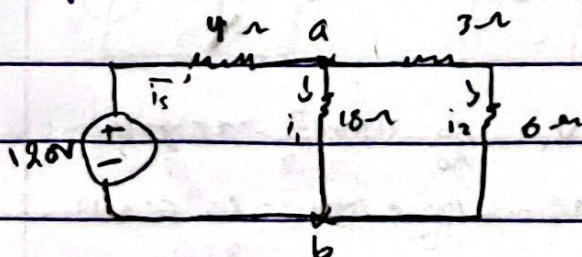
$$i_1 = \frac{V}{R_1}, \quad i_2 = \frac{V}{R_2}$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n}$$

$$R_{eq} = \frac{R_1 R_2}{R_1 + R_2}$$

parallel resistor have the same voltage.

Ex:-



$$R_{eq} = [9 \parallel 18] + 4 = 10 \Omega$$

$$I_s = \frac{V}{R} = \frac{120}{10} = 12 A$$

$$i_1 = \frac{(6+3) \times 12}{(6+3)+18}$$

current divider rule

$$i_2 = \frac{18}{18+(6+3)} \times 12$$

$$V_{ab} = ?$$

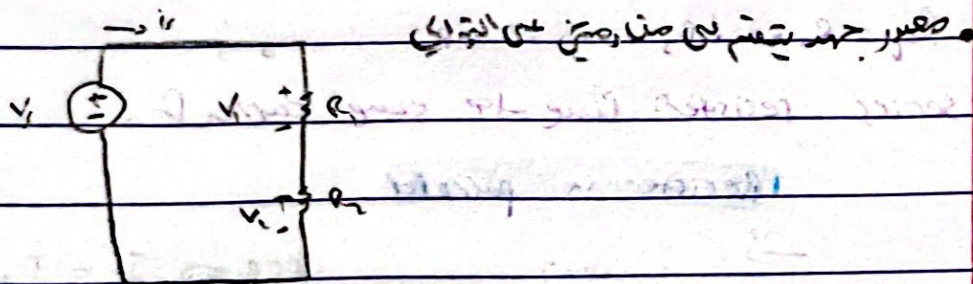
$$-120 = (4 \times 12) + V_{ab} \Rightarrow V_{ab} = 120 - 4 \times 12$$

$$= 72 \text{ Volt}$$

$$\rightarrow i = \frac{72}{16} = 4.5 \text{ A}$$

$$\rightarrow i_v = \frac{72}{8} = 9 \text{ A}$$

→ The Voltage Divider Rule (VDR)

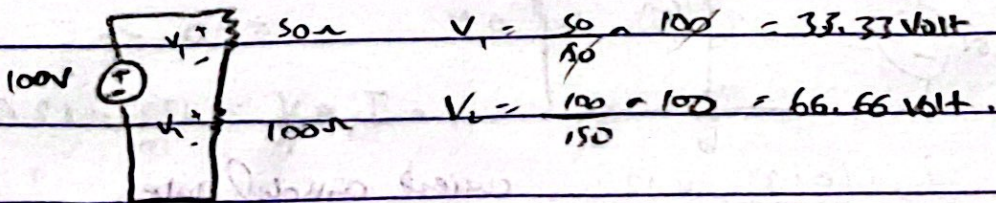


Step (1) $i = \frac{V_s}{R_1 + R_2}$

Step (2) $V_1 = R_1 i = \frac{R_1}{R_1 + R_2} V_s$

$$V_2 = R_2 i = \frac{R_2}{R_1 + R_2} V_s$$

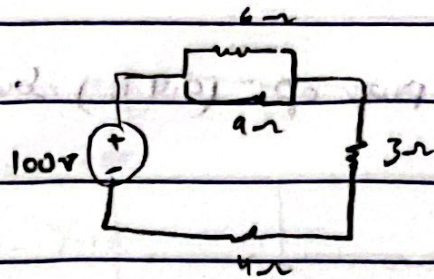
والنسبة بقى الحاصل بقى العكس بقى بقى المقاوم بقى



$$V_1 = \frac{50}{150} \times 100 = 33.33 \text{ Volt}$$

$$V_2 = \frac{100}{150} \times 100 = 66.66 \text{ Volt}$$

Ex:

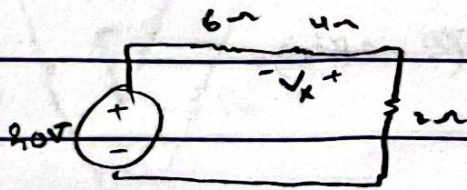


$$V_4 = \frac{4}{4 + (3 + 6 \parallel 9)} \times 100 = 37.73 \text{ V}$$

$$V_3 = \frac{3}{3 + (4 + 6 \parallel 9)} \times 100 = 28.30 \text{ V}$$

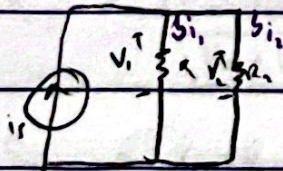
$$V_6 = V_9 = \frac{(6 \parallel 9)}{(6 \parallel 9) + 3} \times 100 = 33.96 \text{ V}$$

Ex:



$$V_x = \frac{-4}{8 + 4} \times 20 = -6.66 \text{ Volt.}$$

→ super current divider rule :- (CDR)



$$V_1 = V_2 = V_L$$

$$V = i_2 R_{eq}$$

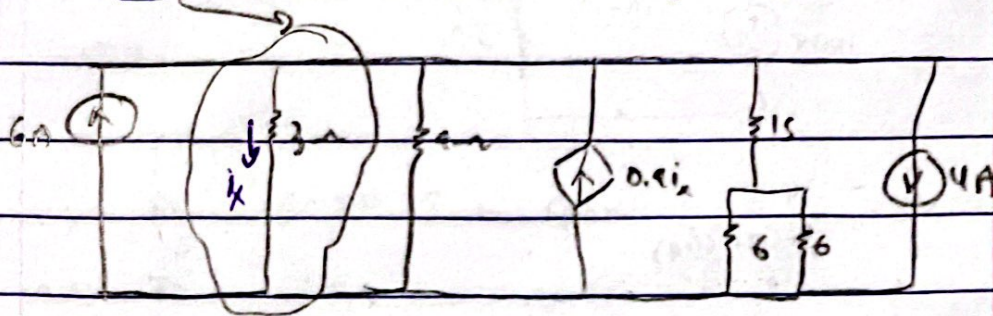
$$= i_2 \times \frac{R_1 R_2}{R_1 + R_2}$$

$$i_1 = \frac{V}{R_1} = \frac{R_2}{R_1 + R_2} i_2$$

$$i_2 = \frac{R_1}{R_1 + R_2} i_2$$

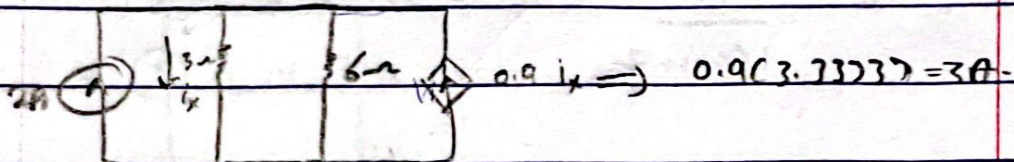
Ex:-

Find for power of $(0.9 i_x)$ source.



$$1) (6 \parallel 6) + 15 = 18$$

$$2) (18 \parallel 4) = 6 \Omega$$



$$CDR \Rightarrow i_x = \frac{6}{6+3} = (2 + 0.9 i_x)$$

$$\therefore i_x = 3.333 \text{ A}$$

$$\therefore V_x = (3) i_x$$

$$V_x = 3 \times \frac{10}{3} = 10 \text{ volt}$$

$$P = -V i = -V_x (3)$$

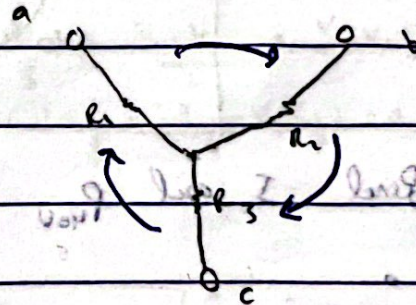
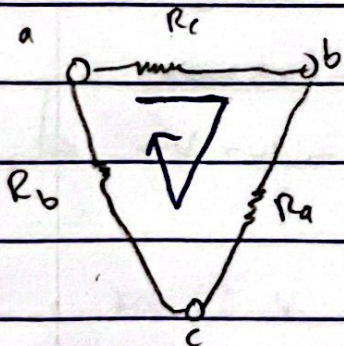
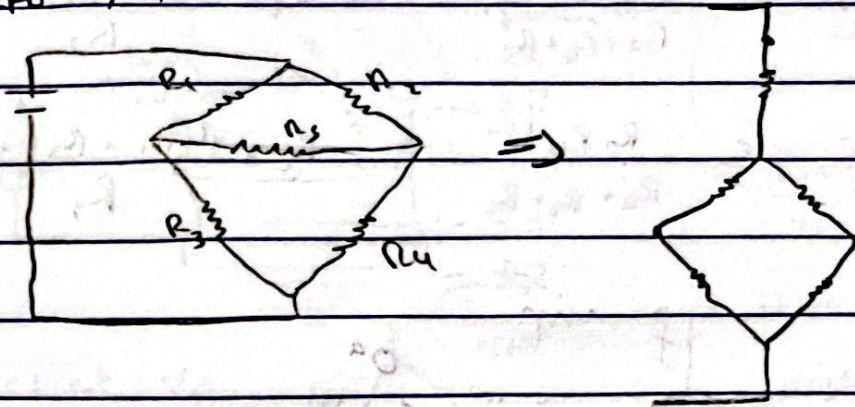
$$= -30 \text{ W del}$$

(3.7)

Delta-to-wye

pi-to-tee.

Δ -to-Y



نفس الحقا. لكن ليس نفس الترتيب لاضداد ترتيب وتسمية المراتح

$$R_{ab} = \frac{(R_1 + R_2) R_3}{R_1 + R_2 + R_3} = R_{ab} = R_1 + R_2$$

$$R_{bc} = \frac{(R_2 + R_3) R_1}{R_1 + R_2 + R_3} = R_{bc} = R_2 + R_3$$

$$R_{ac} = \frac{(R_1 + R_3) R_2}{R_1 + R_2 + R_3} = R_{ac} = R_1 + R_3$$

$$R_1 = \frac{R_b R_c}{R_a + R_b + R_c}$$

$$R_a = \frac{R_1 R_2 + R_1 R_3 + R_2 R_3}{R_1}$$

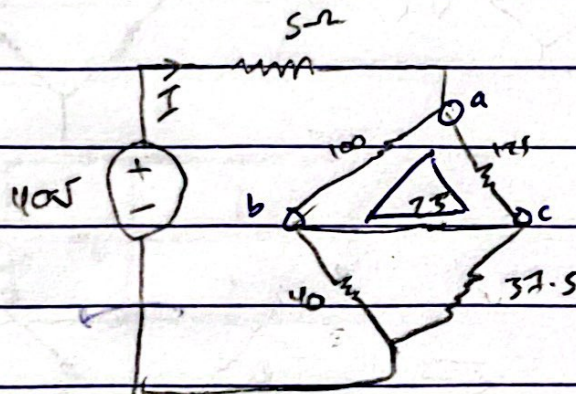
$$R_2 = \frac{R_a R_c}{R_a + R_b + R_c}$$

$$R_b = \frac{R_1 R_2 + R_1 R_3 + R_2 R_3}{R_2}$$

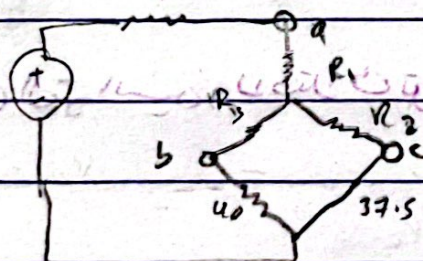
$$R_3 = \frac{R_a R_b}{R_a + R_b + R_c}$$

$$R_c = \frac{R_1 R_2 + R_1 R_3 + R_2 R_3}{R_3}$$

Ex:-



Find I and P_{40V}



$$R_1 = \frac{100 \times 125}{100 + 125 + 125} = 50 \Omega$$

$$R_2 = \frac{125 \times 75}{100 + 125 + 25} = 12.5 \Omega$$

$$R_3 = \frac{100 \times 25}{100 + 125 + 25} = 10 \Omega$$

$$\Rightarrow R_{eq} = (37.5 + R_4) // (40 + R_3) + R_1 + 5$$

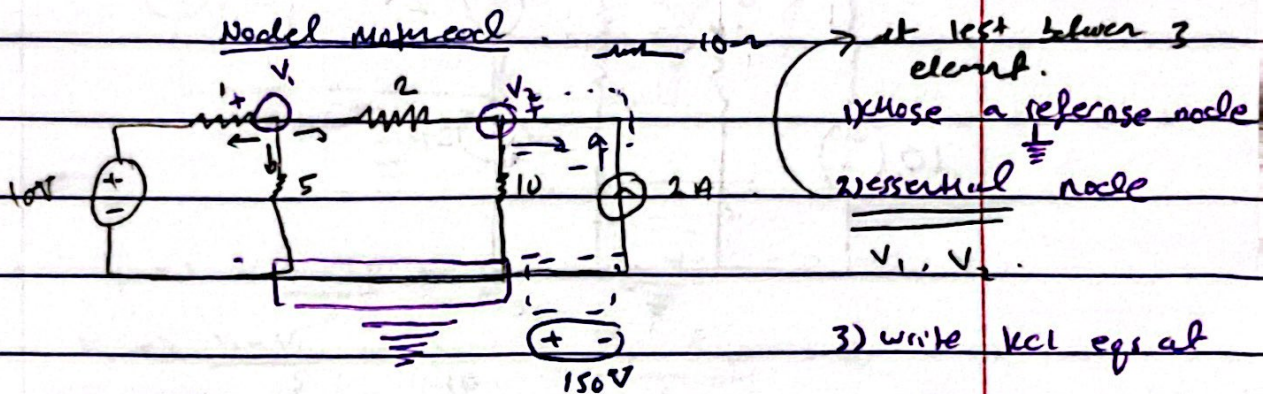
$$= 80 \Omega$$

$$\therefore I = \frac{40}{80} = 0.5 \text{ A}$$

$$\therefore P_{40V} = -40(0.5) = -20 \text{ W} \quad \text{del power in}$$

chapter (4):

• Node-voltage method



• KCL at V_1

$$\sum I_{out} = 0$$

$$I_1 + I_2 + I_3 = 0 \Rightarrow \frac{V_1 - 10}{1} + \frac{V_1}{5} + \frac{V_1 - V_2}{2} = 0 \quad V_1, V_2, \dots, V_n$$

$$\rightarrow -V_1 + 10 + \frac{V_1}{5} + \frac{V_1 - V_2}{2} = 0 \Rightarrow V_1 \left(1 + \frac{1}{5} + \frac{1}{2}\right) - V_2 \left(\frac{1}{2}\right) = 0 \quad (1)$$

• KCL at V_2

$$\sum I_{out} = \frac{V_2 - V_1}{2} + \frac{V_2}{10} - 2 = 0$$

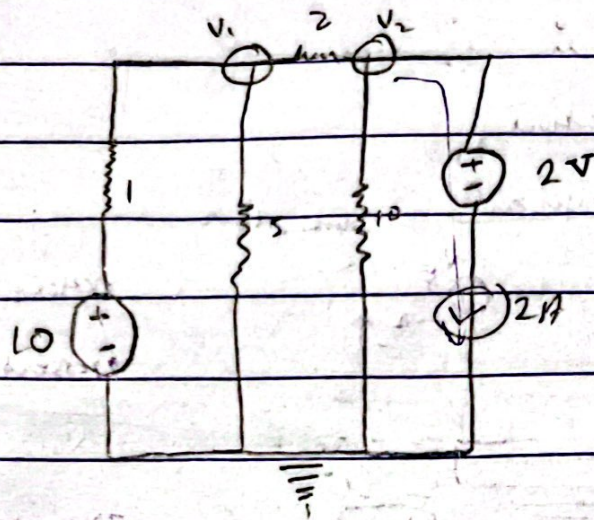
$$= -\frac{1}{2}V_1 + V_2 \left(\frac{1}{2} + \frac{1}{10}\right) = 2 \quad (2)$$

$$\Rightarrow V_1 = 9.09 \text{ V}$$

$$V_2 = 10.91 \text{ V}$$

\Rightarrow Same as above.

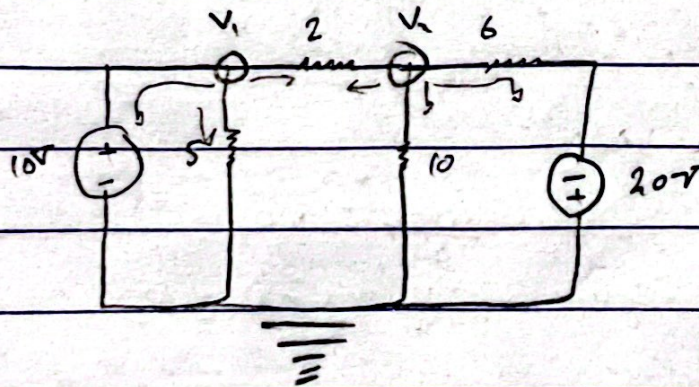
Ex- ①



$$V_1 \Rightarrow \frac{V_1 + 10}{1} + \frac{V_1}{5} + \frac{V_1 - V_2}{2} = 0$$

$$V_2 \Rightarrow \frac{V_2 - V_1}{2} + \frac{V_2}{10} + 2 = 0$$

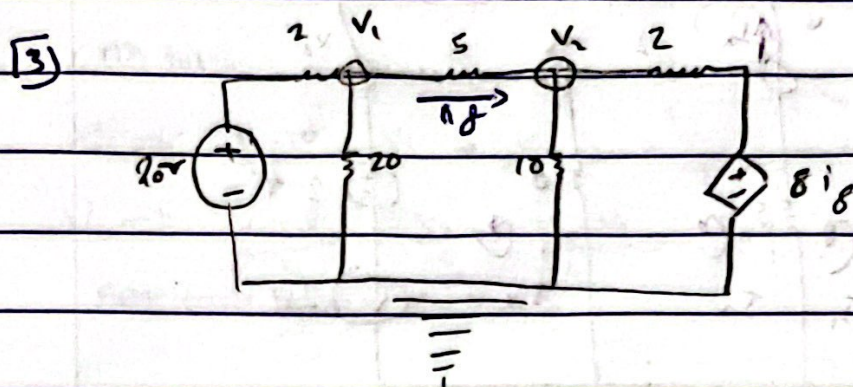
②



$$V_1 = 10 \text{ V}$$

at

$$V_2 \Rightarrow \frac{V_2 - 10}{2} + \frac{V_2}{10} + \frac{V_2 + 20}{6} = 0$$



$$\text{at } V_1 \Rightarrow \frac{V_1 - 20}{2} + \frac{V_1}{20} + \frac{V_1 - V_2}{5} = 0$$

$$\text{at } V_2 \Rightarrow \frac{V_2 - V_1}{5} + \frac{V_2}{10} + \frac{V_2 - 8i_\phi}{2} = 0$$

$$\Rightarrow i_\phi = \frac{V_1 - V_2}{5}$$

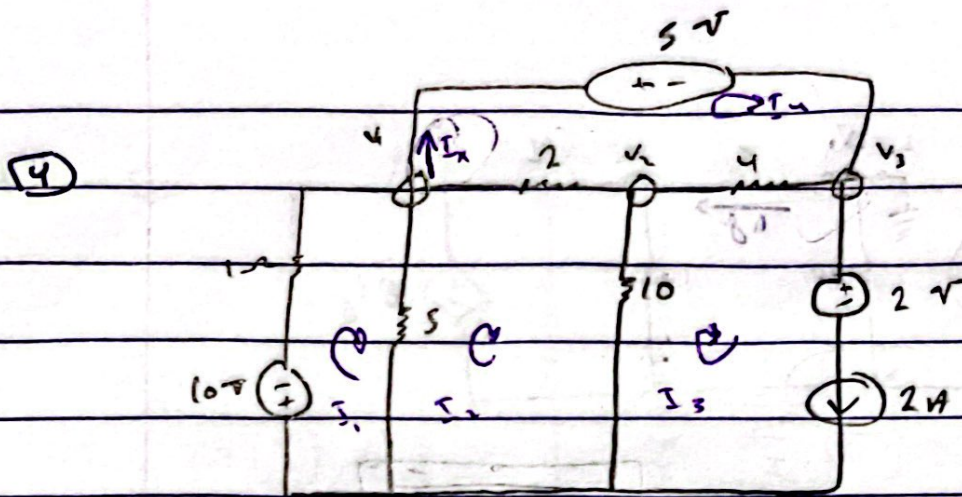
$$\Rightarrow \frac{V_2 - V_1}{5} + \frac{V_2}{10} + \frac{V_2 - 8\left(\frac{V_1 - V_2}{5}\right)}{2} = 0$$

$$\Rightarrow 0.75 V_1 - 0.2 V_2 = 10$$

$$-V_1 + 1.6 V_2 = 0$$

$$\therefore V_1 = 16 \text{ V}$$

$$V_2 = 10 \text{ V}$$

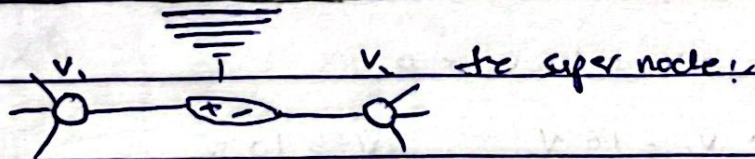
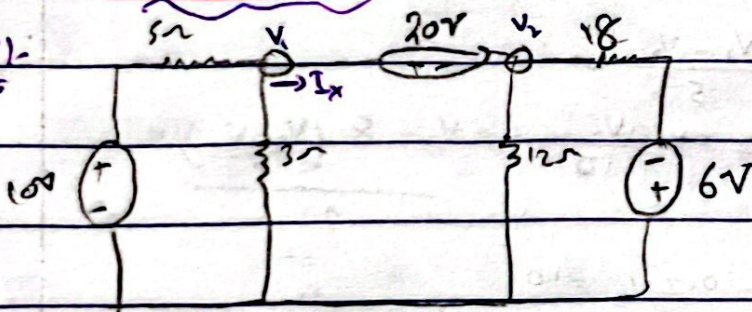


$V_1 = 5V$ id to ground at V_3

special case:-

supernode:-

Ex:-



$$\frac{V_1 - 10}{5} + \frac{V_1}{3} + I_x = 0$$

$$\frac{V_1 - 10}{5} + \frac{V_1}{3} + \frac{V_1}{12} + \frac{V_2 + 6}{18} = 0$$

$$\Rightarrow V_1 - V_2 = 20 \quad (\text{supernode eq})$$

$$\frac{V_1 - V_2 + 20}{15}$$

④ Sol:-

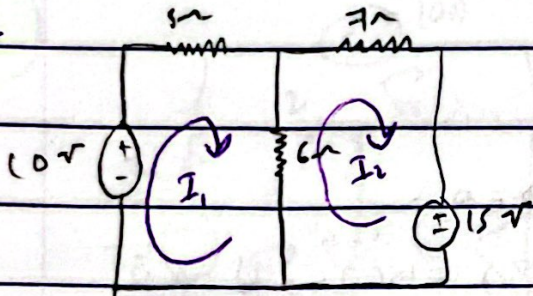
$$V_1 \Rightarrow \frac{V_1 - 10}{1} + \frac{V_1}{5} + \frac{V_1 - V_2}{2} + \frac{V_2 - V_1}{4} + 2 = 0$$

$$V_2 \Rightarrow \frac{V_2 - V_1}{2} + \frac{V_2}{10} + \frac{V_2 - V_1}{4} = 0$$

$$\text{Super node eq:- } V_1 = V_2 = 5$$

Mesh-current method

Ex:-



→ write mesh current I_1, I_2, I_3, \dots

all cw or all ccw.

→ for each mesh current, write KVL eqs.

$$I_1 \Rightarrow -10 + 5I_1 + 6(I_1 - I_2) = 0$$

$$11I_1 - 6I_2 = 10$$

$$I_2 \Rightarrow 15 + 6(I_2 - I_1) + 7I_2 = 0$$

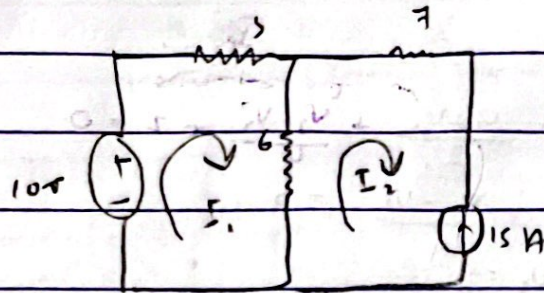
$$13I_2 - 6I_1 = -15$$

$$0 = (15 - 2)I_1 + 7I_2 + 0I_3 \dots$$

$$13I_2 - 6I_1 = -15$$

$$13I_2 - 6I_1 = -15$$

Ex:-



$$I_2 = -15 \text{ A}$$

$$I_1 \Rightarrow -10 + 5I_1 + 6(I_1 - 15) = 0$$

$$11I_1 + (15)(6) = 10 \Rightarrow 11I_1 = 10 - 90 = -80 \Rightarrow I_1 = -7.27 \text{ A}$$

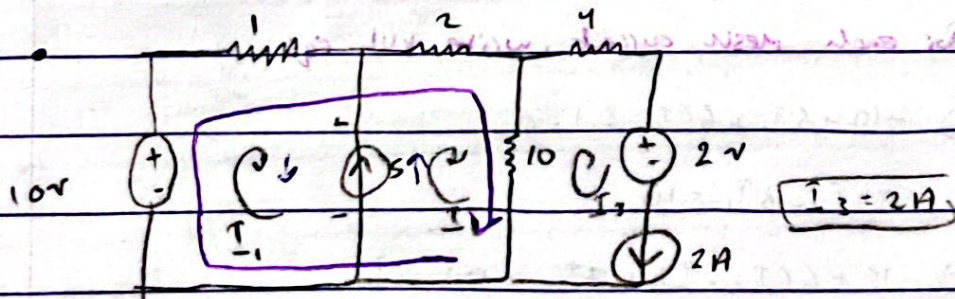
back to ex (4):-

$$I_3 = 2 \text{ A}$$

$$I_1 \Rightarrow -10 + I_1 + 5(I_1 - I_2) = 0$$

$$I_2 \Rightarrow 5(I_1 - I_2) + 2(I_2 - I_4) + 10(I_2 - 2) = 0$$

$$I_4 \Rightarrow 5 + 4(I_4 - 2) + 2(I_4 - I_2) = 0$$

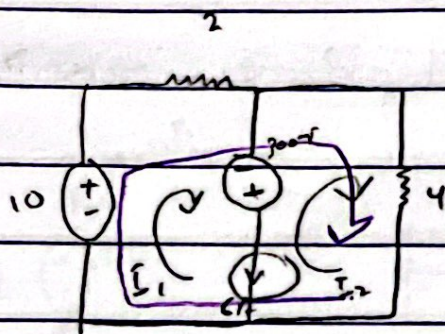


$$\left. \begin{aligned} I_1 \Rightarrow -10 + I_1 + \frac{V}{2\Omega} &= 0 \\ I_2 \Rightarrow - \end{aligned} \right\} \times$$

normal KVL $\Rightarrow -10 + I_1 + 2I_2 + 10(I_2 - 2) = 0$

st mesh current-

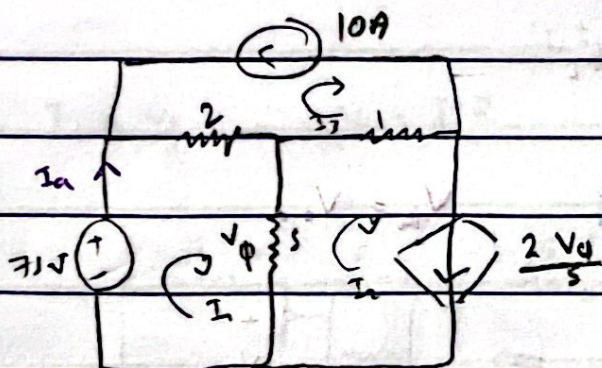
$$S = I_2 - I_1 \Rightarrow \text{super mesh}$$



$$-10 + 2I_1 + 4I_2 = 0$$

$$I_1, I_2 = 6$$

4.11
128



$$I_3 = -10 \text{ A}$$

$$I_2 = \frac{2V_g}{5}$$

$$\text{But } V_g = 5(I_1 - I_2)$$

$$\Rightarrow I_2 = 2I_1 - 2I_2$$

$$2I_1 - 3I_2 = 0 \quad \Rightarrow I_2 = \frac{2}{3}I_1$$

$$I_1 \Rightarrow -7.5 + 2(I_1 + 10) + 5(I_1 - I_2) = 0$$

$$-7.5 + 2I_1 + 20 + 5I_1 - 5 \cdot \frac{2}{3}I_1 = 0$$

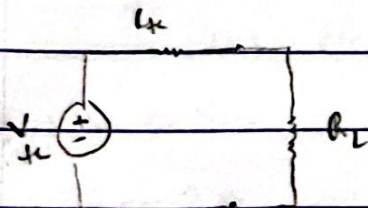
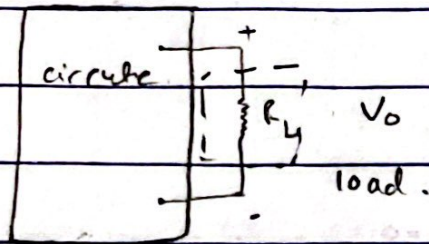
$$5.5 = 7I_1 - \frac{10}{3}I_1$$

$$\Rightarrow I_1 = 15 \text{ A}$$

$$\Rightarrow I_2 = \frac{2}{3} \cdot 15 = 10 \text{ A}$$

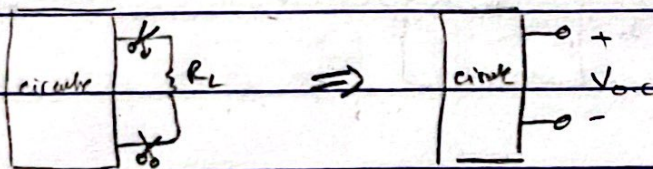


Thermin's theorem:-



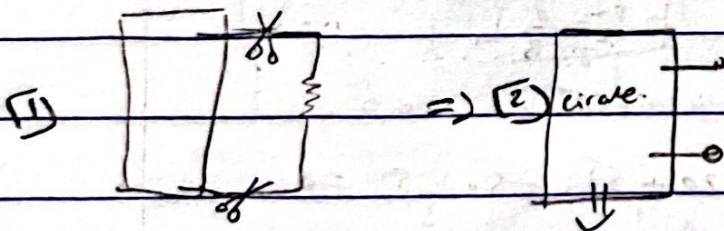
How to find V_{th}

$$V_{th} = V_{oc}$$

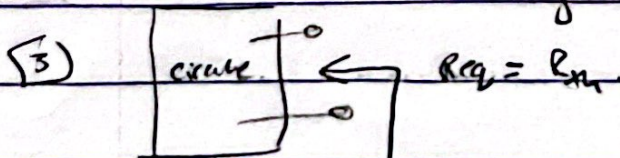


How to find R_{th}

case 1: no dep. sources.

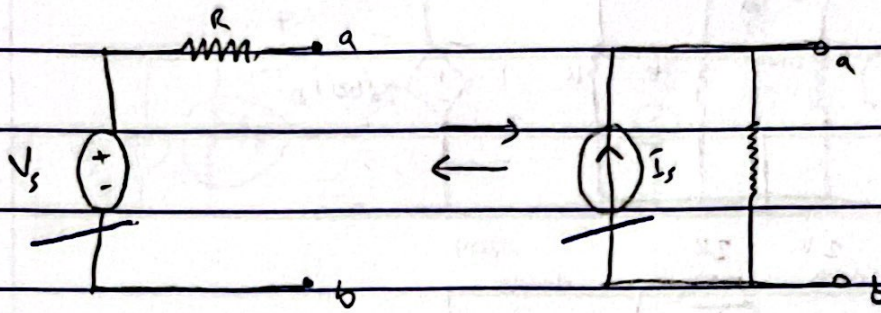


kill all indep. sources (short)



\Rightarrow

Source transformation:-

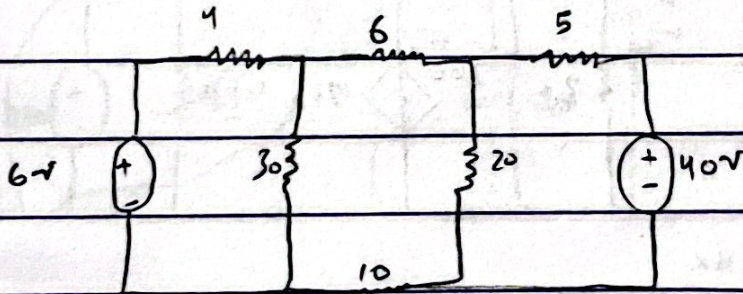


same direction.

النَّارِ صَاحِبِي (بِالطَّرِيقِ)

$$I_s = \frac{V_s}{R}, \quad V_s = I_s R$$

Ex:-

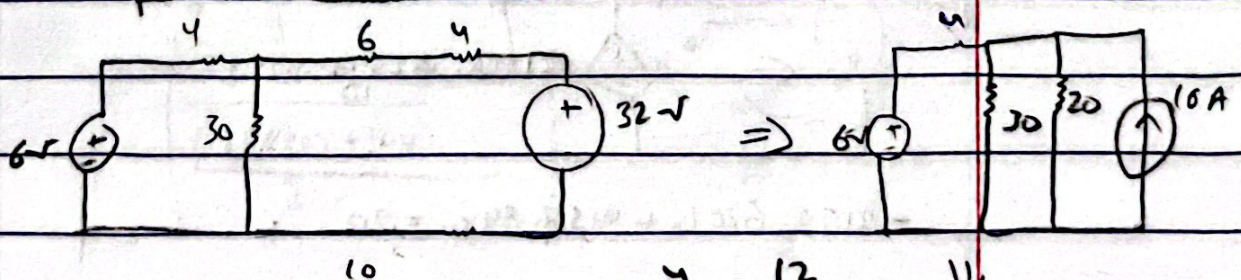
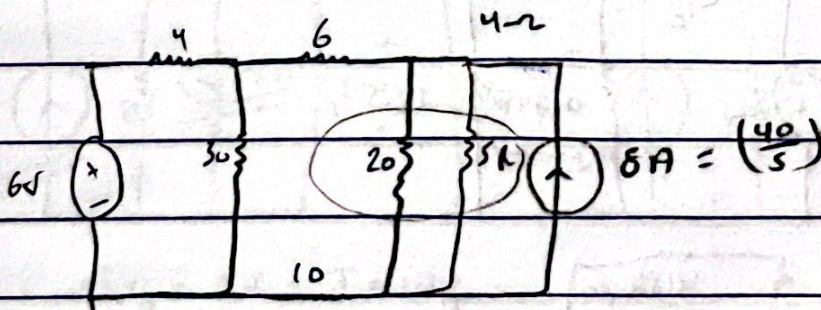


$$P_6 = ?$$

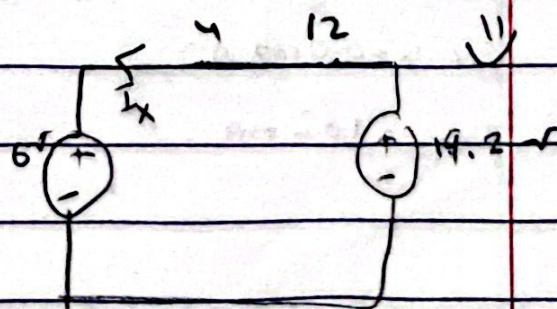
$$= V I_x$$

$$= 6 \times 0.825 = 4.95 \text{ W}$$

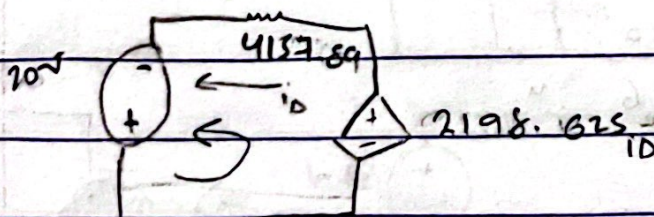
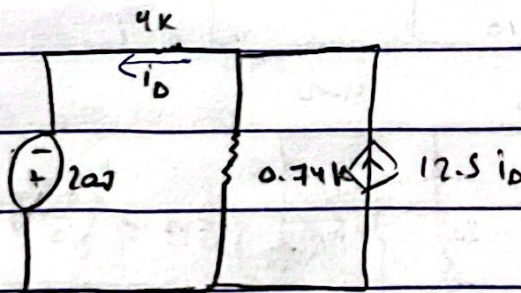
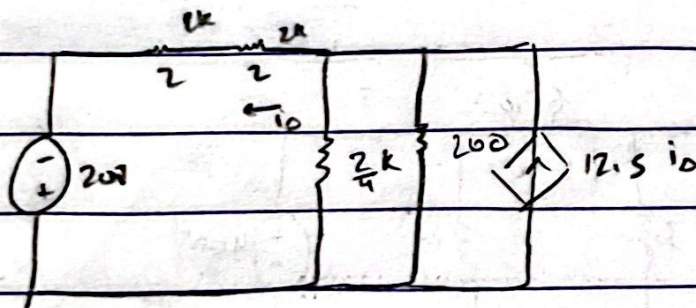
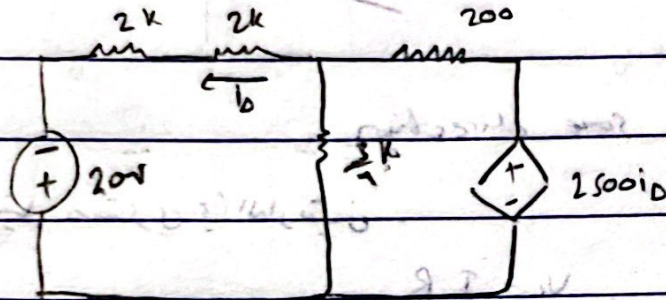
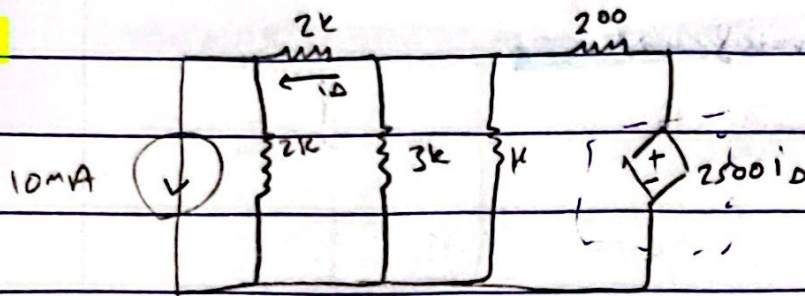
abs.



$$I_x = \frac{19.2 - 6}{4 + 12} = 0.825 \text{ A}$$



Ex:

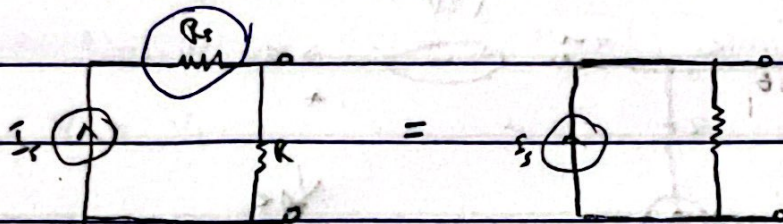
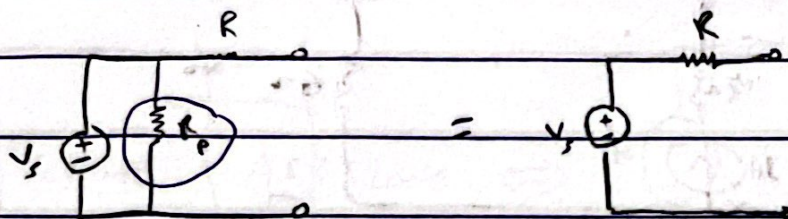


$$-2198.625i_D + 4157.89i_D = 20$$

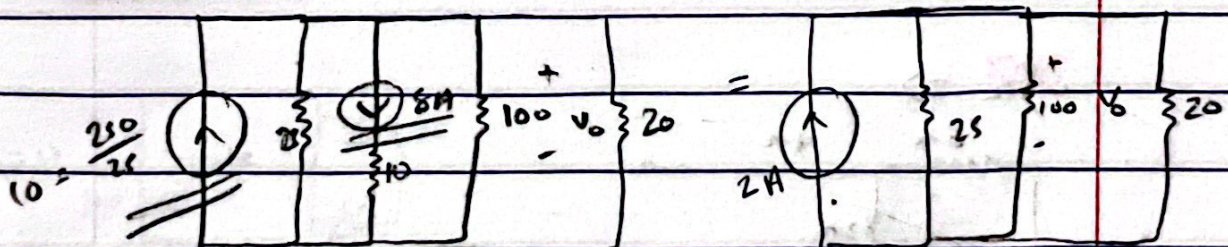
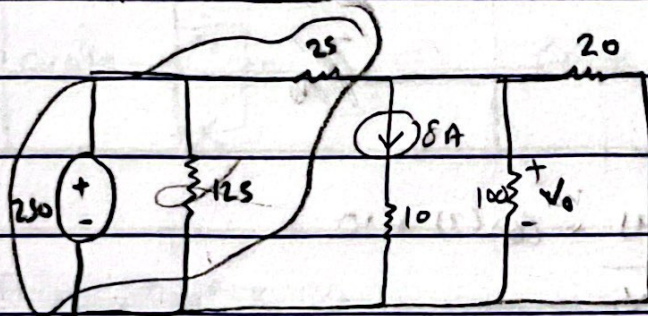
$$i_D = 0.0102 A$$

$$= 10.2 mA$$

Special cases:



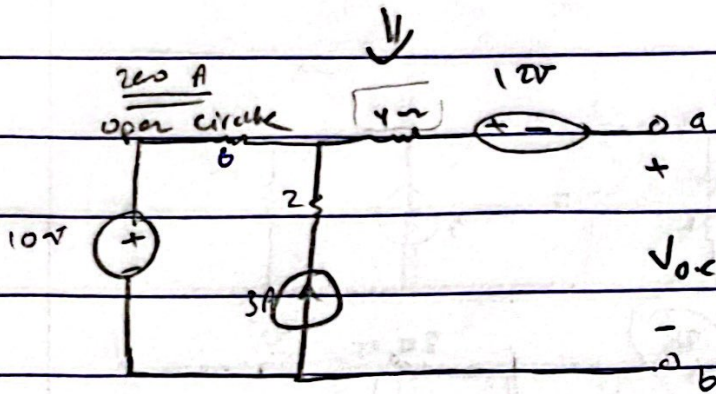
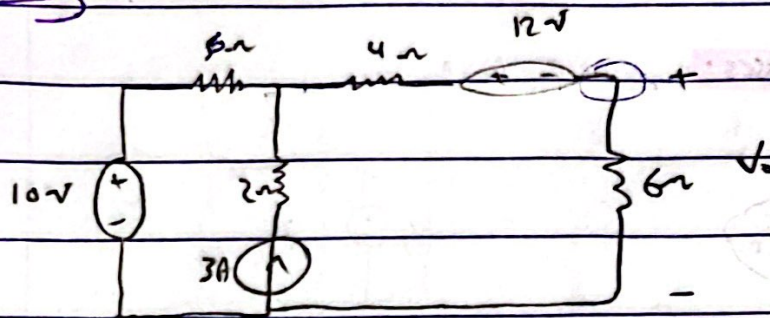
Ex:-



$$V_o = IR = I \times 100$$

$$V_o = \left[\frac{(25 \parallel 20) \times 2}{(25 \parallel 20) + 100} \right] \times 100$$

Ex:-

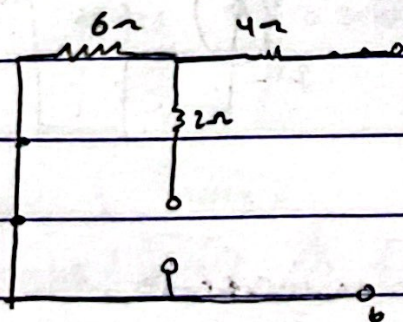


$$V_{th} = V_{oc}$$

$$V_{oc} = -12 + (0.4) + (6)(3) + 10$$

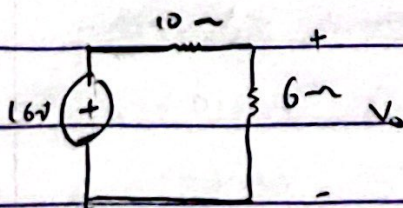
$$= 16 \text{ V} = V_{th}$$

$R_{th} \Rightarrow$



$$R_{th} = 6 + 4 = 10 \Omega$$

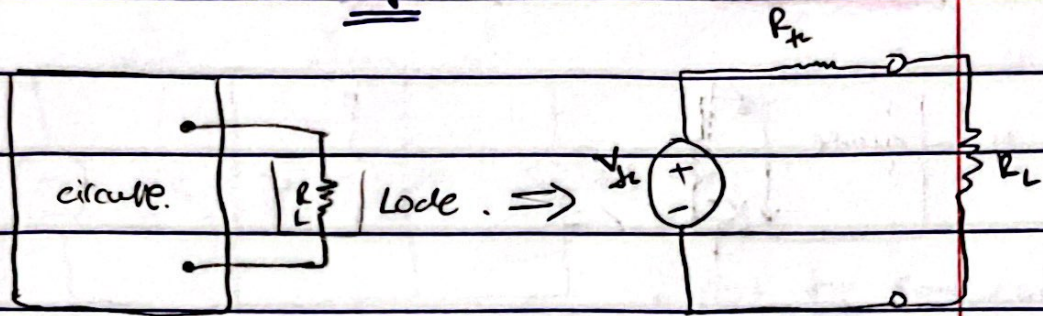
So \Rightarrow



$$V_o = V_{th} = \frac{6}{16} \times 16 = 6 \text{ V}$$

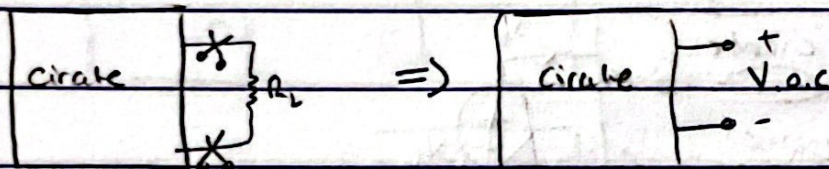
case II:-

Circuit with dep. sources.



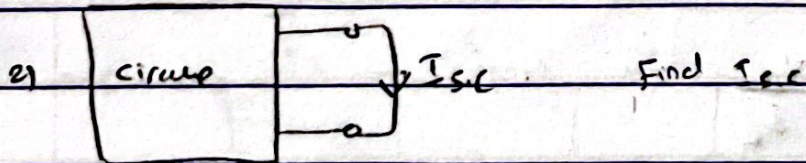
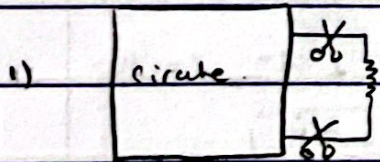
How to find V_L :-

$$V_L = V_{o.c}$$



How to find R_L :-

Method A:-

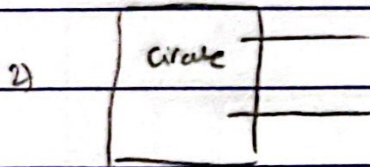
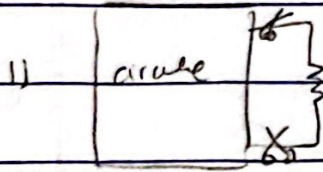


3)

$$R_L = \frac{V_{o.c}}{I_{s.c.}}$$

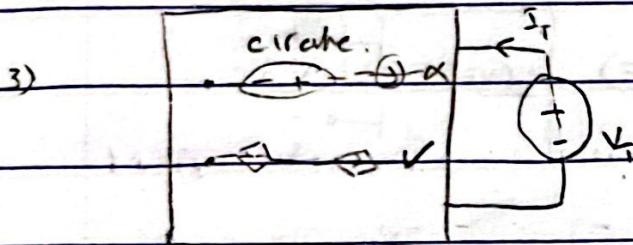
Method B:-

Test source methods



kill all indep. sources.

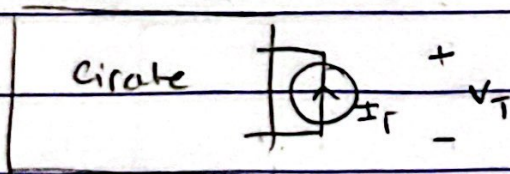
leave all dep. sources



use a test source: voltage source

current source

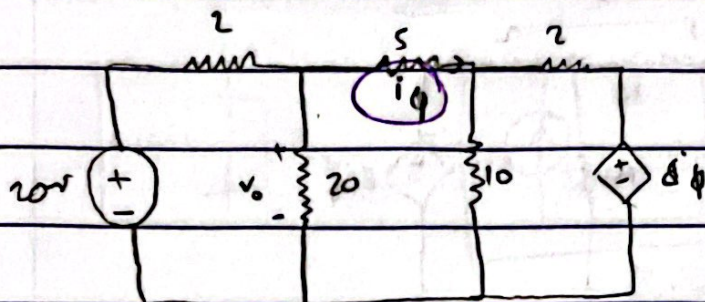
OR



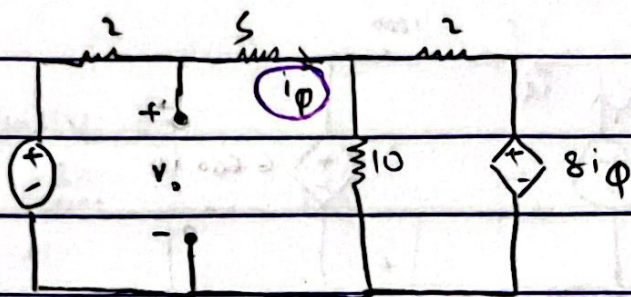
$$R_{th} = \frac{V_T}{I_T}$$

all indep. sources left to zero.

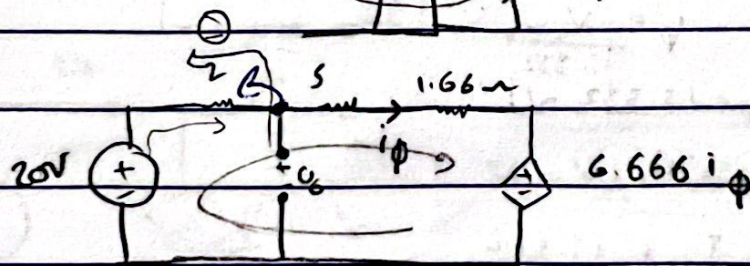
Ex:-



Not the same current



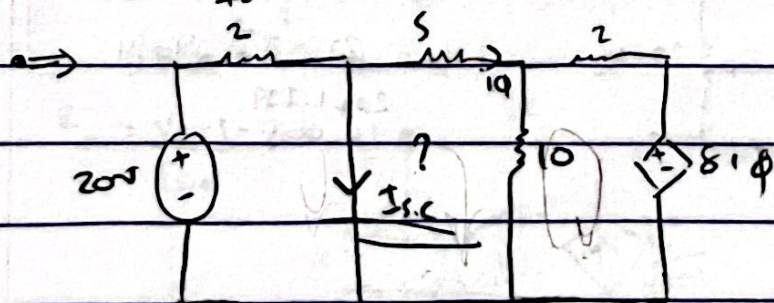
Source transformation



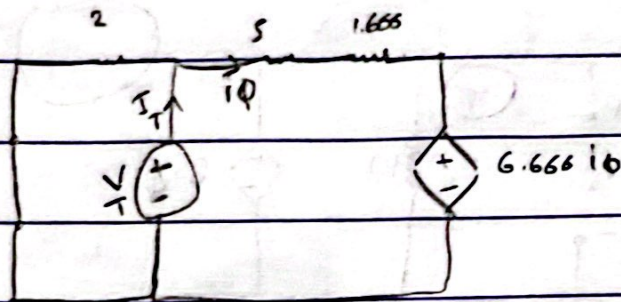
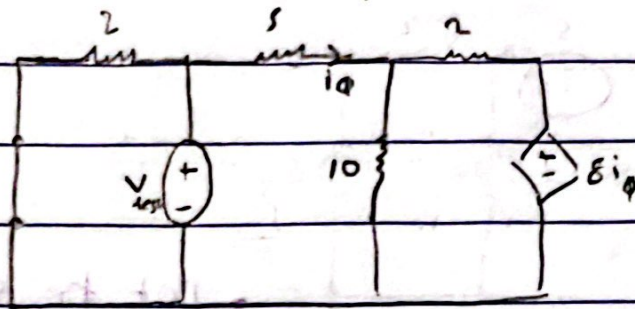
$$KVL \Rightarrow -20 + (2 + 5 + 1.666)i_\phi + 6.666i_\phi = 0$$

$$i_\phi = 1.3A$$

$$V_{0.2} = V = 20 - (1.3 \times 2) = 17.4V$$



⇒ Move to network B:-



$$\text{KVL} \Rightarrow -V_T + (5 + 1.666)i_\phi + 6.666i_\phi = 0$$

$$i_\phi = \frac{V_T}{13.332}$$

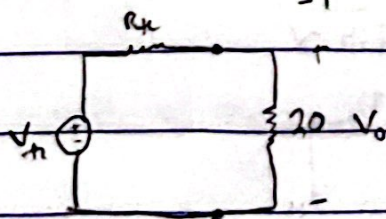
$$\text{Let } V_T = 13.332 \text{ V}$$

$$\therefore i_\phi = 1 \text{ A}$$

$$\therefore I_T = I_\phi + \frac{13.332}{2}$$

$$= 1 + \frac{13.332}{2} = 7.666 \text{ A}$$

$$\therefore R_T = \frac{V_T}{I_T} = 1.739$$

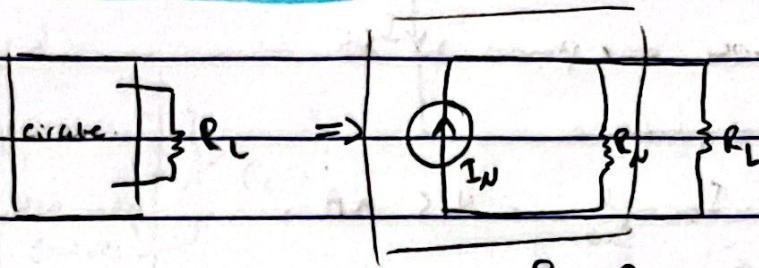


$$\therefore V_o = 20 \times 17.4$$

$$= 20 \times 1.739$$

$$= 16.008 \text{ V}$$

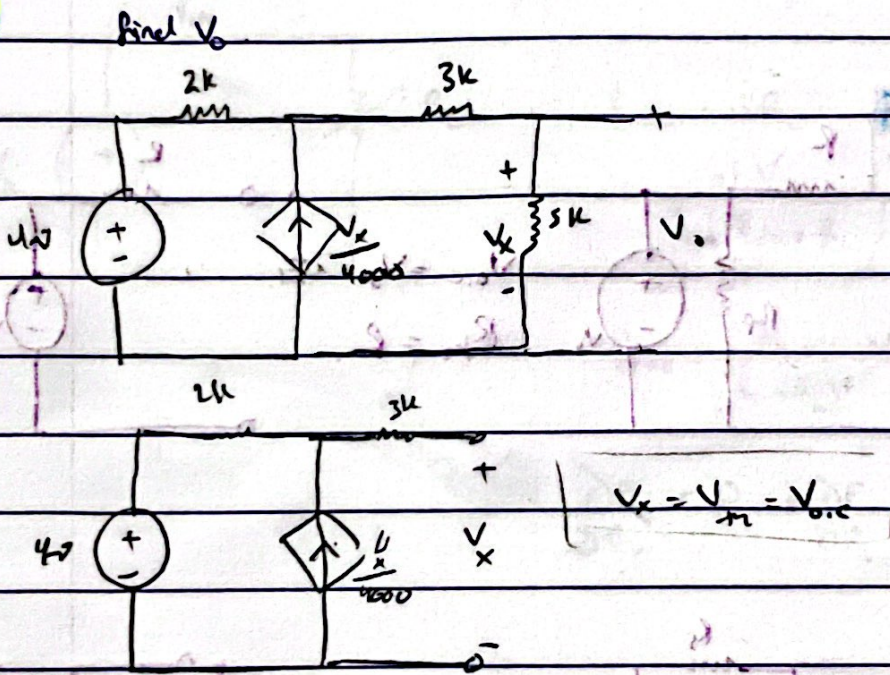
Norton of circuit:



$$R_N = R_{th}$$

$$I_N = I_{sc}$$

Ex:-

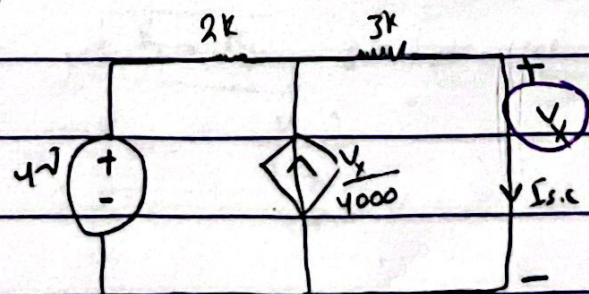


$$\text{in } V_{o.c} = \left(\frac{V_x}{4000} \right) 2k + 4 + (3 \times 0)$$

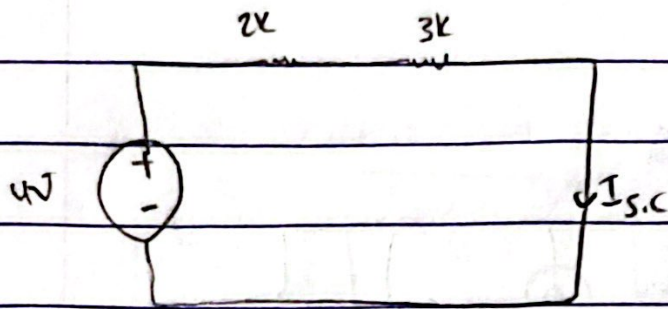
$$\frac{V_x}{4000} = \frac{V_x}{2} + 4$$

$$\text{in } V_x = 8V$$

$$R_N = \frac{V_{oc}}{I_{sc}}$$



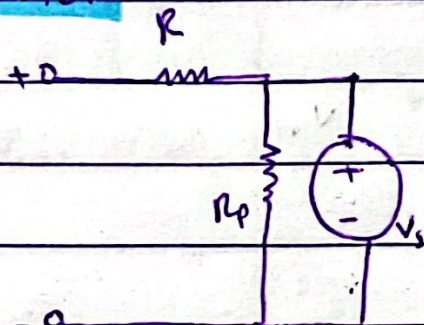
شورت، یعنی
2000 اهم
یعنی $V_x = 0$



$$\therefore I_{s.c} = \frac{4}{5000} = 4/5 \text{ mA}$$

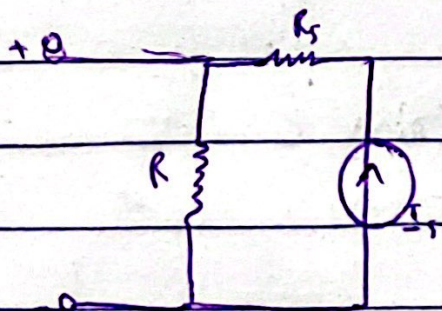
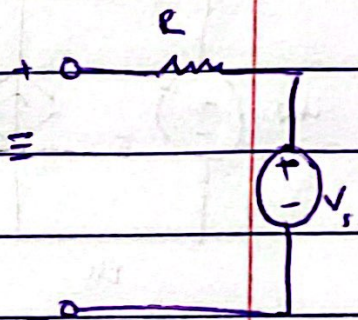
$$\therefore R_{th} = \frac{6}{4/5 \text{ mA}} = 10 \text{ k}\Omega$$

Note:-



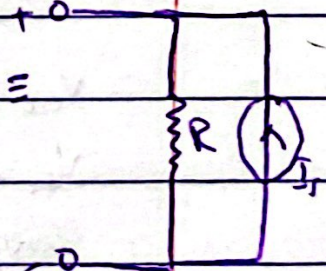
$$V_{o.c} = V_s$$


$$R_{th} = R$$




$$I_s = I_p = I_{s.c}$$

$$R_{th} = R_{in} = R$$



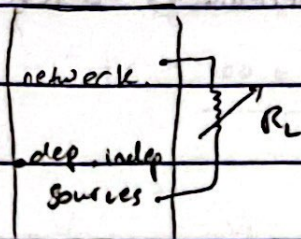
For R_{th} and $I_{s.c}$ 

Reverses 

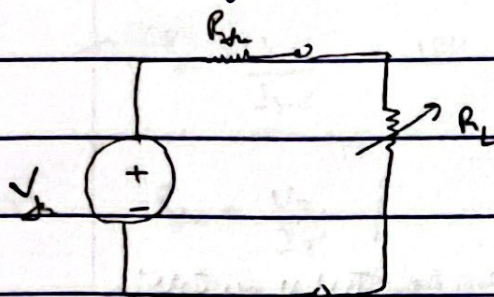
$C = V_s$

4.12

max power transfer:



↓
Thevenin's circuit.



$$P_{max} = i^2 R_L$$

$$= \left(\frac{V_{th}}{R_{th} + R_L} \right)^2 R_L$$

$$= P_{max} = \frac{R_L}{(R_{th} + R_L)^2} V_{th}^2$$

$$\frac{dP}{dR_L} = 0 \Rightarrow \frac{dP}{dR_L} = \frac{(R_{th} + R_L)^2 - 2R_L(R_{th} + R_L)}{(R_{th} + R_L)^4}$$

$$\propto V_{th}^2 = 0$$

$$\Rightarrow \frac{dP}{dR_L} = \frac{V_{th}^2 (R_{th}^2 + 2R_{th}R_L + R_L^2 - 2R_L^2 - 2R_L R_{th})}{(R_{th} + R_L)^4}$$

$$= R_{th}^2 - R_L^2 = 0$$

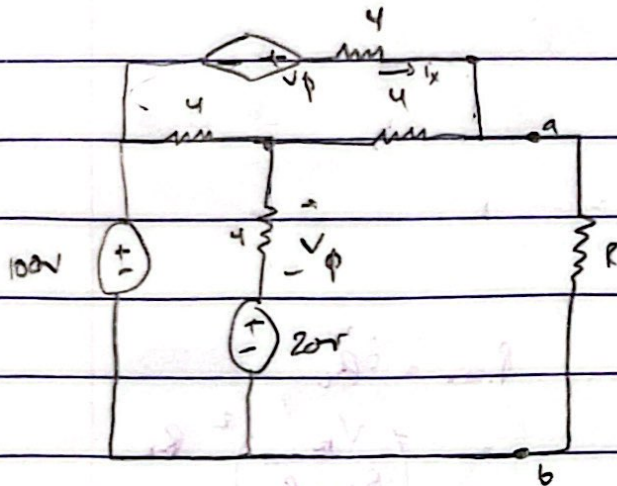
$$| R_L = R_{th} \text{ for max when } R_L = R_{th}$$

⇒

$$P_{max} = \frac{V_{th}^2}{4R_{th}}$$

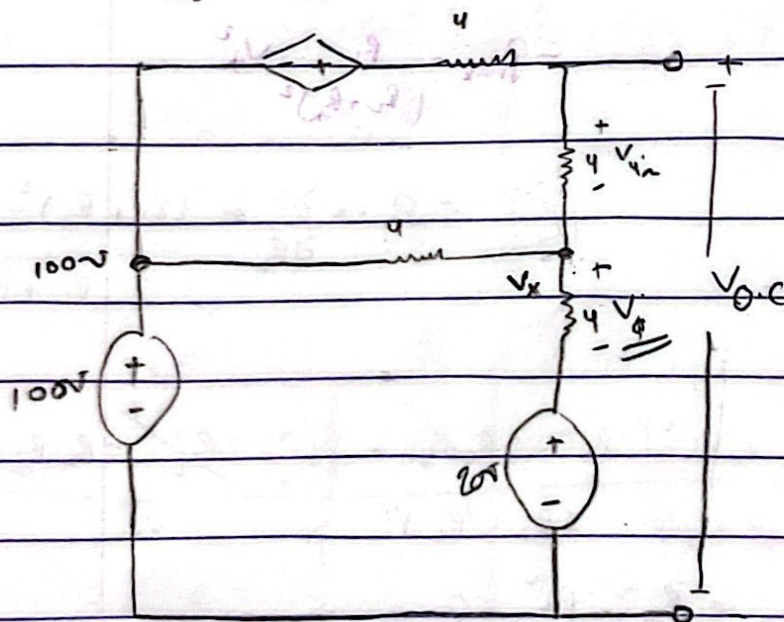
Ex:-

Find the value of R that enables the circuit to deliver max. power to the terminals a & b and then find P_{max} .



$$V_{th} = V_{o.c}$$

حالة رسم الدارة



$$\text{Node method} \Rightarrow \frac{V_x - 20}{4} + \frac{V_x - 100}{4} + \frac{V_x - 100 - V_\phi}{8} = 0$$

$$\text{But, } V_x = V_\phi + 20$$

$$\Rightarrow V_\phi = V_x - 20$$

$$\Rightarrow V_x = 80 \text{ Volt}$$

$$\therefore V_{o.c} = \underline{V_{Th}} + V_x$$

$$\Rightarrow -100 - V_\phi - 8i_x + V_x = 0$$

"to find I_x , KVL"

$$\therefore i_x = \frac{100 + V_\phi - (V_x)(80)}{8}$$

$$\Rightarrow I_x = 10 \text{ A}$$

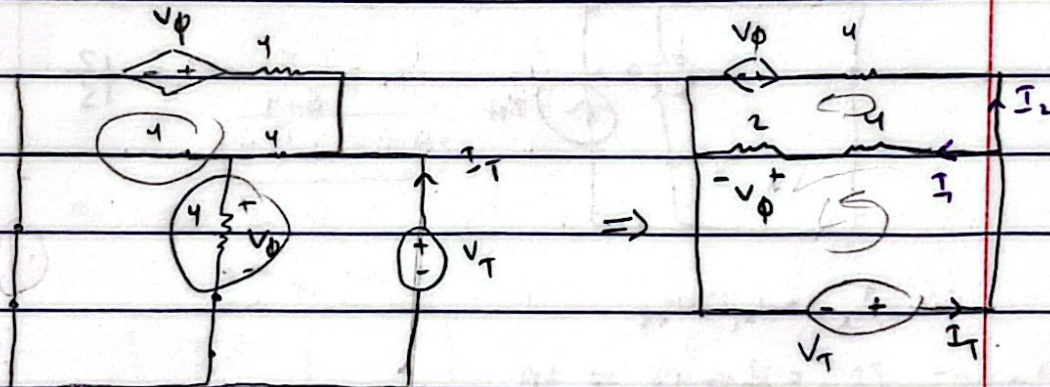
$$\therefore V_{o.c} = V_{Th} + 80$$

$$= 10 \times 4 + 80 = 120 \text{ V}$$

$$\Rightarrow R_{Th} = \frac{V_{o.c}}{I_{s.c}} = \underline{120}$$

$$\Rightarrow R_{Th} = \frac{V_T}{I_T}$$

all indep. sources set to zero.



in parallel
so same V_ϕ

$$\therefore V_\phi = \frac{2}{2+4} V_T = \frac{2}{6} V_T$$

$$\text{let } V_T = 6 \text{ V}, \therefore V_\phi = 2$$

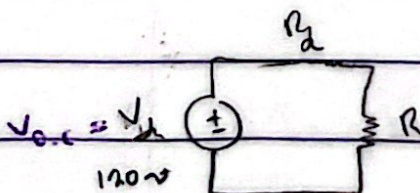
$$\therefore I_T = I_1 + I_2$$

التيار المتدفق في المقاوم
من طريق V_ϕ على R

$$\begin{aligned} &= \frac{V_T}{6} + \frac{(V_T - V_\phi)}{4} \\ &= \frac{6}{6} + \frac{6-2}{4} \\ &= 1 + 1 = \underline{2 \text{ A}} \end{aligned}$$

$$\therefore R_{Th} = \frac{V_T}{I_T} = \frac{6}{2} = 3 \Omega$$

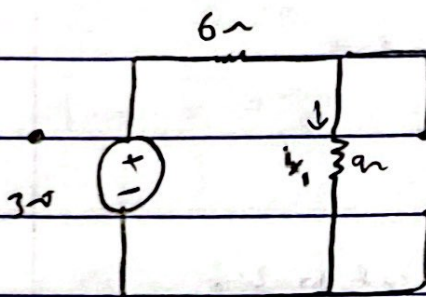
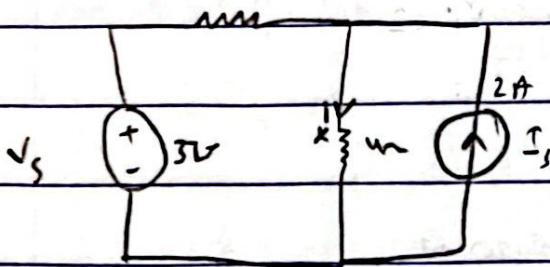
$$\therefore P_{max} = \frac{V^2}{R} = \frac{60^2}{3} = 1.2 \text{ kW}$$



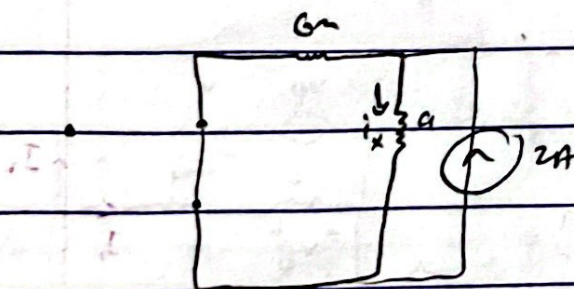
4.13

de super position.

Ex:

Find i_x due to V_s .

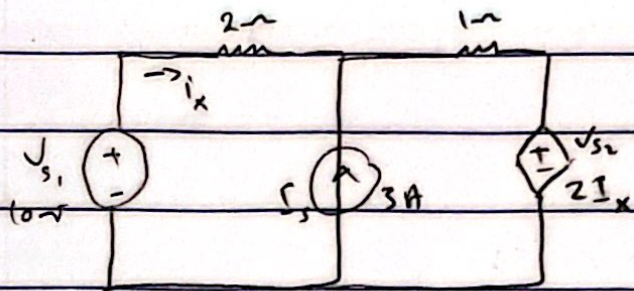
$$i_{x1} = \frac{3}{6+9} = \frac{3}{15} = \frac{1}{5} \text{ A.}$$



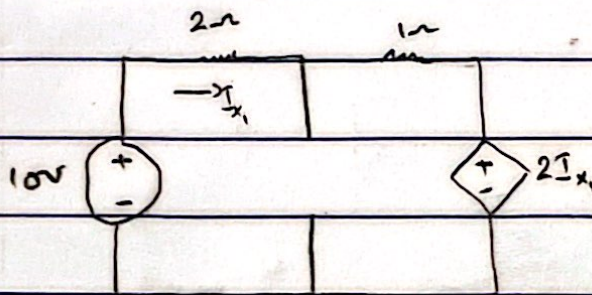
$$i_{x2} = \frac{6}{6+9} \times 2 = \frac{12}{15}$$

$$\begin{aligned} i_x &= i_{x1} + i_{x2} \\ &= \frac{3}{15} + \frac{12}{15} = 1 \text{ A.} \end{aligned}$$

Ex:-



• I_{x1} due to V_{s1} :-

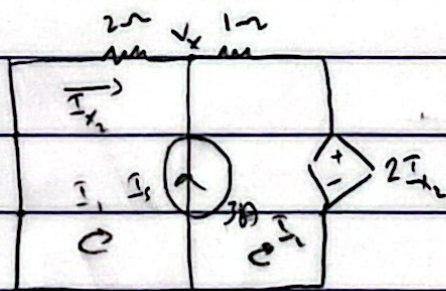


$$KVL \Rightarrow -10 + 2I_{x1} + 1I_{x1} + 2I_{x1} = 0$$

$$10 = 5I_{x1}$$

$$\Rightarrow I_{x1} = 2A$$

• I_{x2} due to V_{s2} :-



• mesh:-

$$2I_1 + 1I_2 + 2I_1 = 0 \Rightarrow 4I_1 + I_2 = 0$$

$$I_2 - I_1 = 3A$$

$$4I_1 + 3 + I_1 = 0$$

$$5I_1 + 3 = 0$$

$$\Rightarrow I_1 = \frac{-3}{5} = -0.6A$$

$$I_x = -\frac{V_x}{2}, \quad \frac{V_x}{2} - 3A + \frac{V_x - 2I_x}{1} = 0$$

$$\Rightarrow I_{x2} = -0.6A \quad \frac{V_x}{2} - 3 + \frac{V_x + 2 \cdot \frac{V_x}{2}}{1} = 0$$

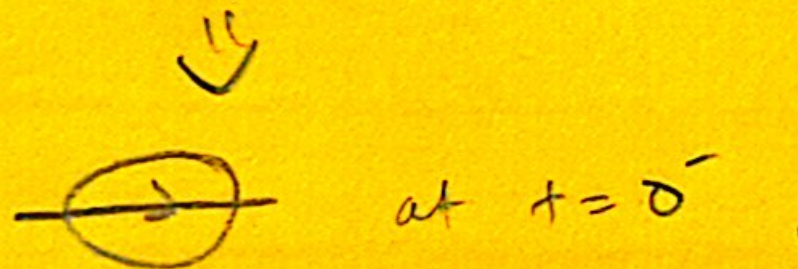
$$\frac{V_x}{2} - 3 + 2V_x = 0 \Rightarrow V_x = 1.2V$$

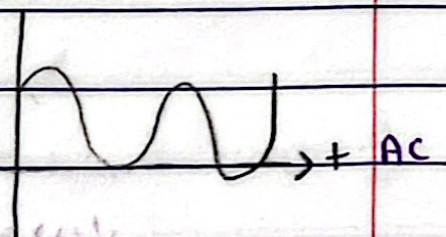
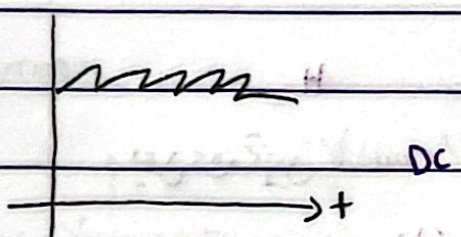
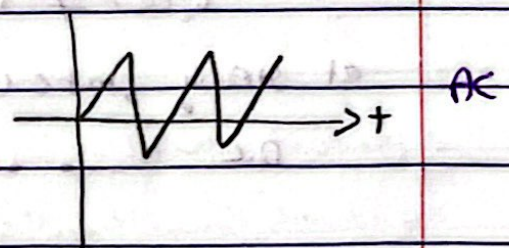
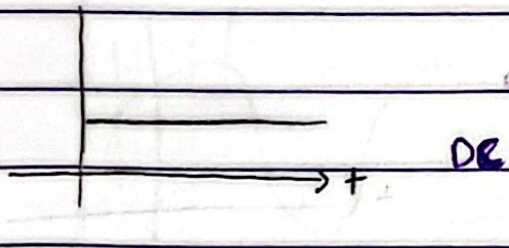
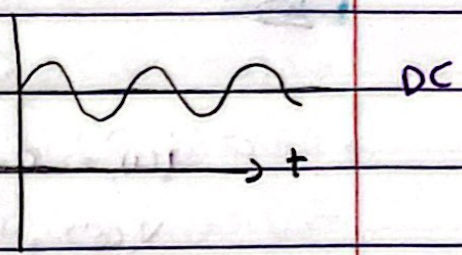
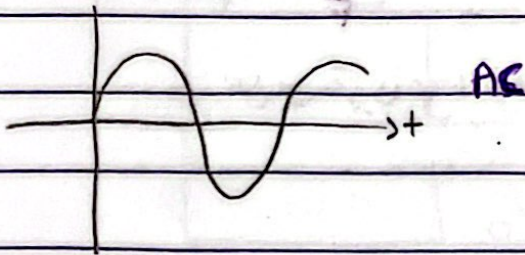
$$\therefore I_x = I_{x1} + I_{x2} = 2 - 0.6 = \underline{\underline{1.4A}}$$

- $V_c(0^-) = 10 \text{ V.}$



- $i(0^-) = 1 \text{ A}$

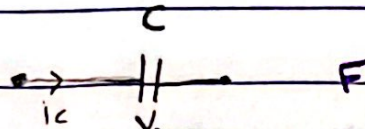




DC:- just positive or negative only

AC:- positive and negative

DC



یہ دیکھ کر یہی فرق پڑتا ہے

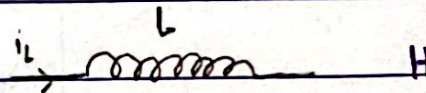
$$i_c(t) = C \frac{dV_c(t)}{dt}$$

$$V_c(0^-) = V_c(0^+)$$

$$i_c(0^-) \neq i_c(0^+)$$

at steady state ($t \rightarrow \infty$)

D.C



یہ دیکھ کر یہی فرق پڑتا ہے

$$V_L(t) = L \frac{di_L(t)}{dt}$$

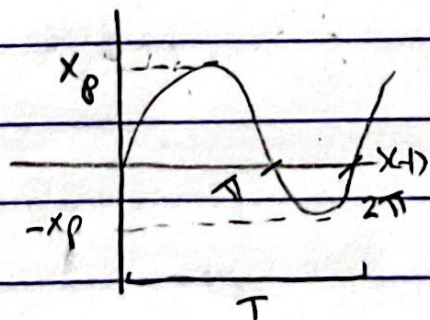
$$i_L(0^-) = i_L(0^+)$$

$$V_L(0^-) \neq V_L(0^+)$$

at steady state ($t \rightarrow \infty$)

S.C

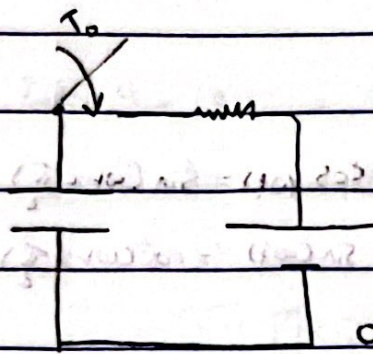
AC



$$f = \frac{1}{T}$$

$$\omega = 2\pi f \text{ rad/sec}$$

H₂



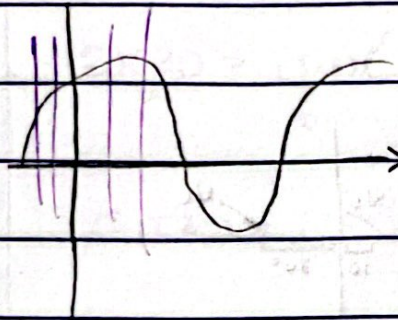
كافة العناصر المتصلة $t=0^+$

قبل انغلاق المفتاح $t=0^-$

في حالة اني C لم تكن مشحونة

يكون الجهد المخزن لها كفة $0^+ = 0^-$

ديسري 0 لانه غير مشحون

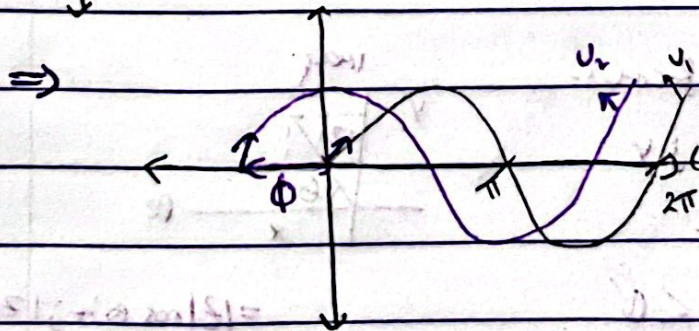
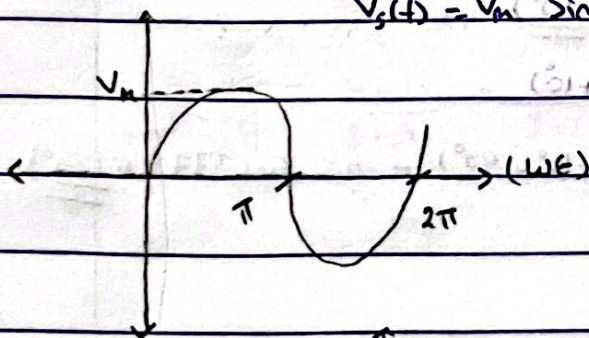


وكانا تكون صفة الموجة

\sin or \cos حسب الجور العاصوبي

Chapter (9):-

$$V_s(t) = V_m \sin(\omega t)$$



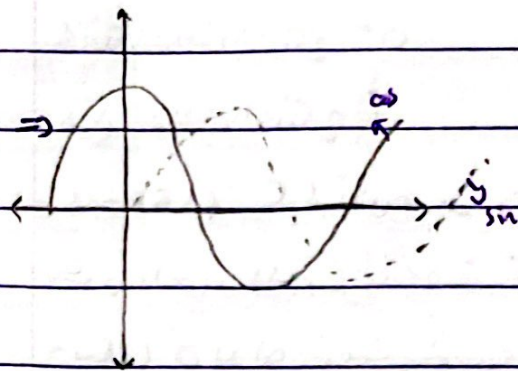
Leads

lags

$$V_1(t) = V_m \sin(\omega t)$$

$$V_2(t) = V_m \sin(\omega t + \phi)$$

$V_2(t)$ leads $V_1(t)$ by ϕ



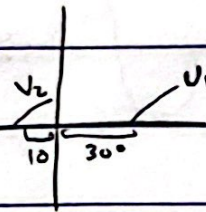
$$\cos(\omega t) = \sin(\omega t + \frac{\pi}{2})$$

$$\sin(\omega t) = \cos(\omega t - \frac{\pi}{2})$$

$$\Rightarrow V_1(t) = 10 \sin(5t - 30^\circ)$$

$$V_2(t) = 15 \sin(5t + 10^\circ)$$

$\therefore V_2(t)$ leads $V_1(t)$ by 40° .



$$\Rightarrow i_1(t) = 2 \sin(377t + 45^\circ)$$

$$i_2(t) = 0.5 \cos(377t + 10^\circ)$$

$$= 0.5 \sin(377t + 10^\circ + 90^\circ) = 0.5 \sin(377t + 100^\circ)$$

$\therefore i_2(t)$ leads $i_1(t)$.

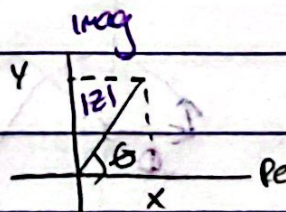
• Rectangular form:-

$$Z = x + jy$$

• Polar form:-

$$Z = |Z| \angle \theta$$

$$= \sqrt{x^2 + y^2} \angle \tan^{-1} \frac{y}{x}$$



$$= |Z| \cos \theta + j |Z| \sin \theta$$

$$\bullet |Z| e^{j\theta}$$

$$e^{j\theta} = \cos \theta + j \sin \theta$$

$$Z_1 = 4 + j3 = 5 \angle 36.9^\circ$$

$$Z_2 = 3 + j4 = 5 \angle 53.1^\circ$$

$$\rightarrow Z = 9 + j4 = 9.84 \angle 23.96^\circ$$

$$\Rightarrow \boxed{P} \boxed{O} \boxed{I} \boxed{X} \boxed{G} \boxed{Y} \boxed{I} \boxed{F} \quad , \text{ RCL F to find } \theta$$

(9, 4)

$$\bullet \quad (Z_1)(Z_2) = (5 \angle 36.9^\circ)(5 \angle 53.1^\circ)$$

or

$$(Z_1)(Z_2) = (4 + j3)(3 + j4) \quad \cdot \quad \boxed{j \cdot j = -1}$$

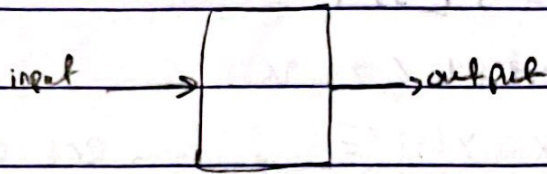
\Rightarrow save as i in defocushel

$$\bullet \quad \frac{Z_1}{Z_2} = \left(\frac{1}{5}\right) \angle 36.9^\circ - 53.1^\circ$$

or

$$\frac{Z_1}{Z_2} = \frac{4 + j3}{3 + j4} \cdot \frac{3 - j4}{3 - j4}$$

phasors:-



$$P_{in} = P_{out}$$

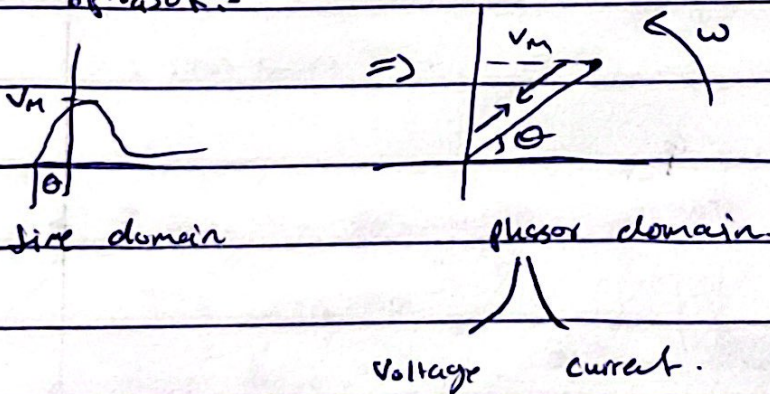
$$\omega_{in} = \omega_{out}$$

|| / < θ who get change.

phase shift \rightarrow in phase

out of phase

phasor:-



let $i(t) = 6 \cos(50t - 40^\circ)$ A (time domain)

$\vec{I} = 6 \angle -40^\circ$ A (phasor)

let $v(t) = -4 \sin(30t + 50^\circ)$ V

$= 4 \cos(30t + 140^\circ)$ V

$\vec{V} = 4 \angle 140^\circ$ V

ازالة اسباب لتبني

$-4 \cos(30t + 50^\circ - 90^\circ)$

$= 4 \cos(30t - 40^\circ)$ after shift to cosine $(+180^\circ)$

$$i\vec{V}_x = 10 \angle 120^\circ \sqrt{}$$

$$f = 50 \text{ Hz}$$

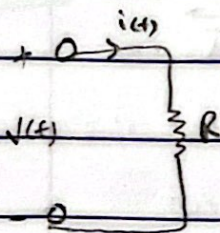
$$10 \cos(50(2\pi)t + 120^\circ) \sqrt{}$$

Phasor relationships for circuit element.

Resistor:-

Time Domain:-

Phasor domain:-



$$v(t) = i(t)R$$

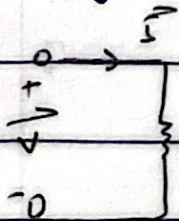
$$V_m e^{j(\omega t + \theta_v)} = I_m e^{j(\omega t + \theta_i)} R$$

$$V_m e^{j\theta_v} = I_m e^{j\theta_i} R$$

$$V_m \angle \theta_v = I_m \angle \theta_i R$$

$$\vec{V} = \vec{I} \cdot R$$

Phasor domain:-

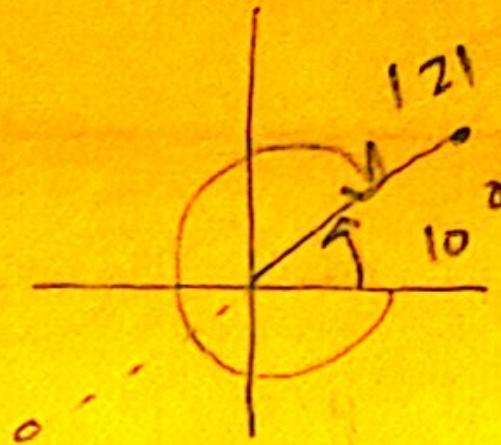


$$|G_v = G_r|$$

Voltage and current are in phase.

$$2 \cos(\omega t + 10^\circ)$$

$$2 \cos(\omega t - 350^\circ)$$

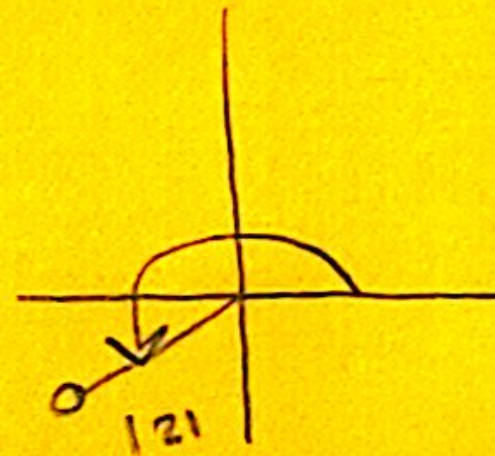


$$\begin{aligned} & -2 \cos(\omega t + 10^\circ) \\ & +180^\circ \\ & \rightarrow 2 \cos(\omega t + 190^\circ) \end{aligned}$$

$$e^{j\theta} = \cos \theta + j \sin \theta$$

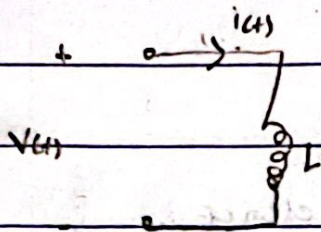
$$v = \cos(\omega t + \theta_v)$$

$$V_m e^{j(\omega t + \theta_v)}$$



Inductor:-

Time domain:-



$$v(t) = L \frac{di(t)}{dt}$$

$$V_m e^{j(\omega t + \theta)} = L \frac{d}{dt} (I_m e^{j(\omega t + \phi)})$$

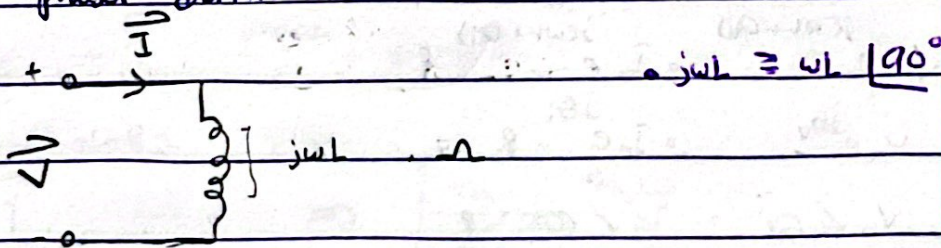
$$V_m e^{j(\omega t + \theta)} = L I_m (j\omega) e^{j(\omega t + \phi)}$$

$$V_m e^{j\theta} = L I_m (j\omega) e^{j\phi}$$

$$V_m e^{j\theta} = (j\omega L) I_m e^{j\phi}$$

$$\vec{V} = (j\omega L) \vec{I}$$

Phasor domain

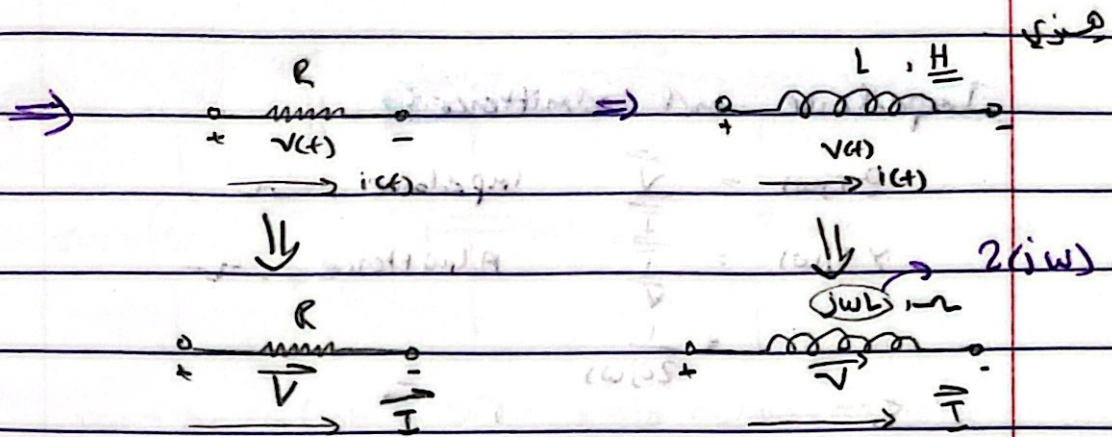


$$(V_m \angle \theta_v) = (j\omega L)(I_m \angle \theta_i)$$

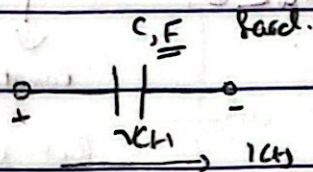
$$\theta_v = \theta_i + 90^\circ$$

• i lags v by 90°

• v leads i by 90°



capacitor:-



Time domain.

$$i(t) = C \frac{d v(t)}{dt}$$

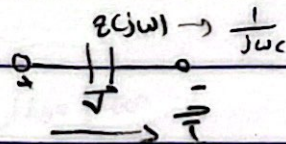
$$I_m e^{j(\omega t + \theta_i)} = C \frac{d}{dt} V_m e^{j(\omega t + \theta_v)}$$

$$I_m e^{j\theta_i} = C V_m j\omega e^{j\theta_v}$$

$$\underline{I} = j\omega C \underline{V}$$

$$\underline{I} = \frac{\underline{V}}{j\omega C} = \frac{-j}{\omega C} \underline{V}$$

phasor domain:-



$$\underline{V} = \left(-\frac{j}{\omega C} \right) \underline{I}$$

$$\theta_v = \theta_i + 90^\circ$$

$$\theta_i = \theta_v - 90^\circ$$

• i leads v by 90° .

• v lags i by 90° .

Impedance and admittance:

$$Z(j\omega) = \frac{\vec{V}}{\vec{I}} \quad \text{Impedance, } \Omega$$

$$Y(j\omega) = \frac{\vec{I}}{\vec{V}} \quad \text{Admittance, } \text{S}$$

$$= \frac{1}{Z(j\omega)}$$

$$\rightarrow Z(j\omega) = \frac{\vec{V}}{\vec{I}} = \frac{V_m \angle \theta_v}{I_m \angle \theta_i} = \frac{V_m}{I_m} \angle (\theta_v - \theta_i)$$

R, L, C just do physics.

$$R + jX$$

complex

$$= R + jX$$

But Not A phasor!!!

$$\begin{array}{c} R + jX \\ \downarrow \quad \swarrow \searrow \\ R \quad C \quad L \\ -V \quad +V \end{array}$$

$$\rightarrow Z(j\omega) = \frac{\vec{V}}{\vec{I}} = \frac{V_m \angle \theta_v}{I_m \angle \theta_i} = R + jX$$

R = Resistive part.

X = Reactive part.

$$\rightarrow Z(j\omega) = |Z| \angle \theta_z$$

$$= R + jX$$

$$|Z(j\omega)| = \sqrt{R^2 + X^2}$$

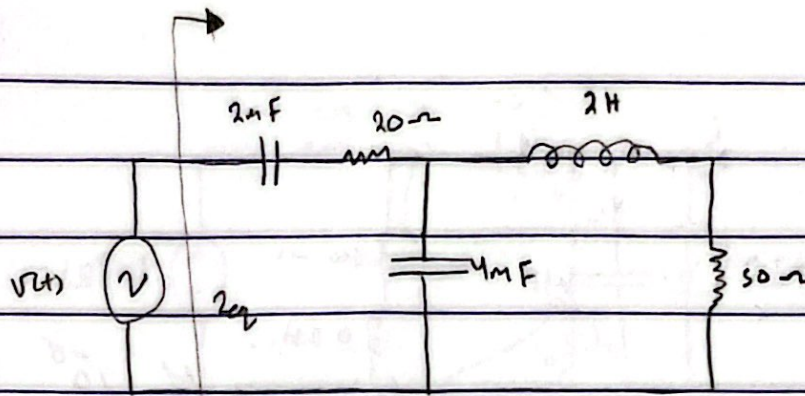
$$\theta_z = \tan^{-1} \frac{X}{R}$$

$$R = |Z| \cos \theta_z$$

$$X = |Z| \sin \theta_z$$

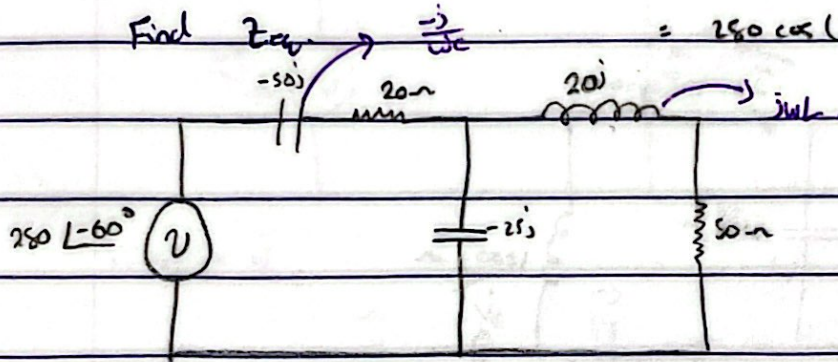
$$\text{OP } \theta_z = \theta_v - \theta_i$$

Ex:-



$$v(t) = 280 \sin(10t + 30^\circ) = 280 \cos(10t + 30 - 90)$$

$$\text{Find } Z_{eq} \rightarrow \frac{-j}{\omega C} = 280 \cos(10t - 60^\circ)$$

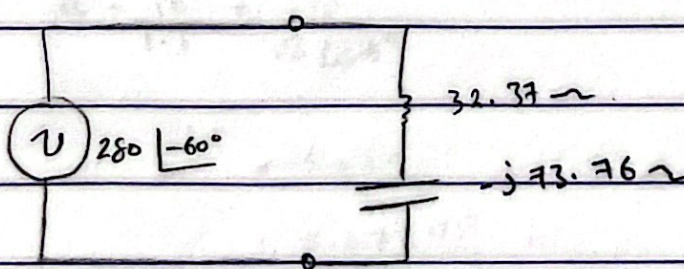


$$Z_{eq} = (50 + j20) // (-j25) + (20 - j40)$$

$$= \left[\frac{500 - 1250j}{50 - 5j} \right] + (20 - j40)$$

$$= \left(\frac{1346.29 \angle -68.2^\circ}{50.249 \angle -5.71^\circ} \right) + (20 - j40)$$

$$= 32.37^\circ - j73.76 \Omega$$

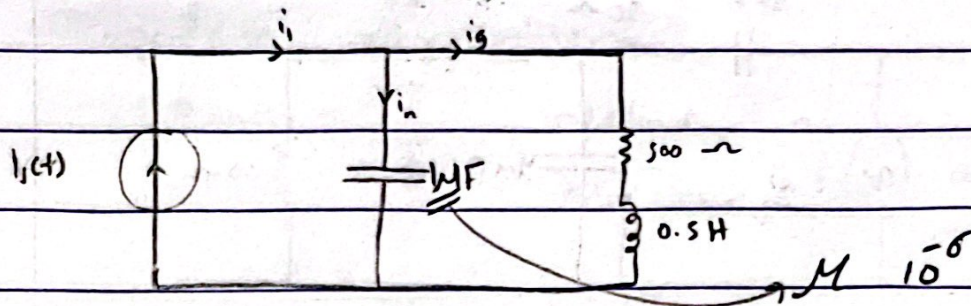


$$\frac{1}{\omega C} = 73.76$$

$$\frac{1}{10C} = 73.76$$

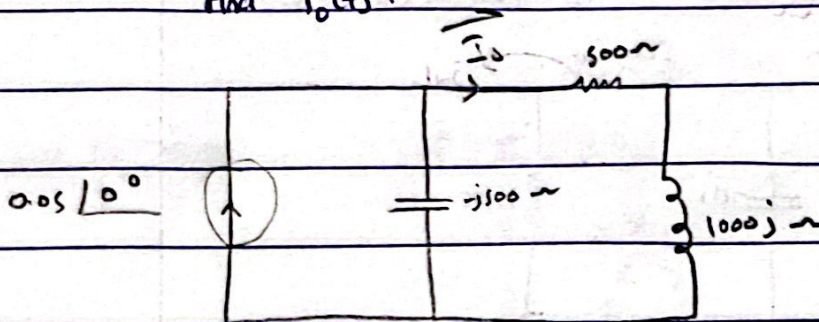
$$C = \frac{1}{737.6} \text{ F}$$

Ex:-



if $i_1(t) = 0.05 \cos(2000t) \text{ A}$

Find $i_o(t)$.



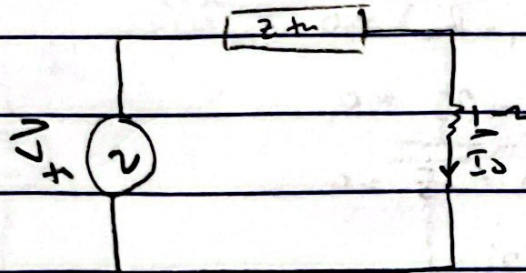
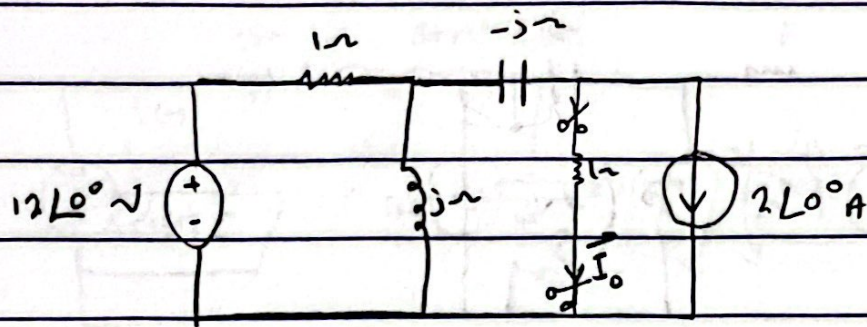
$$\vec{I}_o = \frac{-500j}{j1000 + 500 - 500j} \cdot (0.05)$$

$$= \frac{-500j}{500j + 500} \cdot (0.05)$$

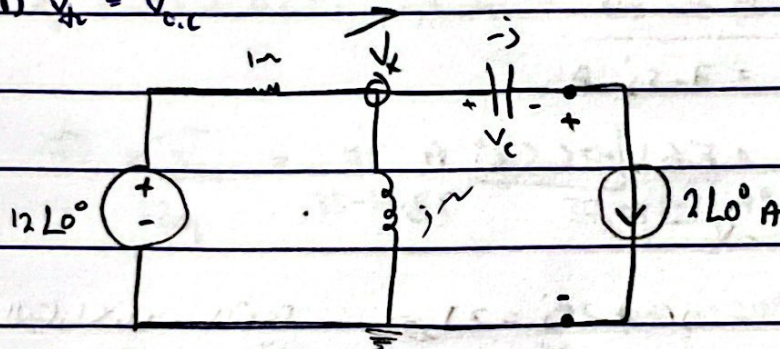
$$= 0.03535 \angle -135^\circ \text{ A}$$

$$i_o(t) = 0.03535 \cos(2000t - 135^\circ) \text{ A}$$

Ex:-



1) $V_{A_2} = V_{O_2}$



Nodal:-

$$\frac{\vec{V}_x - 12}{1} + \frac{\vec{V}_x}{j} + 2 = 0$$

$$\vec{V}_x (1 - j) = 10$$

$$V_x = \frac{10}{1 - j} = \frac{10}{\sqrt{2} \angle -45^\circ}$$

$$= 5 + j5$$

$$= 7.07 \angle 45^\circ \text{ V}$$

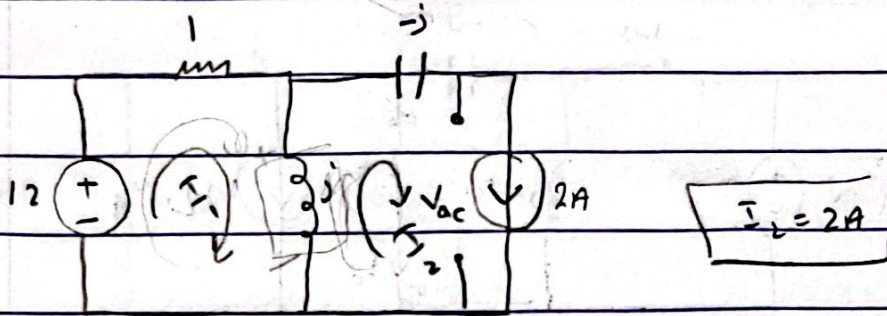
$$V_{A_2} = V_{O_2} = V_x - V_C$$

$$= 5 + j5 - (2)(-j)$$

$$= 5 + 7j$$

$$= 8.6 \angle 54.46^\circ \text{ Volt}$$

Mesh



$$\rightarrow -12 + I_1 + j(I_1 - 2) = 0$$

$$-12 + I_1 + jI_1 - 2j = 0$$

$$-12 + I_1(j+1) - 2j = 0$$

$$\therefore I_1 = \frac{12 + 2j}{1+j}$$

$$= 7 - 5j \text{ A}$$

$$= 8.6 \angle -35.53^\circ \text{ A}$$

$$V_{bc} = V_j - V_c$$

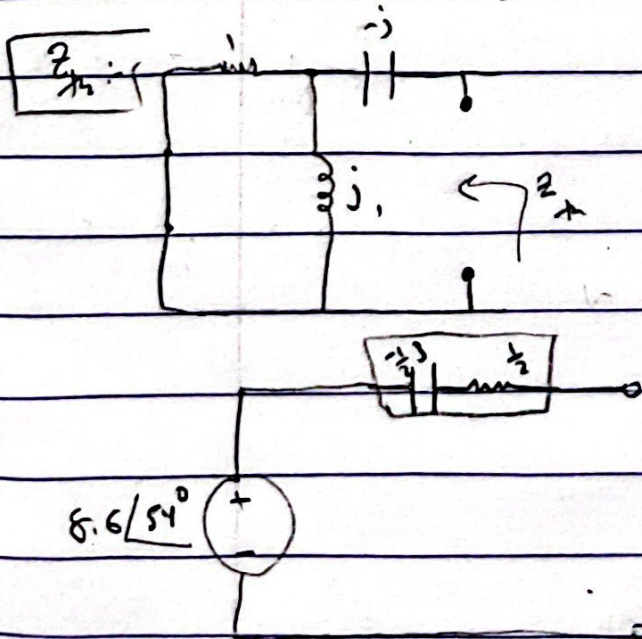
$$= 2j + j(7 - 5j - 2)$$

$$= 2j + j(5 - 5j)$$

$$= 2j + 5j + 5$$

$$= 5 + 7j \text{ Volt}$$

(5W) - (10W) = 5W
super mesh.



$$Z_{th} = (1/j) - j$$

$$= \frac{j}{j+1} - j$$

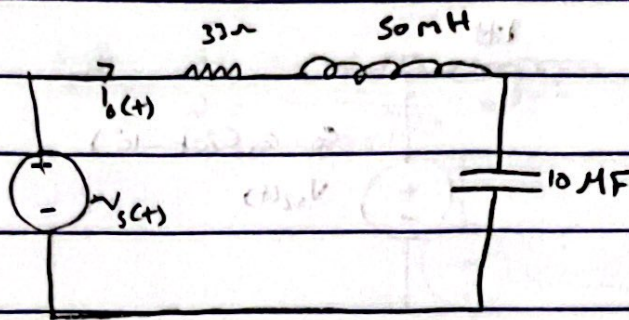
$$= \frac{1}{\sqrt{2}} \angle 90^\circ - j$$

$$= \frac{1}{\sqrt{2}} \angle 45^\circ - j$$

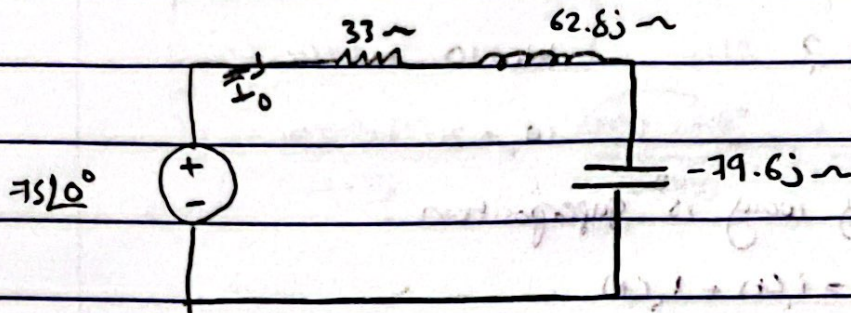
$$= \frac{1}{2} + \frac{1}{2}j - j$$

$$= \frac{1}{2} - \frac{1}{2}j$$

Ex:-



$$v_s(t) = 75 \cos(400\pi t)$$



$$H = 10^{-6}$$

$$Z_{in} = 33 + 62.8j - 79.6j = 33 - 16.8j \quad \text{complex}$$

$$\vec{I}_0 = \frac{\vec{V}_s}{Z_{eq}} = \frac{75}{33 - 16.8j} = \frac{75 \angle 0^\circ}{37.03 \angle -26.9^\circ}$$

$$= \frac{75 \angle 0^\circ - (-27^\circ)}{37.03} = 2.03 \angle 27^\circ \text{ A}$$

I_0 leads \vec{V}_s by 27°

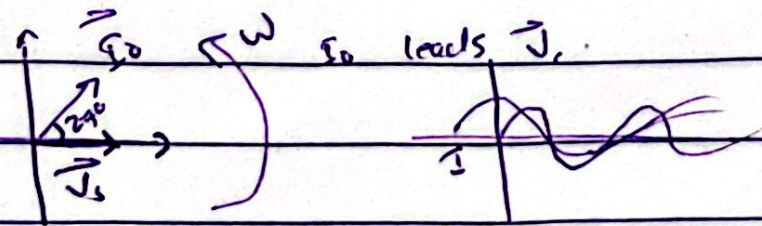
$$V_R = R I_0$$

$$= 33 \times 2.03 \angle 27^\circ$$

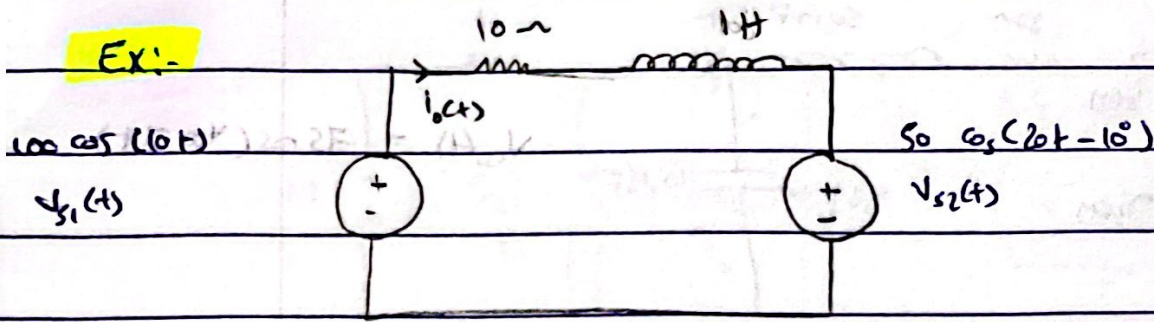
$$= 67 \angle 27^\circ \text{ V} \quad \angle \theta_v = \theta_i = 0^\circ$$

$$V_L = (62.8j) \vec{I}_0 = 127 \angle 117^\circ \text{ V} \Rightarrow \angle \theta_v - \theta_i = 117 - 27 = 90^\circ$$

$$V_C = 162 \angle -63^\circ \text{ V} \Rightarrow \angle \theta_v - \theta_i = -63 - 27 = -90^\circ$$



Ex:-



Find $i_o(t)$?

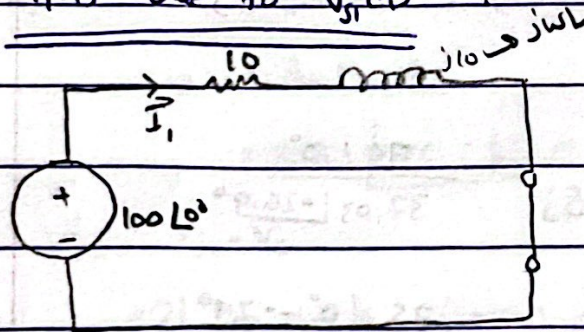
$$\omega_1 = 10 \text{ rad/sec}$$

$$\omega_2 = 20 \text{ rad/sec}$$

The only way is superposition.

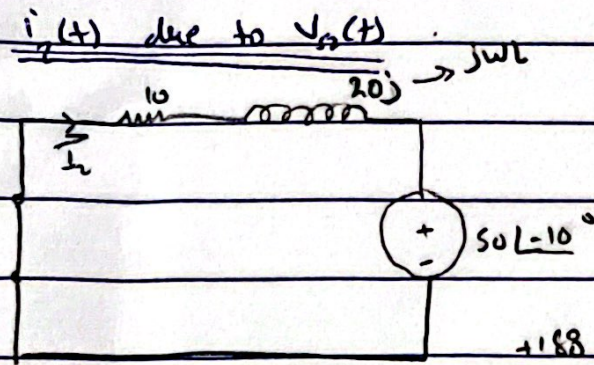
$$i_o(t) = i_1(t) + i_2(t)$$

$i_1(t)$ due to $v_{s1}(t)$



$$\vec{I}_1 = \frac{100 \angle 0^\circ}{10 + j0} = \frac{100 \angle 0^\circ}{14.14 \angle 45^\circ} = 7.07 \angle -45^\circ \text{ A}$$

$$i_1(t) = 7.07 \cos(10t - 45^\circ) \text{ A}$$



$$\vec{I}_2 = \frac{-V_A(t)}{10 + 10j} = \frac{50 \angle -10^\circ}{10 + 10j} = \frac{50 \angle 17^\circ}{10 + 20j}$$

$$= \frac{50 \angle 17^\circ}{22.36 \angle 63.43^\circ}$$

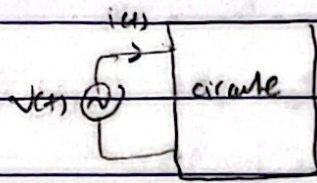
$$= 2.24 \angle 106.57^\circ \text{ A}$$

$$i_2(t) = 2.24 \cos(20t + 106.57^\circ) \text{ A}$$

$$i_2(t) = 7.07 \cos(10t - 45^\circ) + 2.24 \cos(20t + 106.57^\circ) \text{ A}$$

Chapter (02):-

Power Calculation.



$$V(t) = V_m \cos(\omega t + \theta_v)$$

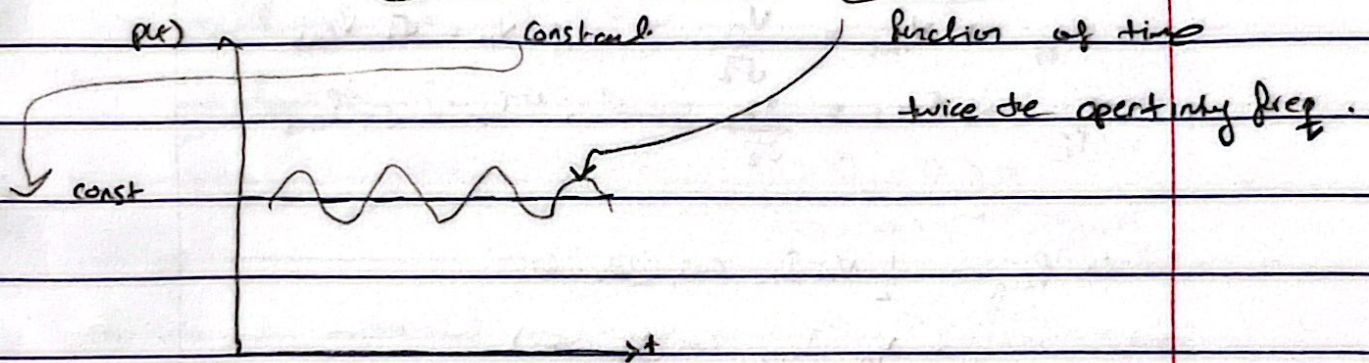
$$i(t) = I_m \cos(\omega t + \theta_i)$$

→ instantaneous power $p(t)$.

$$p(t) = V(t)i(t)$$

$$= V_m I_m \cos(\omega t + \theta_v) \cos(\omega t + \theta_i)$$

$$= \frac{1}{2} V_m I_m \cos(\theta_v - \theta_i) + \frac{1}{2} V_m I_m \cos(2\omega t + \theta_v + \theta_i)$$



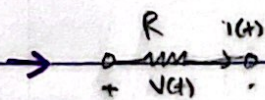
→ Average Power.

Real power.

$$P_{av} = \frac{1}{T} \int_0^T p(t) dt = \frac{1}{2} V_m I_m \cos(\theta_v - \theta_i)$$

$$\theta_v - \theta_i = \theta_z$$

$$\therefore P_{av} = \frac{1}{2} V_m I_m \cos(\theta_v - \theta_i) \quad \text{Watt}$$

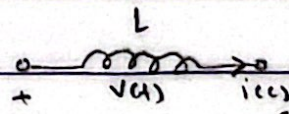


$$\theta_v - \theta_i = 0, \quad \theta_z = 0$$

$$\cos(\theta_v - \theta_i) = 1$$

$$\therefore P_{av} = \frac{1}{2} V_m I_m$$

$$= \frac{1}{2} \frac{V_m^2}{R} = \frac{1}{2} I_m^2 R$$

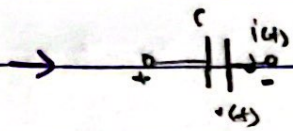


$$\theta_v - \theta_i = 90^\circ$$

$$\theta_z = 90^\circ \quad (\text{j}\omega L)$$

$$\cos(90^\circ) = 0$$

$$\therefore P_{av} = \text{zero}$$



$$\theta_v - \theta_i = -90^\circ$$

$$\theta_2 = -90^\circ \quad \left(\frac{-j}{\omega C}\right)$$

$$\cos(-90^\circ) = 0$$

$$P_{avg} = \text{zero}$$

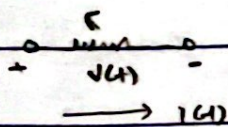
Effective of rms value.
root mean square.

$$V_{eff} = V_{rms} = \frac{V_m}{\sqrt{2}} \quad , \quad V_m = \sqrt{2} V_{rms}$$

$$I_{eff} = I_{rms} = \frac{I_m}{\sqrt{2}} \quad , \quad I_m = \sqrt{2} I_{rms}$$

$$P_{avg} = \frac{1}{2} V_m I_m \cos(\theta_v - \theta_i)$$

$$= V_{rms} I_{rms} \cos(\theta_v - \theta_i)$$



$$P_{avg} = V_{rms} I_{rms} \cos(0)$$

$$= V_{rms} I_{rms}$$

$$= \frac{V_{rms}^2}{R}$$

$$= I_{rms}^2 R$$

Apparent power and power factor.

$$P_{av} = \underbrace{V_{rms} I_{rms}}_{\text{Apparent power}} \underbrace{\cos(\theta_v - \theta_i)}_{\text{Power factor PF}}$$

$$P_a = \text{"VA"}$$

$$P_{av} = P_a P_f \quad \text{و } P_f = \frac{\text{الجزء الحقيقي}}{V_{rms} I_{rms}}$$

$$P_f = \cos(\theta_v - \theta_i)$$

→ P_f of R is 1 "unity P_f "

→ P_f of L is 0

→ P_f of C is 0

• $\theta_v > \theta_i \Rightarrow \theta_v - \theta_i > 0$
 $1 > \cos \theta > 0$ lagging PF

• $\theta_v < \theta_i \Rightarrow \theta_v - \theta_i < 0$
 $1 > \cos \theta > 0$ leading PF

• depends on the current.

Complex power \vec{S}

$$\vec{S} = \vec{V}_{rms} \cdot \vec{I}_{rms}^*$$

$$\vec{V}_{rms} = V_{rms} \angle \theta_v$$

$$\vec{S} = (V_{rms} \angle \theta_v) (I_{rms} \angle -\theta_i)$$

$$\vec{I}_{rms} = I_{rms} \angle \theta_i$$

$$\text{(Polar form)} = V_{rms} I_{rms} \angle \theta_v - \theta_i \quad \text{"VA"}$$

$$\text{(Rectangular form)} = \underbrace{V_{rms} I_{rms} \cos(\theta_v - \theta_i)}_{\text{Average power (W)}} + j \underbrace{V_{rms} I_{rms} \sin(\theta_v - \theta_i)}_{\text{Reactive Power (VAR)}}$$

Average power
(W)

Reactive Power
(VAR)

$$\vec{S} = P + jQ$$

W VAR

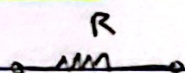
$$P_{av} = \text{Re} \{ \vec{S} \} \rightarrow Q = I_{rms} \int \vec{S} \cdot \vec{e}_z dz$$

$$P_{av} = V_{rms} I_{rms} \cos(\theta_v - \theta_i)$$

$$Q = j V_{rms} I_{rms} \sin(\theta_v - \theta_i)$$

$$\vec{S} = \sqrt{P_{av}^2 + Q^2} \angle \tan^{-1} \frac{Q}{P_{av}}$$

note:-



$$\theta_v - \theta_i = 0$$

$$\cos 0 = 1$$

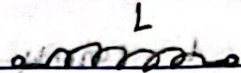
$$\sin 0 = 0$$

$$P_{av} = V_{rms} I_{rms}$$

$$Q = 0$$

$$P_{av} = \frac{V_{rms}^2}{R}$$

$$= I_{rms}^2 R$$



$$\theta_v - \theta_i = 90^\circ$$

$$\cos 90^\circ = 0$$

$$\sin 90^\circ = 1$$

$$P_{av} = 0$$

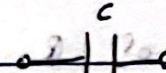
$$Q_L = V_{rms} I_{rms}$$

$$V_{rms} = (\omega L) I_{rms}$$

$$Q_L = (\omega L) I_{rms}^2$$

$$= \frac{V_{rms}^2}{\omega L}$$

$$\rightarrow X_L = \omega L$$



$$\theta_v - \theta_i = -90^\circ$$

$$\cos -90^\circ = 0$$

$$\sin (-90^\circ) = -1$$

$$P_{av} = 0$$

$$Q_C = -V_{rms} I_{rms}$$

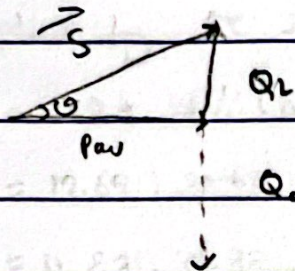
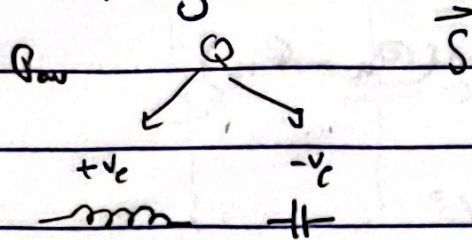
$$V_{rms} = \left(\frac{1}{\omega C} \right) I_{rms}$$

$$Q_C = -\frac{I_{rms}^2}{\omega C}$$

$$= -V_{rms}^2 (\omega C)$$

$$\rightarrow X_C = -\frac{1}{\omega C}$$

Power Triangle



$$\vec{S} = V_{rms} I_{rms} \angle \theta_v - \theta_i$$

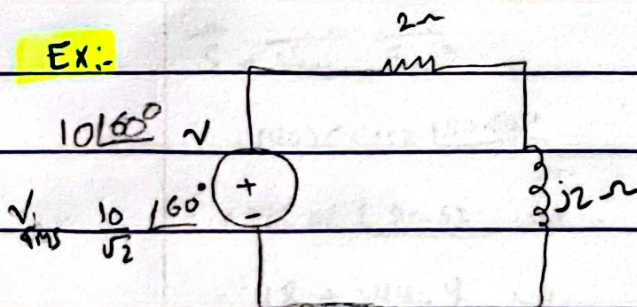
$$\cos \theta = \frac{P_{av}}{|\vec{S}|} = P.F$$

$$P_s = |\vec{S}| = \sqrt{P_{av}^2 + Q_c^2}$$

$$\tan \theta = \frac{Q_c}{P_{av}}$$

$$\theta = \tan^{-1} \frac{Q_c}{P_{av}}$$

Ex.:



Find the avg power absorbed by each element.

$$\vec{I}_{rms} = \frac{10/\sqrt{2} \angle 60^\circ}{2 + j2} = 2.5 \angle 15^\circ \text{ A}$$

$$P_{av \text{ del}} = V_{rms} I_{rms} \cos(\theta_v - \theta_i)$$

$$= \left(\frac{10}{\sqrt{2}}\right)(2.5) \cos(60^\circ - 15^\circ)$$

$$= 12.5 \text{ W}$$

$$|\vec{S}| = V_{rms} \vec{I}_{rms}^* = \left(\frac{10}{\sqrt{2}} \angle 60^\circ\right)(2.5 \angle -15^\circ)$$

$$= 12.5 + j12.5$$

$$P_{av} = 12.5 \text{ W}$$

$$Q_L = V_{rms,L} I_{rms,L} \sin(\theta_v - \theta_i)$$

$$\begin{aligned} \vec{V}_{rms} &= \frac{j2}{j2+2} \cdot \frac{10}{\sqrt{2}} \angle 60^\circ \\ &= -1.294 + j4.829 \\ &= 5 \angle 105^\circ \text{ V}_{rms} \end{aligned}$$

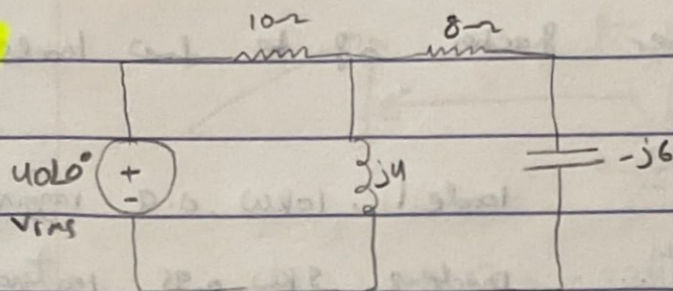
$$\begin{aligned} Q_L &= (5)(2.5) \sin(105-15) \\ &= 12.5 \text{ VAR} \end{aligned}$$

$$Q_L = I_{rms}^2 X_L$$

$$= (2.5)^2 (2)$$

$$= 12.5 \text{ VAR}$$

Ex:-



calculate the pf seen by the source and the avg power supplied by the source.

$$Z_{in} = 10 + j4 \parallel (8 - j6)$$

$$= 12.69 \angle 20.62^\circ \Omega$$

$$= 11.81 + j4.47 \Omega$$

$$\vec{I}_{rms} = \frac{40 \angle 0^\circ}{12.69 \angle 20.62^\circ} = 3.152 \angle -20.62^\circ \text{ A}$$

$$\vec{S} = \vec{V}_{rms} \vec{I}_{rms}^*$$

$$= (40)(3.152 \angle 20.62^\circ)$$

$$= 126.08 \angle 20.62^\circ \text{ VA}$$

$$= 118 + j44.4 \text{ VA}$$

$$P_{av} = \text{Re} \{ \vec{S} \} = 118 \text{ VA}$$

$$1) \text{ pf} = \cos \theta = \cos (\theta_v - \theta_i)$$

$$= \cos (\tan^{-1} \frac{44.4}{118})$$

too messy

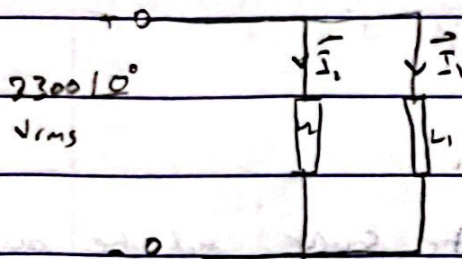
$$= \cos \tan^{-1} \left(\frac{44.4}{118} \right)$$

$$= 0.937 \text{ lagging}$$

$$2) \text{ pf} = \cos (\theta_v - \theta_i) = \cos (0 + 20.62^\circ) = 0.937^\circ \text{ lagging}$$

EX:-

Find the power factor of the two loads.



Load 1, 10kW, 0.9 lagging PF

Load 2, 5kW, 0.95 leading PF

Load 1 $P_{av} = 10 \text{ kW}$, PF = 0.9 lagging

$$P_{av} = V_{rms} I_{rms} \text{ P.F.}$$

$$10,000 = 2300 I_{rms} (0.9)$$

$$\therefore I_{rms} = 4.83 \text{ A}$$

$$\vec{I}_{rms} = 4.83 \angle -\cos^{-1} 0.9 \text{ A}$$

$$= 4.83 \angle -25.84^\circ \text{ A}$$

Load 2

$$I_{rms} = \frac{5000}{2300 \times 0.95} \angle \cos^{-1} 0.95$$

$$= 2.282 \angle 18.19^\circ \text{ Arms}$$

$$\vec{I}_{tot} = \vec{I}_{rms1} + \vec{I}_{rms2} = 6.78 \angle -12^\circ \text{ Arms}$$

$$\text{PF} = \cos(\theta_v - \theta_i)$$

$$= \cos(0 - (-12))$$

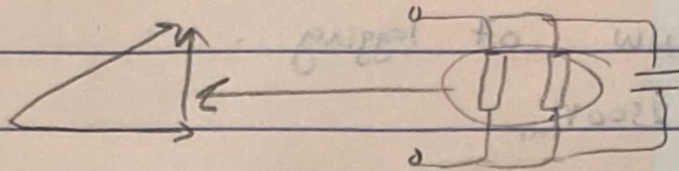
$$= 0.978 \text{ lagging}$$

$$\vec{V} = 2300 \angle 0^\circ$$

$$\vec{I} = 6.78 \angle -12^\circ$$

$$\vec{S} = (2300 \angle 0^\circ)(6.78 \angle -12^\circ)$$

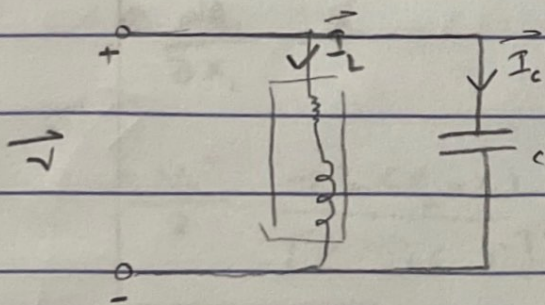
$$= 15253.23 + j3242.17$$



$$\Rightarrow Q_c = -3242.17 \text{ VAR.}$$

$$\begin{aligned} \vec{I}_{\text{rms}} &\Rightarrow \vec{S}_{\text{rea}} = \vec{I}_{\text{rms}}^* \vec{V}_{\text{rms}} \\ 15253.23 &= \vec{I}_{\text{rms}}^* (230 \angle 0^\circ) \\ \vec{I}_{\text{rms}}^* &= 6.63 \angle 0^\circ \\ \vec{I}_{\text{rms}} &= 6.63 \angle 0^\circ \end{aligned}$$

power factor correction:-



$$\text{PF} = \cos(\theta_v - \theta_i)$$

$$\underline{R} \text{ --- PF} = 1$$

$$Q_c = Q_{\text{ind}} - Q_{\text{int}}$$

$$\sqrt{\omega}$$

$$X_c = -\frac{Q_c}{\omega V_{\text{rms}}^2}$$

$$Q_c = \frac{V_{\text{rms}}^2}{X_c} = -\omega C V_{\text{rms}}^2$$

Ex:-

$$P = 1 \text{ MW} \quad 0.7 \text{ lagging}$$

$$V = 2300 \text{ V}_{\text{rms}}$$

45

$$C = ??$$

$$PF_{\text{new}} = 0.9 \text{ lagging}$$

page

$$\omega = 377 \text{ rad/sec}$$

المسألة

$$\tan \theta = \frac{Q}{P}$$

$$Q = P \tan \theta$$

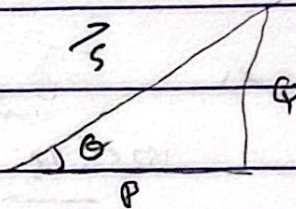
$$Q = P \tan \cos^{-1} PF$$

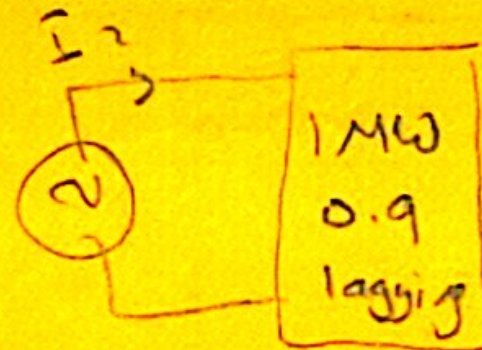
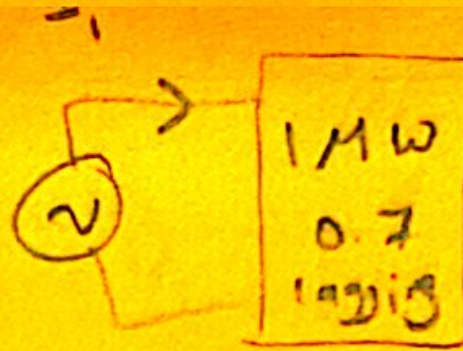
$$Q_{\text{init}} = (1 \times 10^6) \tan \cos^{-1} 0.7$$
$$= 1.02 \text{ MVAR}$$

$$Q_{\text{final}} = (1 \times 10^6) \tan \cos^{-1} 0.9$$
$$= 0.484 \text{ MVAR}$$

$$Q_c = Q_{\text{final}} - Q_{\text{init}}$$
$$= -0.536 \text{ MVAR}$$

$$C = \frac{-Q_c}{\omega V_{\text{rms}}^2} = 269 \text{ MF}$$





$$I_1 = \frac{P}{V \cos \phi} = \frac{10^6}{2300 \times 0.7} = 621 \text{ Arms}$$

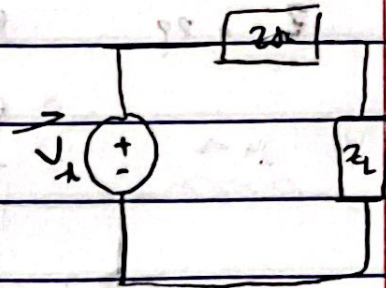
$$I_2 = \frac{10^6}{2300 \times 0.9} = 483 \text{ Arms}$$

Max power transfer:

$$Z_s = R_s + jX_s$$

$$Z_L = R_L + jX_L$$

$$P_{avg} = 0$$



$$I_s = \frac{V_s}{(R_s + R_L) + j(X_s + X_L)}$$

$$V_s = V_{rms} \angle 0^\circ$$

$$P_{av} = \frac{1}{2} I_s^2 R_L$$

$$= \frac{1}{2} \left(\frac{V_s}{\sqrt{(R_s + R_L)^2 + (X_s + X_L)^2}} \right)^2 R_L = \frac{1}{2} \frac{V_s^2 R_L}{(R_s + R_L)^2 + (X_s + X_L)^2}$$

$$\textcircled{1} \frac{\partial P_{av}}{\partial X_L} = 0$$

$$= \frac{V_s^2}{2} \frac{-2R_L(X_s + X_L)}{[(R_s + R_L)^2 + (X_s + X_L)^2]^2} = 0$$

$$X_L = -X_s$$

$$\textcircled{2} \frac{\partial P_{av}}{\partial R_L} = 0$$

$$= \frac{V_s^2}{2} \frac{(R_s + R_L)^2 + (X_s + X_L)^2 - 2R_L(R_s + R_L)}{[(R_s + R_L)^2 + (X_s + X_L)^2]^2} = 0$$

$$(R_s + R_L)^2 = 2R_L(R_s + R_L)$$

$$R_L = R_s$$

$$\therefore \text{for } P_{avg, \max} \rightarrow R_L = R_s$$

$$\rightarrow X_L = -X_s$$

$$Z_L = Z_s^*$$

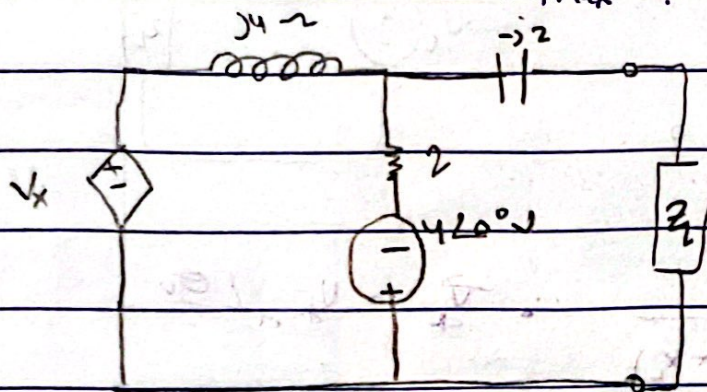
$$P_{avg, \max} = \frac{V_m^2}{8R_s} = \frac{V_{rms}^2}{4R_s}$$

Ex:-

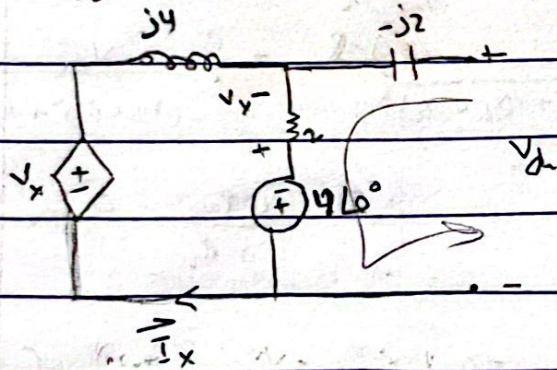
$Z_L = ??$

for $P_{av, max}$

$P_{av, max} = ?$



$V_{th} = V_{oc}$



to change from pol to rect

$\text{rect}(1.4) = X$

$\text{PCLF} = \theta$

$$\text{KVL} \Rightarrow -V_x + j4I_x + 2I_x - 4 = 0.$$

$$V_x = -2I_x$$

$$-4 + 2I_x + j4I_x + 2I_x = 0.$$

$$(4 + 4j)I_x = 4$$

$$I_x = \frac{4}{4 + 4j} = \frac{4}{5.656 \angle 45^\circ} = 0.707 \angle -45^\circ \text{ A.}$$

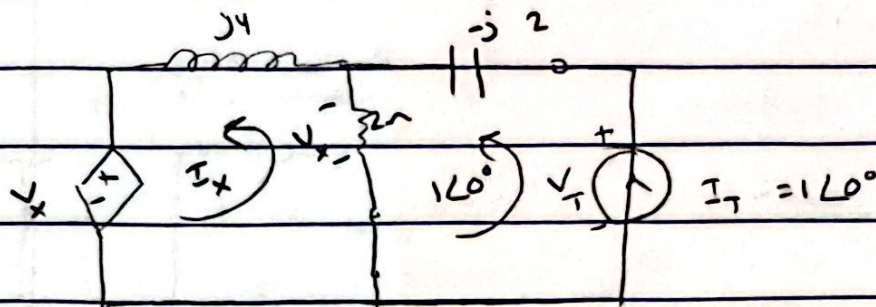
$$= 0.5 - 0.5j$$

$$\Rightarrow V_{th} = -2I_x - 4$$

$$= 2(\frac{1}{2} - \frac{j}{2}) - 4 = -3 - j$$

$$= 3.16 \angle -161.56^\circ \text{ V}$$

$$Z_{in} = \frac{V_T}{I_T} \quad \text{all indep set to 0.}$$



$$+V_x + 2(I_x - 1) + j4I_x = 0.$$

$$4(I_x - 1) + j4I_x = 0.$$

$$4I_x - 4 + j4I_x = 0.$$

$$(4 + j4)I_x = 4$$

$$I_x = 0.5 - 0.5j$$

$$\vec{V_T} \Rightarrow \underline{KVL} \quad -V_T - j2(1) + 2(1 - I_x) = 0$$

$$V_T = -2j + 2 - 2(\frac{1}{2} - \frac{1}{2}j)$$

$$= -2j + 2 - 1 + j$$

$$= 1 - j$$

$$Z_{in} = 1 - j$$

$$Z_L = Z_{in}^* = 1 + j$$

$$\Rightarrow P_{avg \max} = \frac{V_{rms}^2}{8 R_L} = \frac{(3.16)^2}{8(1)} = 1.25 \text{ W.}$$

$$I(t), V(t) = Ae^{st}$$

$$(L) \quad s = -\frac{R}{L}, \quad \tau = \frac{L}{R}$$

$$\bullet Ae^{\frac{-t}{\tau}}$$

• A from $t \rightarrow 0^+$

$$(C) \quad s = -\frac{1}{RC}, \quad \tau = RC$$

$$V(0^+) = V_s e^{\frac{-t}{\tau}}$$

general sol:-

$$x(t) = [x(0^+) - x(\infty)]e^{\frac{-t}{\tau}}$$

$$t \rightarrow \infty \quad L \Rightarrow \text{---} \text{---}$$

$$C \Rightarrow \text{---} \text{---}$$

$t \rightarrow 0^+$ - def. source

• V Value or I Value from $t < 0$.

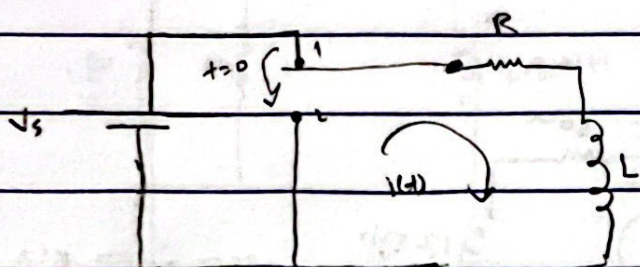
• Req from $t > 0$

• constant from $t = 0^+$

chapter (7):- Natural Response of 1st order circuits.

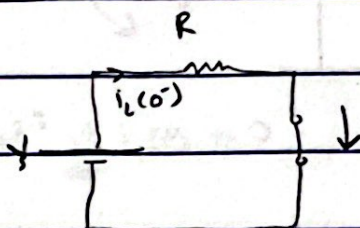
Ex 1.

find $i_L(t)$ of $t \geq 0$.



for $t < 0$

$$i_L(0^-) = \frac{V_s}{R}$$



for $t \geq 0$

$$R i_L(t) + L \frac{di_L(t)}{dt} = 0$$

$$i_L(t) = A e^{st}$$

$$\Rightarrow R A e^{st} + L A s e^{st} = 0$$

$$A e^{st} (R + Ls) = 0$$

$$s = -\frac{R}{L}$$

$$i_L(t) = A e^{-\frac{R}{L}t}, \quad t \geq 0$$

How to find A.

(A) from $t = 0^+$

$$i_L(0^+) = i_L(0^-) = \frac{V_s}{R}$$

$$\text{Sub in } i_L(t) = A e^{-\frac{R}{L}t} = \frac{V_s}{R}$$

$$A = \frac{V_s}{R}$$

$$i_L(t) = \frac{V_s}{R} e^{-\frac{R}{L}t}, \quad t \geq 0$$

$$\tau = \frac{L}{R} \quad \text{time constant}$$

$$i_L(t) = A e^{-\frac{t}{\tau}}$$

$0^- = 0^+$ عند التبدل

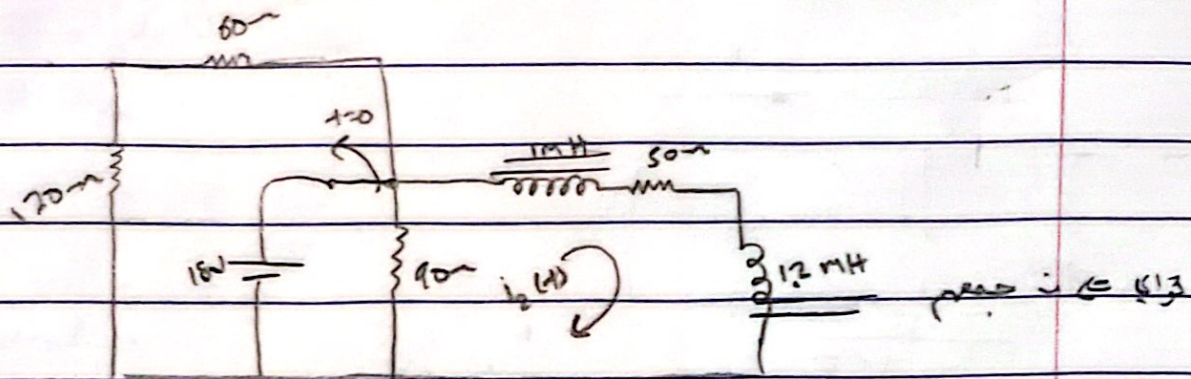
\neq الجهد

لأنه لا Voltage

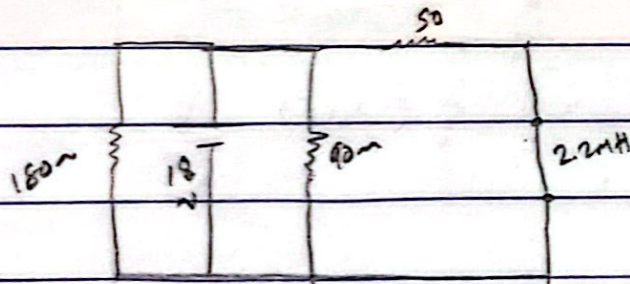
$0^- \neq 0^+$

Ex:

find $i_L(t)$ for $t > 0$

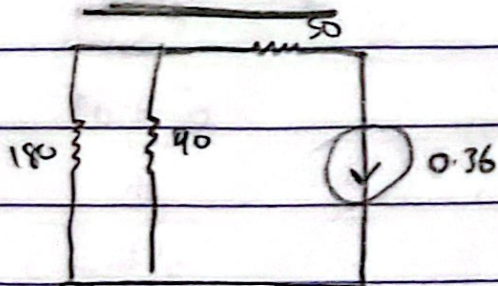


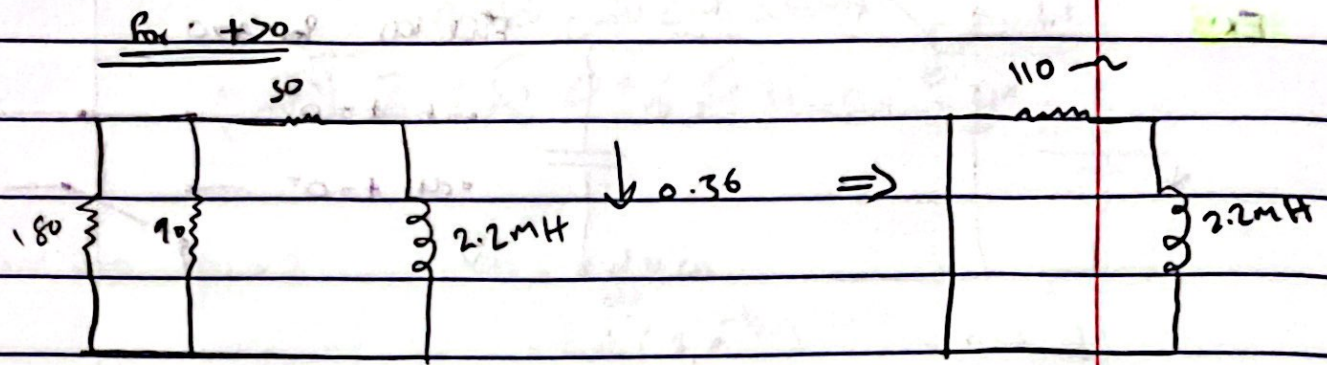
for $t < 0$



$$i_L(0^-) = \frac{18V}{50\Omega} = 0.36A$$

for $t = 0^+$





$$i_2(t) = ?$$

$$KVL \Rightarrow 110 i_2(t) + 2.2 \times 10^{-3} \frac{d i_2(t)}{dt} = 0$$

$$i_2(t) = A e^{st}$$

$$110 A e^{st} + 2.2 \times 10^{-3} A s e^{st} = 0$$

$$110 + 2.2 \times 10^{-3} s = 0$$

$$s = -\frac{110}{2.2 \times 10^{-3}}$$

OR

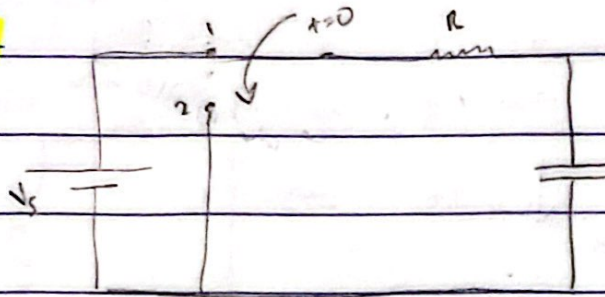
$$\tau = \frac{L}{R} = \frac{2.2 \text{ mH}}{110} = 20 \mu \text{ sec.}$$

$$i_2(t) = A e^{-\frac{t}{\tau}}$$

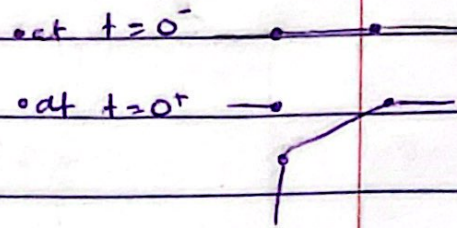
$$= 0.36 e^{-10000 t}$$

for $t > 0$

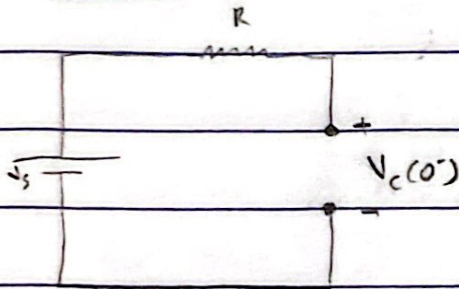
Ex:



Find $i(t)$ for $t > 0$.

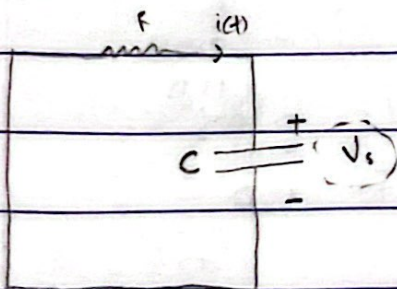


for $t < 0$



$$V_c(0^-) = V_s$$

for $t > 0$



$$i(t) = C \frac{dV_c(t)}{dt}$$

$$\text{KVL: } Ri(t) + V_c(t) = 0$$

$$RC \frac{dV_c(t)}{dt} + V_c(t) = 0$$

$$V_c(t) = Ae^{st}$$

$$T = RC, \quad S = -\frac{1}{RC}$$

$$\Rightarrow RCAs e^{st} + Ae^{st} = 0$$

$$Ae^{st}(RCs + 1) = 0$$

$$A = ? \Rightarrow t = 0^+$$

$$S = -\frac{1}{RC}$$

$$\text{at } t = 0^+ \Rightarrow V_c(0^+) = V_s$$

$$= V_c(0^+) = Ae^{\frac{-t}{RC}} = V_s$$

$$= Ae^0 = V_s \Rightarrow A = V_s$$

$$\therefore V_c(t) = V_s e^{\frac{-t}{RC}} \quad \text{forall } t > 0.$$

لما نتي [حدة σ^- بقى كانه لهن
ولكن كنهنا كونه σ^+ بكونه σ^- آخر

continue $\Rightarrow i(t) = ?$

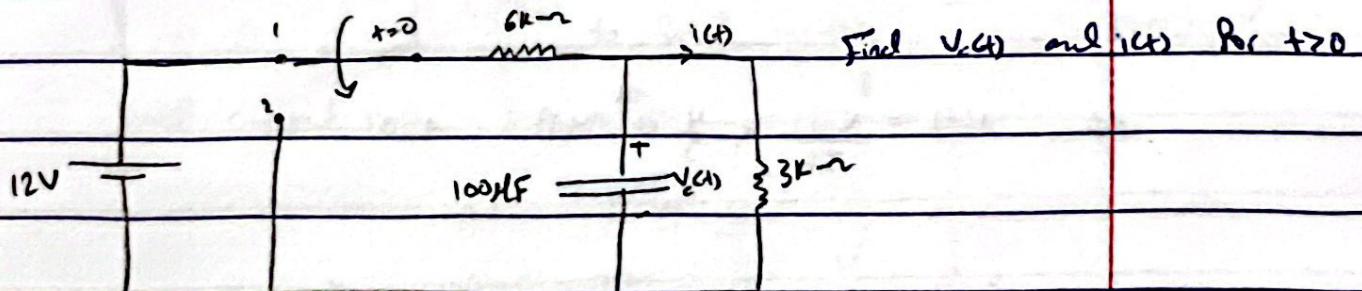
$$i(t) = C \frac{dV_c(t)}{dt}$$

$$= C \frac{d}{dt} \left(V_s e^{-t/RC} \right)$$

$$= \frac{-C V_s}{RC} e^{-t/RC}$$

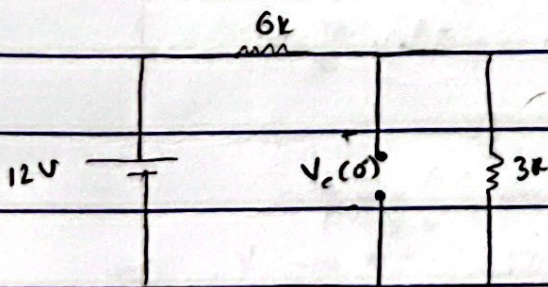
$$i(t) = \frac{-V_s}{R} e^{-t/RC}, t > 0$$

Ex:-



$$V_c(t) = A e^{-t/RC}, t > 0$$

for $t < 0$ (0)



$$V_c(0) = \frac{3}{3+6} \cdot 12 = 4 \text{ Volt.}$$

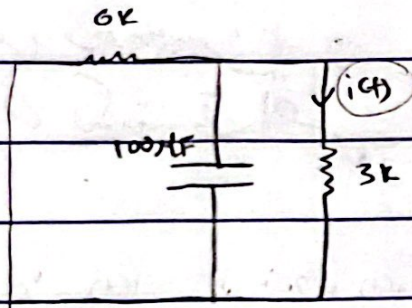
$$[V_c(0^-) = V_c(0^+) = 4 \text{ Volt.}]$$

for $t > 0$

$$\tau = R_{eq} C$$

$$C = 10 \mu F$$

$$R_{eq} = ?$$



$$R_{eq} = 3 \parallel 6 = 2k \Omega$$

$$\tau = 100 \times 10^{-6} \times 2 \times 10^3$$

$$= 0.2 \text{ sec.}$$

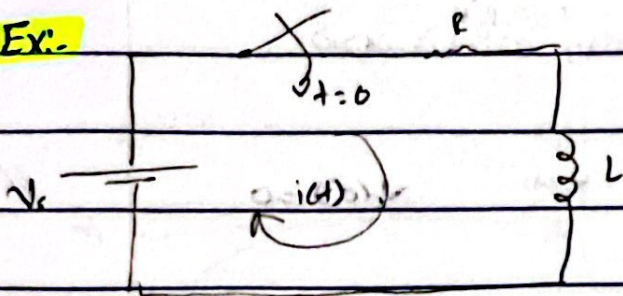
$$\Rightarrow V_c(t) = V_c(t) e^{-\frac{t}{\tau}}$$
$$= 4 e^{-5t}, t > 0$$

Calculation for the time constant exponent: $\frac{-1}{R_{eq}C} = \frac{-1}{2000 \times 10^{-6} \times 100} = -5$

$$\Rightarrow i(t) = \frac{V_c(t)}{3k} = \frac{4}{3} e^{-5t} \text{ mA}, t > 0$$

• Forced + Natural.
 \Rightarrow Step Response :-

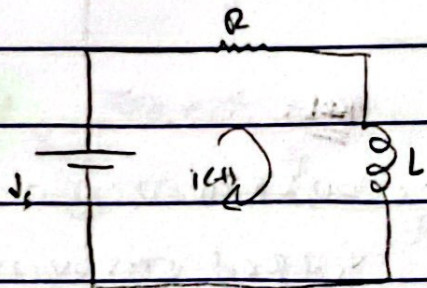
Ex:-



$$i(0^-) = 0$$

Find $i(t)$ for $t \geq 0$.

for $t \geq 0$



$$V_s = Ri(t) + L \frac{di(t)}{dt}$$

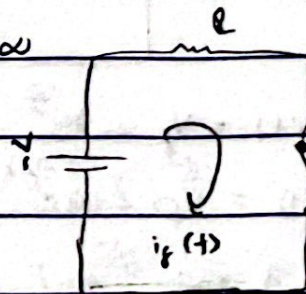
$$i(t) = i_n(t) + i_f(t)$$

natural forced.

to find $i_f(t)$:

constant

find current source from $t \rightarrow \infty$



$$\Rightarrow i(t) = \frac{V_s}{R} + Ae^{-\frac{t}{\tau}}$$

$$i_f(t) = \frac{V_s}{R}$$

Final Value

$$= \frac{V_s}{R} + Ae^{-\frac{t}{\tau}} \quad \tau = \frac{L}{R}$$

$$i(0^-) = i(0^+) = 0$$

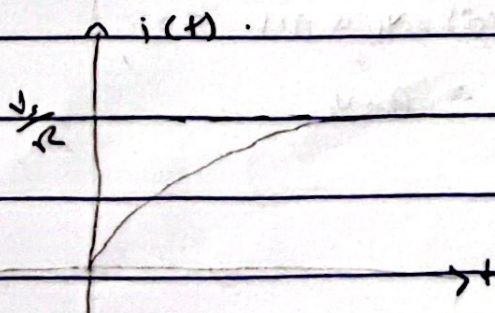
to find A: $t=0$

$$i(0^+) = \frac{V_s}{R} + A \cdot 1 = 0$$

$$= \frac{V_s}{R} + A = 0$$

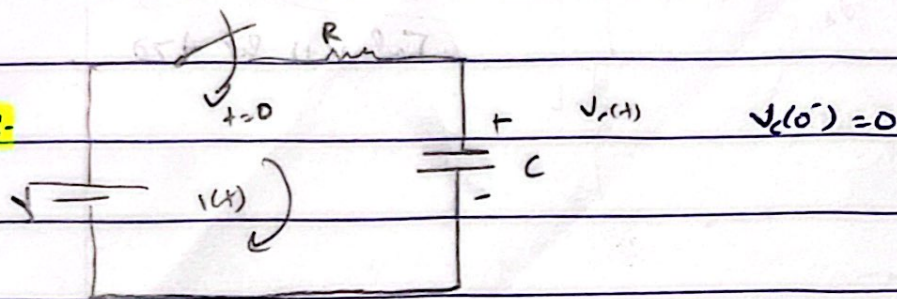
$$A = -\frac{V_s}{R}$$

$$\Rightarrow \frac{V_s}{R} - \frac{V_s}{R} e^{-\frac{t}{\tau}} \quad t \geq 0$$

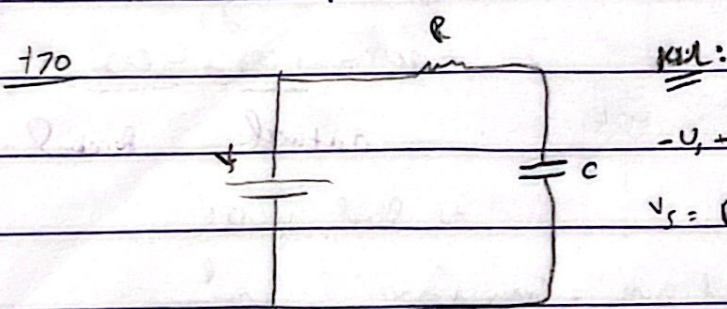


$$V_L(t) = L \frac{d}{dt} i(t) = L \left(\frac{V_s}{L} e^{-\frac{R}{L}t} \right) = V_s e^{-\frac{R}{L}t}, t > 0.$$

Ex:-



Find $i(t)$ for $t > 0$



KVL:

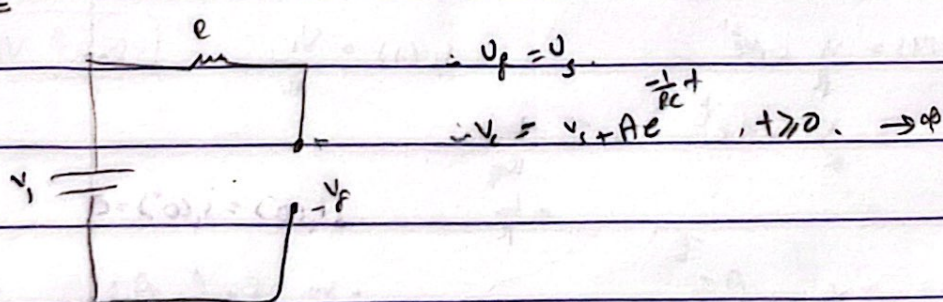
$$-V_s + R i(t) + V_c(t) = 0$$

$$V_s = R \left(\frac{d}{dt} V_c(t) \right) + V_c(t) = 0$$

$$V_c(t) = V_f + A e^{-\frac{t}{\tau}}, \quad \tau = RC$$

$$V_c(t) = V_f + A e^{-\frac{1}{RC}t}, \quad t > 0.$$

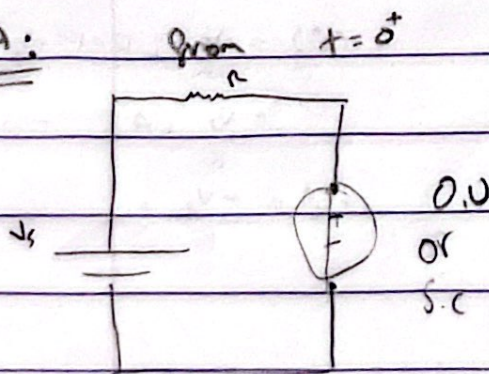
to find V_f : from $t \rightarrow \infty$.



$$V_f = V_s$$

$$V_c = V_s + A e^{-\frac{1}{RC}t}, \quad t > 0. \rightarrow \infty$$

to find A:



$$V_c(0^+) = 0 \quad \text{from S.C.}$$

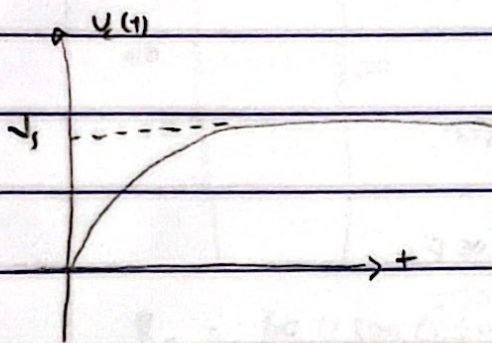
$t \rightarrow 0^+$ in eq. 6

$$V_c(0^+) = V_s + A(1) = 0$$

$$\therefore A = -V_s$$

$$V_c(t) = V_s - V_s e^{-\frac{1}{RC}t}, \quad t \geq 0$$

$$= V_s (1 - e^{-\frac{1}{RC}t}), \quad t \geq 0$$



$$i(t) = C \frac{d}{dt} V_c(t) = \frac{V_s}{R} e^{-\frac{1}{RC}t}, \quad t \geq 0$$

General Sol:-

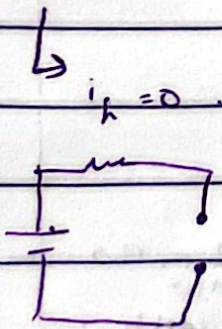
$$x(t) = x_p(\infty) + [x(0^+) - x_p(\infty)] e^{-t/\tau}$$

$$\tau = \frac{L}{R_{eq}} \quad \text{or} \quad \tau = R_{eq} C$$

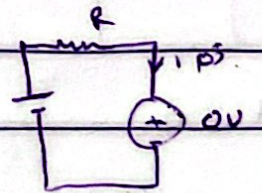
ex:- like the last circle:-

$$i(t) = i(\infty) + [i(0^+) - i(\infty)] e^{-t/\tau}$$

$$= I_f + [i(0^+) - I_f] e^{-t/\tau}$$



$$i(0^+) = \frac{V_s}{R}$$

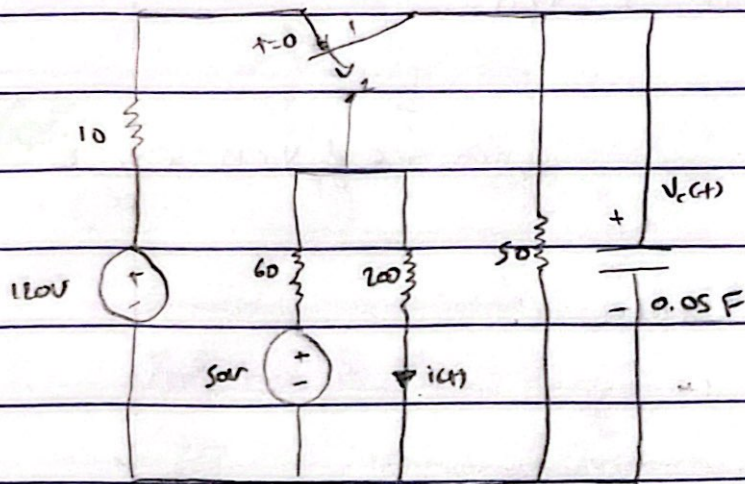


$$i(t) = 0 + \left[\frac{V_s}{R} - 0 \right] e^{-\frac{t}{RC}}$$

$$= \frac{V_s}{R} e^{-\frac{t}{RC}}, \quad t \geq 0$$

Ex:-

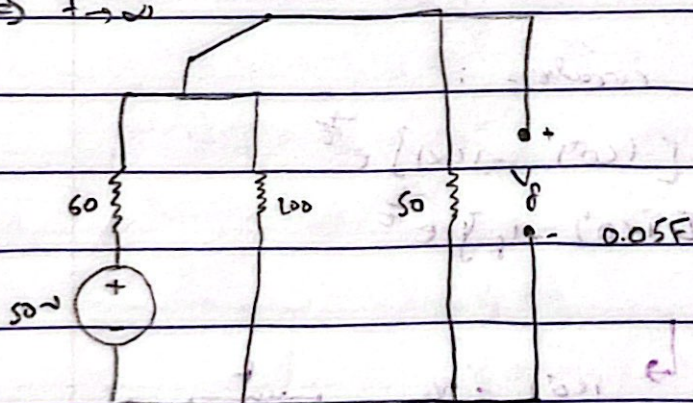
Find $i(t)$ for $t > 0$



$$V_c(t) = \text{---}, \text{ then } i(t) = \frac{V_c(t)}{200}$$

$$V_c(t) = V_f - [V_c(0^+) - V_f] e^{-t/\tau}$$

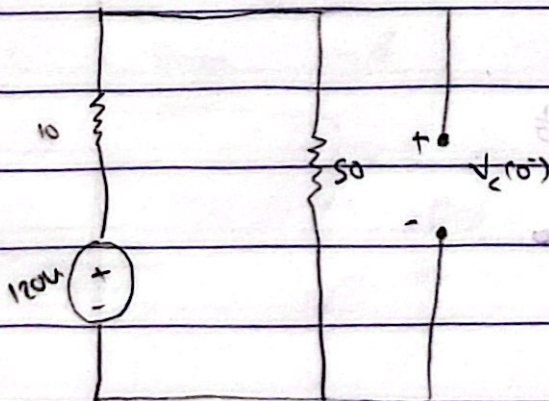
$V_f \Rightarrow t \rightarrow \infty$



$$V_f = \frac{50 \parallel 200}{(50 \parallel 200) + 60} \times 50$$

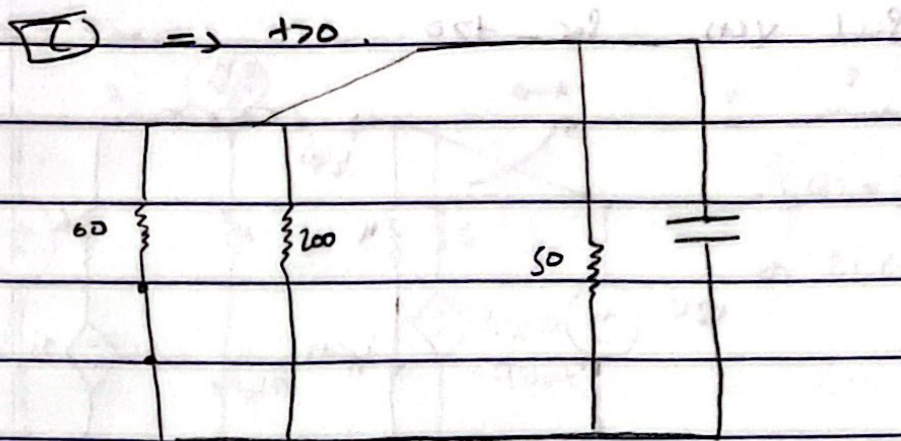
$$= 20 \text{ Volt.}$$

$V_c(0^+) \Rightarrow t \rightarrow 0^+$



$$V_c(0^+) = \frac{50 \parallel 120}{50 \parallel 120 + 10} \times 120$$

$$= 100 \text{ Volt.}$$



$$R_{eq} = 60 \parallel 200 \parallel 50$$

$$= 24 \Omega$$

$$\tau = 0.05 \times 24$$

$$= 1.2 \text{ Sec}$$

$$\Rightarrow V_c(t) = 20 [100 - 20] e^{-\frac{t}{1.2}}$$

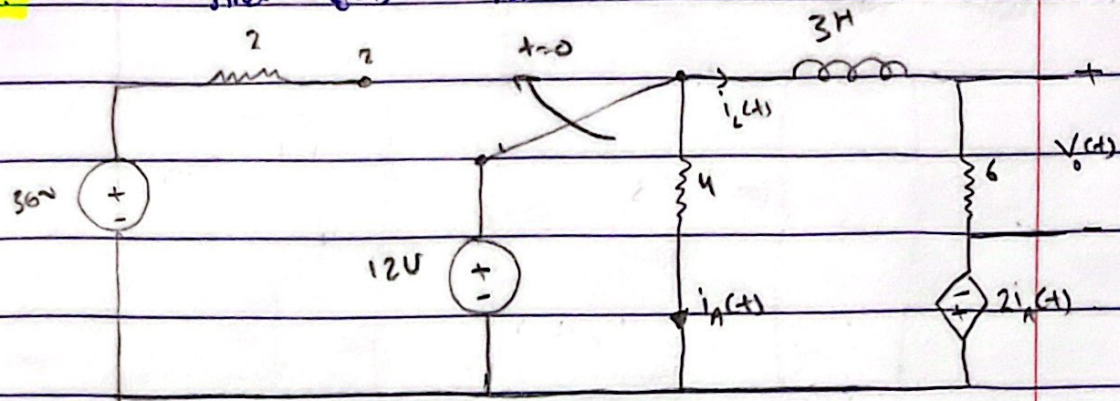
$$= 20 + 80 e^{-\frac{t}{1.2}}, t \geq 0$$

$$\Rightarrow i(t) = \frac{V_c(t)}{200} = \frac{20}{200} + \frac{80}{200} e^{-\frac{t}{1.2}}$$

$$= 0.1 + 0.4 e^{-\frac{t}{1.2}}, t \geq 0$$

EX:-

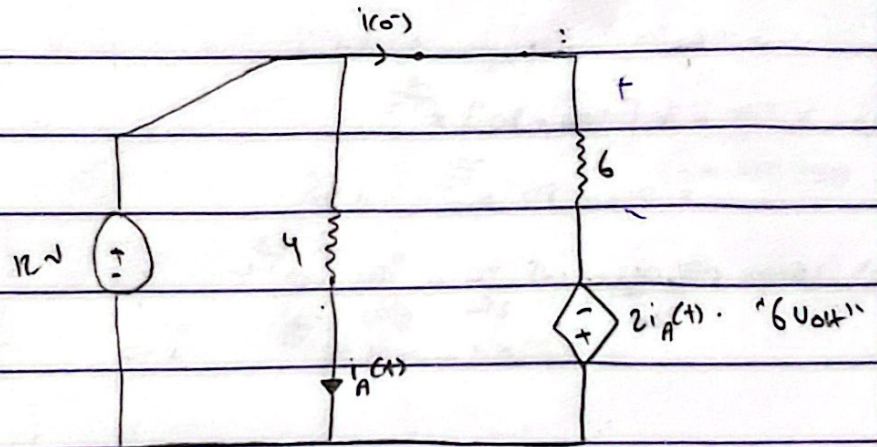
Find $V(t)$ for $t > 0$.



$$i_L(t) = i_g + [i_L(0^-) - i_g] e^{-t/\tau}$$

$$\text{for } V(t) = 6i_L(t)$$

$$i_L(0^+) = i_L(0^-) \Rightarrow \text{from } 0^-$$



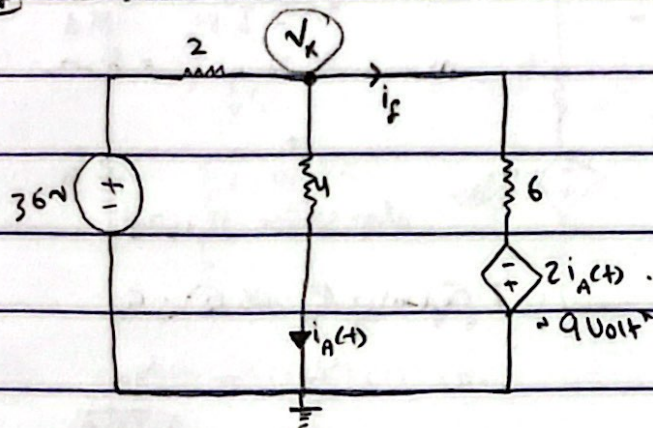
$$i_A(t) = \frac{12}{4} = 3A$$

$$= i_L(0^-) = \frac{12 + 6}{6} = 3A$$

$$\boxed{i_L(0^-) = 3A}$$

i_f

$\Rightarrow t \rightarrow \infty$



$$i_A(t) = \frac{V_x}{4}$$

$$\Rightarrow 2i_A(t) = 2 \cdot \frac{V_x}{4} = \frac{V_x}{2}$$

nodal

$$\frac{V_x - 36}{2} + \frac{V_x}{4} + \frac{V_x + 2i_A(t)}{6} = 0$$

$$\Rightarrow V_x = 18 \text{ Volt}$$

$$\Rightarrow i_A(t) = \frac{18}{4} = 4.5 \text{ A}$$

$$i_f \Rightarrow \frac{18 + 9}{6} = 4.5 \text{ A}$$

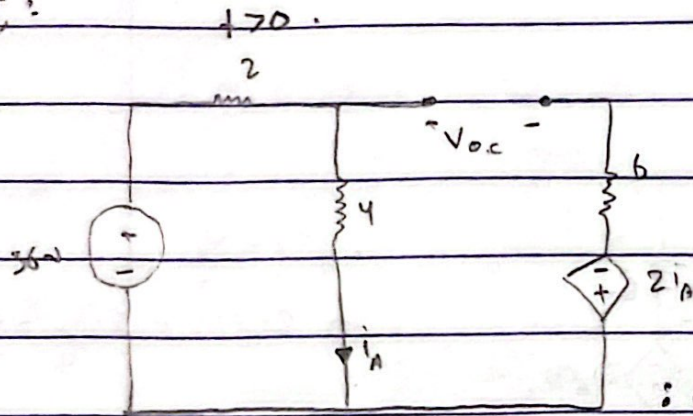
$$i(t) = 4.5 + [3 - 4.5] e^{-\frac{t}{\tau}}$$

$$= 4.5 - 1.5 e^{-\frac{t}{\tau}} \text{ A}$$

$$v_o(t) = 6(4.5 - 1.5 e^{-\frac{t}{\tau}})$$

$$= 27 - 9 e^{-\frac{t}{\tau}} \text{ Volt}$$

T:



$$R_{eq} = \frac{V_{oc}}{I_{sc}} = \frac{36}{4.5} = 8 \Omega$$

dep. source

سعی می‌کنیم R_{eq} را بیابیم:

$$\begin{aligned} \underline{V_{oc}} &= V_{4\Omega} + 2i_A \\ &= \frac{4}{4+2} \cdot 36 + 2 \cdot \frac{36}{6} \\ &= 36 \text{ Volt} \end{aligned}$$

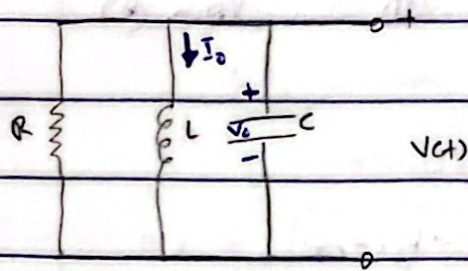
$$\frac{V_T}{I_T} \text{ or } \frac{V_{oc}}{I_{sc}}$$

\Rightarrow already found

$$\tau = 318$$

$$I_{sc} = i_A$$

Impedance (Z): Natural Response of parallel RLC circuit.



Find $V(t)$ for $t > 0$.

KCL

$$i_R(t) + i_L(t) + i_C(t) = 0$$

$$V_L = L \frac{di_L}{dt}$$

$$\frac{d}{dt} \left(\frac{V(t)}{R} + \frac{1}{L} \int V(t) dt + I_0 + C \frac{dV(t)}{dt} \right) = 0$$

$$i_L = \frac{1}{L} \int V_L dt + I_0$$

$$\frac{1}{R} \frac{dV(t)}{dt} + \frac{1}{L} V(t) + C \frac{d^2 V(t)}{dt^2} = 0$$

$$\Rightarrow \text{Let } V(t) = A e^{st}$$

$$\Rightarrow \frac{1}{R} A s e^{st} + \frac{1}{L} A e^{st} + C A s^2 e^{st} = 0$$

$$A e^{st} \left(\frac{1}{R} s + \frac{1}{L} + C s^2 \right) = 0$$

$$\Rightarrow \frac{1}{R} s + \frac{1}{L} + C s^2 = 0$$

$$s^2 + \frac{1}{CL} + \frac{1}{RC} s = 0$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$s_{1,2} = \frac{-1}{2RC} \pm \sqrt{\left(\frac{1}{2RC}\right)^2 - \frac{1}{LC}}$$

$$\omega_0 = \frac{1}{\sqrt{LC}}$$

resonance freq.

$$\alpha = \frac{1}{2RC}$$

damping freq.

$$s_{1,2} = -\alpha \pm \sqrt{\alpha^2 - \omega_0^2}$$

i) if $\alpha > \omega_0$ overdamped response.

$s_{1,2}$ real and distinct.

$$s_1 = -\alpha + \sqrt{\alpha^2 - \omega_0^2}, \quad s_2 = -\alpha - \sqrt{\alpha^2 - \omega_0^2}$$

$$\text{① } V(t) = A_1 e^{s_1 t} + A_2 e^{s_2 t}$$

to find A_1 and $A_2 \Rightarrow$ from $V(t)$ and $\frac{dV(t)}{dt}$

circulate

$$V(t) = V_0 = A_1 + A_2 \quad \dots (1) \quad \text{from (1)}$$

Circuit:

$$i_1(t) + i_2(t) + i_3(t) = 0.$$

$$\frac{V(t)}{R} + I_0 + C \frac{dV(t)}{dt} = 0$$

$$\frac{dV(t)}{dt} = \frac{-I_0}{C} - \frac{V(t)}{RC}$$

from eq (2).

$$\frac{dV(t)}{dt} = A_1 s_1 e^{s_1 t} + A_2 s_2 e^{s_2 t}$$

$$A_1 s_1 + A_2 s_2 = \frac{-I_0}{C} = \frac{-V_0}{RC} \quad (2)$$

Solve for A_1 and A_2 from Eqs (1) and (2)

1) if $\alpha = \omega_0$ critically damped.

$$s_1 = s_2 = s = -\alpha, \text{ repeated}$$

$$V(t) = A_1 t e^{-\alpha t} + A_2 e^{-\alpha t}$$

$$V(0) = A_2 = V_0$$

$$\frac{dV(t)}{dt} = \frac{-I_0}{C} - \frac{V_0}{RC} = -\alpha A_1 + A_2$$

III) if $\alpha < \omega_0$ underdamped response.

$s_{1,2}$ complex.

$$s_{1,2} = -\alpha \pm j\sqrt{\omega_0^2 - \alpha^2} \\ = -\alpha \pm j\omega_d$$

$\omega_d = \sqrt{\omega_0^2 - \alpha^2}$ damped freq of oscillator.

$$v(t) = e^{-\alpha t} [b_1 \cos \omega_d t + b_2 \sin \omega_d t]$$

$$v(0^+) = v_0 = b_1$$

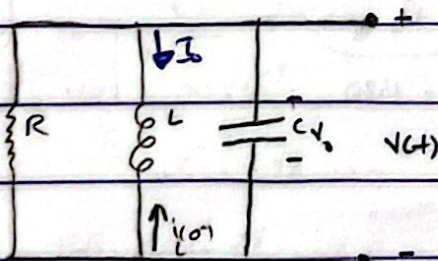
$$\frac{d}{dt} v(0^+) = \left[\frac{-T_0}{C} \frac{v_0}{RC} = \alpha b_1 + \omega_d b_2 \right]$$

Ex:-

$$R = 6 \Omega \quad L = 3 \text{ H} \quad C = \frac{1}{42} \text{ F}$$

$$v(0^+) = 0$$

$$i_L(0^+) = 10 \text{ A}$$



Find $v(t)$ for $t > 0$?

$$\alpha = \frac{1}{2RC} = 3.5 \text{ rad/sec}$$

$$\omega_0 = \frac{1}{\sqrt{LC}} = \sqrt{6} \text{ rad/sec} \\ = 2.45$$

$$s_1 = -\alpha + \sqrt{\alpha^2 - \omega_0^2} = -1 \quad \text{in } \alpha > \omega_0 \Rightarrow \text{overdamped}$$

$$s_2 = -\alpha - \sqrt{\alpha^2 - \omega_0^2} = -6$$

$$v(t) = A_1 e^{-t} + A_2 e^{-6t}$$

$$v(0^+) = A_1 + A_2 = v_0 = v_c(0^+) = 0$$

$$\therefore A_1 + A_2 = 0 \quad \dots \text{SD}$$

$$\frac{d}{dt} V(0^+) = \frac{-I_0}{C} - \frac{V_0}{RC}$$

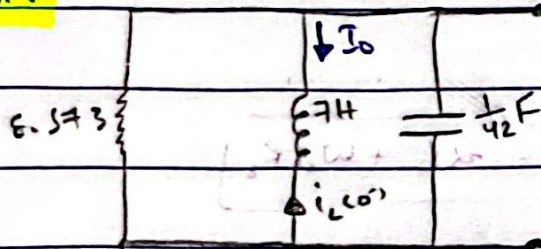
$$= \frac{-(-10)}{1/42} - 0 = 420$$

$$420 = -A_1 - 6A_2 \quad (2)$$

$$\Rightarrow A_1 = 84, A_2 = -84$$

$$V(t) = 84(e^{-t} - e^{-6t}) \text{ Volt, } t > 0$$

Ex:-



$$V_C(0) = 0$$

$$i_C(0) = 10 \text{ A}$$

Find $V(t)$ for $t > 0$.

$$\alpha = \sqrt{6}, \omega_0 = \sqrt{6} \quad \text{H.D. = } -\alpha \pm j\omega_0$$

$\alpha = \omega_0 \Rightarrow$ critically damped.

$$V(t) = A_1 e^{-\alpha t} + A_2 t e^{-\alpha t}$$

$$V(0) = 0 = A_1 + A_2 \Rightarrow A_2 = -A_1$$

$$\frac{d}{dt} V(0^+) = \frac{-I_0}{C} - \frac{V_0}{RC} = 420$$

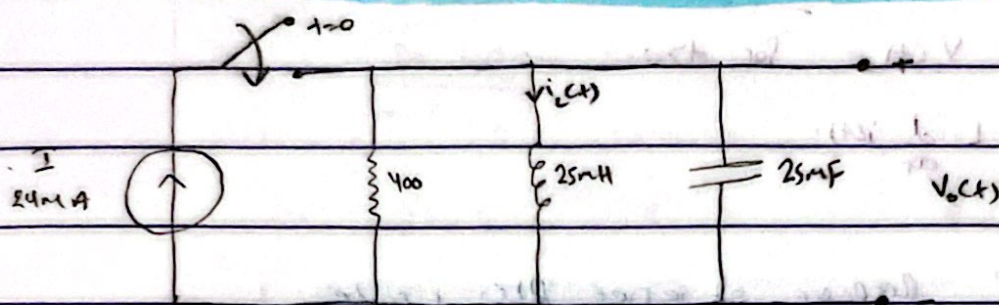
$$\frac{d}{dt} V(t) = A_1 \frac{d}{dt} (t e^{-\alpha t})$$

$$= A_1 (e^{-\alpha t} - \alpha t e^{-\alpha t})$$

$$\frac{d}{dt} V(0^+) = A_1 = 420$$

$$V(t) = 420 t e^{-\sqrt{6} t} \text{ Volt}$$

Step Response of Parallel RLC Circuits

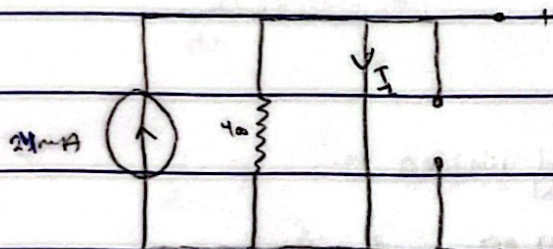


$$i_L(0^-) = 0, \quad V_C(0^-) = 0 \quad \text{Find } i_L(t)$$

$$i(t) = i_R(t) + i_L(t)$$

$$i_R(t) = 24 \text{ mA}$$

$$(t \rightarrow \infty)$$



$$\alpha = \frac{1}{2RC} = 50,000$$

$$\omega_0 = \frac{1}{\sqrt{LC}} = 40,000$$

$\alpha > \omega_0 \rightarrow$ overdamped

$$i(t) = 24 \times 10^{-3} + A_1 e^{s_1 t} + A_2 e^{s_2 t}$$

$$s_1 = -20,000, \quad s_2 = -80,000$$

$$i(t) = 24 \times 10^{-3} + A_1 e^{-20000t} + A_2 e^{-80000t}$$

$$\text{From } i(0^+) \Rightarrow -24 \times 10^{-3} = A_1 + A_2 \quad \text{--- (I)}$$

$$\Rightarrow \frac{d}{dt} i(0^+), \quad V_L(t) = L \frac{d}{dt} i(t)$$

$$\frac{d}{dt} i_L(t) = \frac{1}{L} V_C(t) = 0$$

$$\frac{d}{dt} i(0^+) = -20000 A_1 - 80000 A_2 = 0 \quad \text{--- (II)}$$

$$\Rightarrow A_1 = -32 \text{ mA}, \quad A_2 = 8 \text{ mA}$$

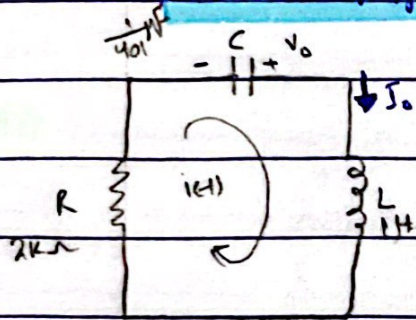
$$i_L(t) = 24 - 32 e^{-20000t} + 8 e^{-80000t} \text{ mA for } t > 0$$

find $v_c(t) = ?$

$$v_c(t) = v_c(t) \quad \text{for } t > 0 \quad \underline{\underline{\text{not } 0}}$$

$$= L \frac{d}{dt} i(t)$$

Natural response of series RLC circuit



$$V_c(0^-) = V_0, \quad i_c(0^-) = I_0$$

$$R i(t) + v_c(t) + L \frac{d}{dt} i(t) = 0$$

$$R i(t) + \frac{1}{C} \int i(t) dt = V_0 + L \frac{d}{dt} i(t) = 0$$

$$R \frac{d}{dt} i(t) + \frac{1}{C} i(t) + L \frac{d^2}{dt^2} i(t) = 0$$

$$\text{Let } i(t) = A e^{st}$$

$$\Rightarrow s R A e^{st} + \frac{1}{C} A e^{st} + L s^2 A e^{st} = 0$$

$$A e^{st} (R s + \frac{1}{C} + L s^2) = 0$$

$$s^2 + \left(\frac{R}{L}\right) s + \frac{1}{LC} = 0$$

$$s_{1,2} = \frac{-R}{2L} \pm \sqrt{\left(\frac{R}{2L}\right)^2 - \left(\frac{1}{LC}\right)}$$

$$= -\alpha \pm \sqrt{\alpha^2 - \omega_0^2}$$

$$\alpha = \frac{R}{2L}$$

$$\omega_0 = \frac{1}{\sqrt{LC}}$$

$$\text{Let } V_0 = 2 \text{ Volt}, \quad I_0 = 2 \text{ mA}$$

$$\alpha = 1000, \quad \omega_0 = 20025$$

$$\alpha < \omega_0 \Rightarrow \text{underdamped}$$

$$i(t) = e^{\alpha t} [\beta_1 \cos \omega_d t + \beta_2 \sin \omega_d t]$$

$$\omega_d = \sqrt{\omega_0^2 - \alpha^2} = 20,000$$

$$i(t) = e^{-1000t} [\beta_1 \cos(20,000t) + \beta_2 \sin(20,000t)]$$

$$\Rightarrow i(0^+) = i(0^-) = 2 \text{ mA} = \beta_1$$

↑ تعريف $i(0^-)$ في المخطط

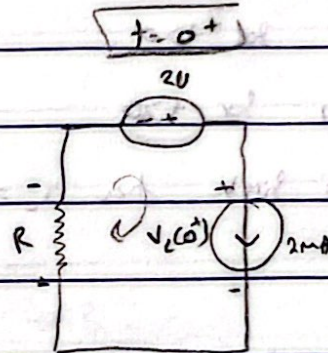
$$\Rightarrow \frac{d}{dt} i(0^+) = ??$$

$$V_L(0^+) = L \frac{d}{dt} i(0^+)$$

$$V_L - RI = L \frac{d}{dt} i(0^+)$$

$$2 - 2k \cdot 2m = \frac{d}{dt} i(0^+)$$

$$\Rightarrow \frac{d}{dt} i(0^+) = -2$$

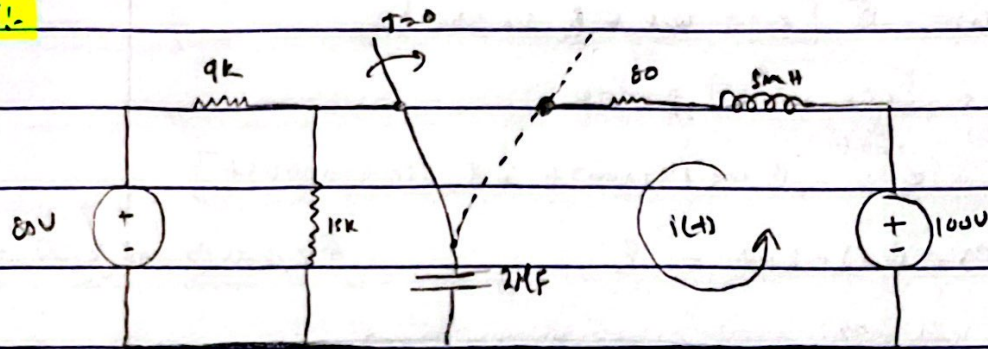


$$\frac{d}{dt} i(t) = -\alpha \beta_1 + \omega_d \beta_2$$

$$\Rightarrow \beta_2 = 0$$

$$\Rightarrow i(t) = 2e^{-1000t} \cos(20,000t) \text{ mA}, t \geq 0$$

Ex:-

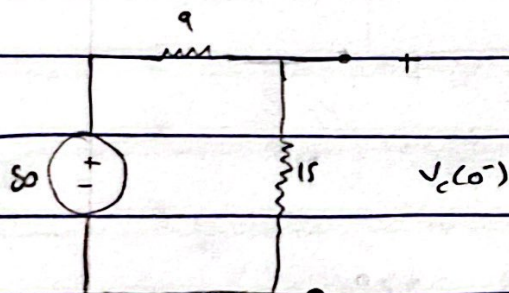


Find $i(t)$ for $t > 0$. , $i_0 = 0$, $V_0 = ?$

Find $V_c(t)$ for $t > 0$

• Find $V_c(t)$ first then $i_L = C \frac{dV_c(t)}{dt}$

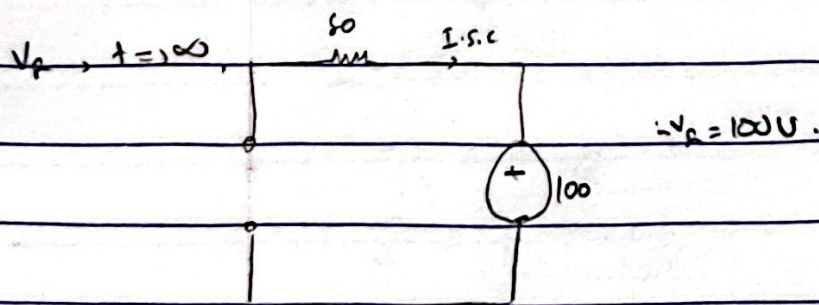
at $t = 0^-$:-



$$V_c(0^-) = V_0 = \frac{15}{15+9} \cdot 50$$

$$= 50 \text{ Volt.}$$

$$\Rightarrow V_c(t) = V_f + V_n(t)$$



$$\alpha = \frac{R}{2L} = 8000$$

$$\omega_0 = \frac{1}{\sqrt{LC}} = 10,000 \quad \text{in } \alpha < \omega_0 \Rightarrow \text{underdamped.}$$

$$v(t) = v_p + e^{\alpha t} [\beta_1 \cos \omega_d t + \beta_2 \sin \omega_d t]$$

$$\rightarrow \omega_d = \sqrt{\omega_0^2 - \alpha^2} = 6000$$

$$\Rightarrow 100 + e^{-8000t} [\beta_1 \cos 6000t + \beta_2 \sin 6000t]$$

$$v(0^+) = v(0^-) = 50 = 100 + \beta_1$$

$$\Rightarrow \beta_1 = -50$$

$$\Rightarrow \frac{d}{dt} v(0^+) = ??$$

$$i(0^+) = C \frac{d}{dt} v(0^+)$$

$$\rightarrow i(0^+) = 0 \Rightarrow -\omega_d \beta_1 + \omega_0 \beta_2$$

$$\Rightarrow \frac{d}{dt} v(0^+) = 0 = -8000\beta_1 + 6000\beta_2$$

$$\Rightarrow \beta_2 = -66.67$$

$$v(t) = 100 - e^{-8000t} [50 \cos 6000t + 66.67 \sin 6000t]$$

\rightarrow to find $i(t)$.

$$i(t) = C \frac{d}{dt} v(t)$$

$$= 2 \times 10^{-6} \left[e^{-8000t} [-3 \times 10^5 \sin 6000t + 400020 \cos 6000t] + 8000 e^{-8000t} [50 \cos 6000t + 66.67 \sin 6000t] \right]$$

$$= e^{-8000t} [-4 \times 10^{-5} \cos 6000t + 1.666 \sin 6000t]$$

\Rightarrow from the book.

Chapter (12):-

table 112.1)	435
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• table C(2.2)	<u>440</u>
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$$\bullet \quad v(t) = \underline{\underline{Q(t)}} \Rightarrow v(s) = \underline{\underline{Q(s)}}$$

constant \Rightarrow still the same

Ex:- $F(s) = \frac{96(s+5)(s+12)}{s(s+8)(s+6)}$

$$\rightarrow \frac{K_1}{5} = \frac{K_2}{(5+8)} = \frac{K_3}{(5+6)} \Rightarrow K_1 = 120$$

$$V_2 = -72$$

$$\bullet K_2 = 48$$

$$\Rightarrow \frac{120}{5} - \frac{72}{(5+8)} + \frac{48}{(5+6)}$$

$$p(t) = (120 - 72e^{-8t} + 48e^{-6t}) u(t) \quad \text{منه بدانی}$$

كانت عازا الى انما يكون ٥ اذا لم يكن نال الحارة

Ex:-

$$F(s) = \frac{100(s+3)}{(s+6)(s^2+6s+25)} = \frac{A}{s+6} + \frac{Bs+C}{s^2+6s+25}$$

$$= \underline{AS^2} + \underline{ABS} + \underline{7SA} + \underline{B1^L} + \underline{CS} + \underline{6BS} + \underline{6C} = 100S + 300$$

$$75A + 6C = 300$$

• $A, B = 0$

~~$$6A + 6B + C = 100 \Rightarrow 6(A+B) + C = 100$$~~

$$\therefore C = 100, A = -12, B = 12$$

$$\frac{-12}{s+6} + \frac{125 + 100}{s^2 + 6s + 25} \quad \nearrow \quad (s+3)^2 + 16$$

الحال من عين

$$\frac{-12}{s+6} + \frac{12s+100}{(s+3)^2+16} \Rightarrow \frac{12 \cdot s + \frac{25}{3}}{(s+3)^2+16} + 3-3$$

$$\Downarrow$$

$$-12e^{-6t}$$

$$12 \cdot \frac{(s+3) + 16/3}{(s+3)^2+16}$$

$$12 \cdot \left[\frac{(s+3)}{(s+3)^2+16} + \frac{16/3}{(s+3)^2+16} \right]$$

$$12 \cdot \left[\cos 4t e^{-3t} + \frac{4}{3} \sin 4t e^{-3t} \right]$$

$$\Rightarrow -12e^{-6t} + 12e^{-3t} \cos 4t + 16e^{-3t} \sin 4t$$

$$e^{-3t} (12 \angle 0^\circ + 16 \angle 90^\circ)$$

$$e^{-3t} (12, 16j)$$

$$-12e^{-6t} + e^{-3t} (20 \angle -53.13^\circ)$$

$$\bullet (-12e^{-6t} + 20e^{-3t} \cos(4t - 53.13^\circ)) u(t)$$

Ex:

$$F(s) = \frac{100(s+25)}{(s+5)^3}$$

$$\frac{K_1}{s} + \frac{K_2}{(s+5)^3} + \frac{K_3}{(s+5)^2} + \frac{K_4}{(s+5)}$$

• قواسم صفر لاف

$$K_1(s+5)^3 + K_2s + K_3s + sK_4 + K_4(s+5)^2 \cdot (s+5)^3$$

$$\left[\begin{array}{l} K_1s^3 + 15K_1s^2 + 75K_1s + 125K_1 + K_3s^2 + 5K_3s + K_4s^2 + 10K_4s + 25K_4 + K_4(s^2 + 10s + 25) \\ K_1s^3 + 15K_1s^2 + 75K_1s + 125K_1 + 2500 \end{array} \right] = s^3 + 10s^2 + 25s + 125$$

$$\rightarrow 125K_1 = 2500$$

$$\therefore K_1 = 20$$

$$\Rightarrow s^3 + 15s^2 + 75s + 125$$

$$K_4 = -20$$

$$\rightarrow 15K_1 + 10K_4 + K_3 = 0$$

$$300 + 200 + K_3 = 0$$

$$\therefore K_3 = -500$$

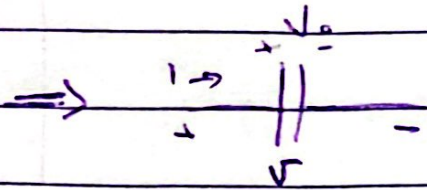
$$\Rightarrow 75 \cdot 20 + (-500) + K_2 - 500 = 100$$

$$1500 + K_2 = 100$$

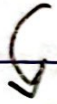
$$\therefore K_2 = -1400$$

$$\Rightarrow \frac{20}{s} - \frac{1400}{(s+5)^3} - \frac{500}{(s+5)^2} - \frac{20}{s+5}$$

$$\left[20 - 1400t^2e^{-5t} - 500te^{-5t} - 20e^{-5t} \right] u(t)$$



$$I = C \frac{dV(t)}{dt}$$



$$I = C(SV - V_0)$$

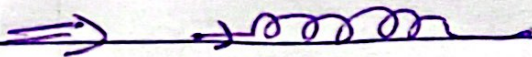
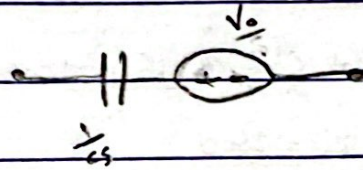
$$VI = C(SV - V_0)$$

$$V = \frac{I}{CS} + \frac{V_0}{S}$$

Voltage.

$$V = ZI \quad \therefore Z = \frac{1}{CS}$$

Impedance



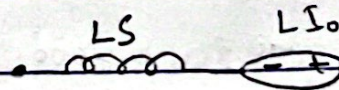
$$V = L \frac{dI(t)}{dt}$$



$$V = L(SI - I_0)$$

$$V = \frac{LSI}{S} - LI_0$$

Z



current source

⇒ without initial condition.

$$V_c(0^-) = 0$$

$$i_L(0^-) = 0$$

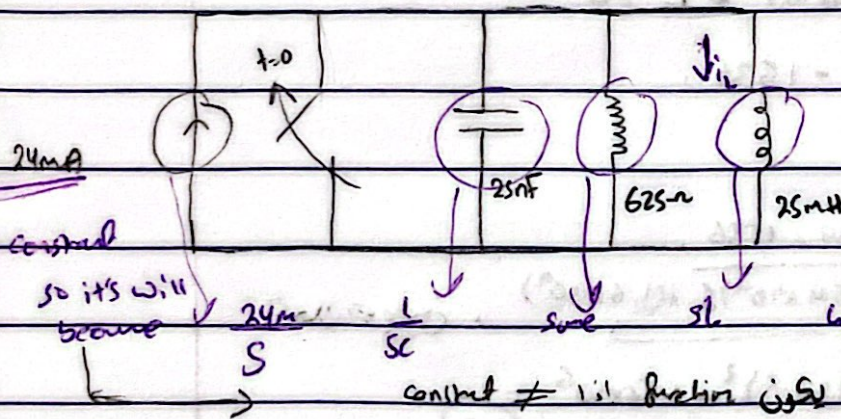
C	→	$\frac{1}{sC}$	sC
L	→	sL	$\frac{1}{sL}$
R	→	R	$\frac{1}{R}$

Ex:- Step response of a parallel RLC

→ Find $i_L(t)$

$$V_c(0^-) = 0$$

$$i_L(0^-) = 0$$



constant \neq 1st function $V(s)$, $i(s)$, $i_L(s)$
 $I(s)$, $V(s)$ مخرج

Sol:-

CD: $i_L(s)$ لا كاد

$$1) \frac{\frac{1}{sC} \cdot R}{\frac{1}{sC} + R} = \frac{R}{RCs + 1}$$

$$2) \frac{\frac{R}{RCs + 1}}{\frac{R}{RCs + 1} + sL} \cdot \left(\frac{24mA}{s}\right) = \frac{RCs + 1}{RCs + 1}$$

$$\frac{1}{R + s^2LC + sL} \cdot \frac{24mA}{s} = \frac{24mA \cdot R}{s(R + LCs^2 + Ls)}$$

$$\Rightarrow \frac{1/LC}{S(S^2 + \frac{1}{RC}S + \frac{1}{LC})} = \frac{3.84 \times 10^7}{S[S^2 + (6.4 \times 10^4)S + (1.6 \times 10^9)]}$$

$$= \frac{A}{S} + \frac{BS + C}{S^2 + (6.4 \times 10^4)S + (1.6 \times 10^9)}$$

$$= \frac{AS^2 + A(6.4 \times 10^4)S + (1.6 \times 10^9)A}{S^2 + (6.4 \times 10^4)S + (1.6 \times 10^9)} + \frac{BS^2 + CS}{S^2 + (6.4 \times 10^4)S + (1.6 \times 10^9)} = \frac{3.84 \times 10^7}{S^2 + (6.4 \times 10^4)S + (1.6 \times 10^9)}$$

$$A(1.6 \times 10^9) = 3.84 \times 10^7$$

$$\therefore A = 0.024$$

$$\Rightarrow A + B = 0$$

$$\therefore B = -0.024$$

$$(0.024)(6.4 \times 10^4) + C = 0$$

$$\therefore C = -1536$$

$$\Rightarrow \frac{0.024}{S} - \frac{0.024 + 1536}{S^2 + (6.4 \times 10^4)S + (1.6 \times 10^9)}$$

$$(S + 32 \times 10^3)^2 + 576 \times 10^6$$

$$\Rightarrow \frac{0.024}{S} - 0.024 \left[\frac{S + 64 \times 10^3}{(S + 32 \times 10^3)^2 + 576 \times 10^6} \right]$$

$$\frac{0.024}{S} - 0.012 \left[\frac{S + (32 \times 10^3)}{(S + (32 \times 10^3))^2 + 576 \times 10^6} \right]$$

$$0.024 - 0.012 e^{-32 \times 10^3 t} \cos(24 \times 10^3 t)$$

$$0.024 - 24000 \angle 90^\circ \quad A \quad \text{✓}$$

2.17

$$\bullet \text{ KCL } \Rightarrow 0.02 = i_1 + i_2$$

$$\bullet \text{ KVL } \Rightarrow -V_o + V_s - 5 = 0$$

$$5 = -5000 i_1 + 2000 i_2$$

$$5 = -5000 i_1 + 2000 (0.02 - i_1)$$

$$5 = -5000 i_1 + 40 - 2000 i_1$$

$$5 = -7000 i_1 + 40$$

$$35 = 7000 i_1$$

$$\therefore i_1 = 0.005 \text{ A} = 5 \text{ mA}$$

$$= 5000 \times 5 \times 10^{-3} = 25 \text{ V} = V_o$$

$$\Rightarrow i_2 = 0.02 - 0.005 = 0.015 \text{ A}$$

the test:-

$$P_{20} = -(20 \times 10^{-3})(25) = -0.5 \text{ W}$$

$$P = i^2 R$$

$$P_2 = (2000)(0.015)^2 = 0.45 \text{ W}$$

$$P_5 = (5000)(0.005)^2 = 0.125 \text{ W}$$

$$P_{5V} = 5(0.015) = -0.075 \text{ W}$$

$$\bullet 0.45 + 0.125 - 0.075 - 0.5 = 0$$

2.20

$$\bullet \text{ KCL } \Rightarrow 50 \times 10^{-3} = i_1 + i_2$$

$$(1) \bullet \text{ KVL } \Rightarrow -250i_2 + 200i_1 + 175i_1 = 0$$

$$-250i_2 + 375i_1 = 0$$

$$-250(0.05 - i_1) + 375i_1 = 0$$

$$-12.5 + 250i_1 + 375i_1 = 0$$

$$12.5 = 625i_1$$

$$\boxed{i_1 = 0.02 \text{ A}}$$

$$V_1 = 250i_2 = 250(0.05 - 0.02)$$

$$= \boxed{7.5 \text{ V}}$$

$$(2) \bullet \text{ KVL } \Rightarrow -V_g + 50i_1 + V_1 = 0$$

$$-V_g + 50(0.05) + 7.5 = 0$$

$$\boxed{V_g = 10 \text{ V}}$$

$$P_g = (-0.05)(10) = \boxed{-0.5 \text{ W}} \text{ ~delivering power}$$

2.27 a) $P_{up} = -(147)(28) = -4116 \text{ W}$

$P_x = -(147)(21) = -3087 \text{ W}$

b) abs $\Rightarrow (28)^2 + (21)^2 + (7)^2 + (14)^2 + (10)^2 + (21)^2 + (7)^2 + (35)^2 = 7203 \text{ W}$
 $p = Vi = i^2 R$
 $\text{del} \Rightarrow 7203 \text{ W}$

therefore $\sum P_{abs} = \sum P_{del}$

2.32

KCL $\Rightarrow 45 = i_x + i$

KVL $\Rightarrow -i \times 6 + 2i + 2i_x = 0$

$-4i_x + 2(45 - i_x) = 0$

$90 - 6i_x = 0 \Rightarrow i_x = 15 \text{ A}$

$i = 30 \text{ A}$

$V_o = 2i = 2(30) = 60 \text{ V}$

$V_x = 6i_x = 6(15) = 90 \text{ V}$

$\Rightarrow P_{45} = -Vi = (-90)(45) = -4050 \text{ W}$

$P_{2i_x} = Vi = (2i_x)(i) = (2 \cdot 15 \times 30) = 900 \text{ W}$

So the source who supplying power is P_{45} by 4050 W .

2.33 • KVL $\Rightarrow -20 + 450i + 150i = 0$

① $20 = 600i, \therefore i = 0.033333 \text{ A}$

$\therefore V_x = 0.03333 \times 150 = 5 \text{ V}$

$V_o = \left(\frac{V_x}{100}\right) 300$

$= (0.5) 300 = 15 \text{ V}$

\Rightarrow power:-

$P_{20} = -20(0.03333) = -0.667 \text{ W}$

$P_{450} = 450(0.0333)^2 = 0.5 \text{ W}$

$P_{150} = 150(0.0333)^2 = 0.1667 \text{ W}$

$P_{300} = 300(0.5)^2 = 0.75 \text{ W}$

$P_p = -V_o(0.05) = -0.75 \text{ W}$

$\therefore \text{net } \Sigma P_{\text{abs}} = 1.4167 \text{ W}$

2.34

• $V_1 = (4000)(10 \times 10^{-3}) = 40 \text{ V}$

• KVL $\Rightarrow -20 + 2000i_o + 6000i_o = 0$

$\therefore 20 = 8000i_o$

$\therefore i_o = 2.5 \text{ mA} = 0.0025$

\Rightarrow power:-

$P_4 = (4000)(10 \times 10^{-3})^2 = 0.4 \text{ W}$

$P_2 = (2000)(0.0025)^2 = 0.0125 \text{ W}$

$P_6 = (6000)(0.0025)^2 = 0.0375 \text{ W}$

$P_p = (-10 \times 10^{-3})(40) = -0.4 \text{ W}$

$P_{V_1} = (0.0025)(20) = -0.05 \text{ W}$

$\therefore \Sigma P_{\text{abs}} = 0.45 \text{ W}, \Sigma P_{\text{del}} = 0.45 \text{ W}$ so it's ok

3.5

a) $R = 12 \Omega$

$V = 18 \text{ V}$

$V = iR \Rightarrow I = \frac{18}{12}$

$\Rightarrow I = 1.5 \text{ A}$

$\Rightarrow P = (1.5)(18) = 27 \text{ W}$

b) $R = 900 \Omega$

$V = 27 \text{ V}$

$\Rightarrow I = \frac{27}{900}$

$\Rightarrow I = 0.03 \text{ A}$

$\Rightarrow P = (-0.03 \times 27)$

$= -0.81 \text{ W}$

c) $R = 30 \Omega$

$V = 90 \text{ V}$

$\Rightarrow I = \frac{90}{30}$

$\Rightarrow I = 3 \text{ A}$

$\Rightarrow P = (-3 \times 90)$

$= -270 \text{ W}$

d) $R = 120 \Omega$

$I = 30 \times 10^{-3} \text{ A}$

$\Rightarrow V = 30 \times 10^{-3} \times 120 = 3.6 \text{ V}$

$\Rightarrow P = (-30 \times 10^{-3}) \times 3.6 = -0.108 \text{ W}$

3.6

a) $R = 36 \Omega$

$$V = 18 \text{ V}$$

$$I = \frac{18}{36} = 0.5 \text{ A}$$

$$P \Rightarrow (0.5)(18) = 9 \text{ W}$$

b) $R = 60 \Omega$

$$I = 30 \times 10^{-3} \text{ A}$$

$$V = (30 \times 10^{-3})(60) = 1.8 \text{ V}$$

$$P \Rightarrow (30 \times 10^{-3})(1.8) = 0.054 \text{ W}$$

c) $R = 150 \text{ k} \Omega$

$$V = 60 \text{ V}$$

$$I = \frac{60}{150 \times 10^3} = 4 \times 10^{-4} \text{ A}$$

$$P \Rightarrow (4 \times 10^{-4})(60) = 0.024 \text{ W}$$

d) $R = 3250 \Omega$

$$V = 65 \text{ V}$$

$$I = \frac{65}{3250} = 0.02 \text{ A}$$

$$P \Rightarrow (0.02)(65) = 1.3 \text{ W}$$

3.21

$$a) \quad R_1 = \frac{K - \alpha}{\alpha k} R_0$$

$$V_0 = kV_s = \frac{R_2}{R_1 + R_2} V_s \quad \text{No load}$$

$$V_0 = \alpha V_s = \frac{R_2}{R_1 + R_e} V_s \quad \text{Full load}$$

$$\Rightarrow R_e = \frac{R_2 R_0}{R_1 + R_0}$$

$$\therefore k = \frac{R_2}{R_1 + R_2} \Rightarrow \therefore R_1 = \frac{R_2 (1 - k)}{k}$$

$$\therefore \alpha = \frac{R_e}{R_1 + R_e} \Rightarrow \therefore R_1 = \frac{R_e (1 - \alpha)}{\alpha}$$

$$\text{That's mean :- } \left(\frac{1 - k}{k} \right) R_2 = \left(\frac{1 - \alpha}{\alpha} \right) R_e \left[\frac{R_2 R_0}{R_1 + R_0} \right]$$

$$\Rightarrow \text{So } R_2 = \left(\frac{k - \alpha}{\alpha (1 - k)} \right) R_0$$

$$R_1 = \left(\frac{1 - k}{k} \right) \left(\frac{k - \alpha}{\alpha (1 - k)} \right) R_0 = \frac{k - \alpha}{\alpha k} R_0$$

$$b) \quad R_1 = \left(\frac{k - \alpha}{\alpha k} \right) R_0 \Rightarrow \frac{0.85 - 0.80}{(0.85)(0.80)} \cdot 34 \times 10^3 = 2.5 \text{ k}\Omega$$

$$R_2 = \left(\frac{k - \alpha}{\alpha (1 - k)} \right) R_0 \Rightarrow \left(\frac{0.85 - 0.80}{0.80(1 - 0.85)} \right) \cdot 34 \times 10^3 = 14.167 \text{ k}\Omega$$

3.23

a) $R = 12 \text{ k}\Omega$

$I = 1.5 \text{ A}$

$$V_0 = \frac{4 \text{ k}\Omega}{4 \text{ k}\Omega + 8 \text{ k}\Omega} (15) = 6 \text{ V}$$

b) $V = 6 \text{ V}$

$R = 12 \text{ k}\Omega$

$I = 0.5 \text{ A}$

$$V = (0.5)(12) = 6 \text{ V}$$

3.24

a) $R = 120 \Omega$

$I = 30 \times 10^{-3} \text{ A}$

$V = 3.6 \text{ V}$

$$I_{50} = \frac{120}{60 + 90 + 50} (30 \times 10^{-3}) = 0.018 \text{ A}$$

b) $\frac{60}{80 + 70} \times 0.018 = 7.2 \text{ mA}$

3.25

$$a) \frac{25}{25+10+25} \times 30 = 12.5 \text{ V}$$

$$b) V = iR \Rightarrow i = \frac{12.5}{25} = 0.5 \text{ A}$$

$$c) \frac{(12+18+20) \parallel 50}{50} \times 0.5 = 0.25 \text{ A}$$

$$d) V = iR \Rightarrow 0.25 \times 50 = 12.5 \text{ V}$$

$$e) \frac{12}{12+8+20} \times 12.5 = 3 \text{ V}$$

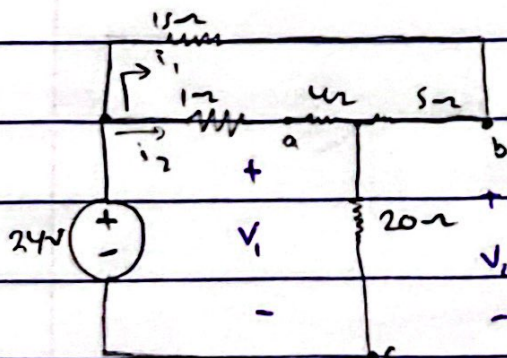
3.31

$$i_s = \frac{V}{R} = \frac{125}{10} = 12.5 \text{ A}$$

$$\frac{40 \parallel 10}{10} \times 12.5 = 10 \text{ A}$$

$$i_o = \frac{4}{20} \times 10 = 2 \text{ A}$$

3.59



$$R_1 = 10 \times 40 / 100 = 4 \Omega$$

$$R_2 = 50 \times 10 / 100 = 5 \Omega$$

$$R_3 = 40 \times 50 / 100 = 20 \Omega$$

$$R_{eq} = 24 \Omega$$

$$i_1 = \frac{(20 \parallel 15)}{20} \times 1 = 0.2 \text{ A}$$

$$i = 1 \text{ A}$$

$$i_2 = 1 - 0.2 = 0.8 \text{ A}$$

• $V_1 =$

نقطة 4 و 20

$$4i_1 + 20i_1 = 4 \times 0.8 + 20$$

$$= 23.2 \text{ V}$$

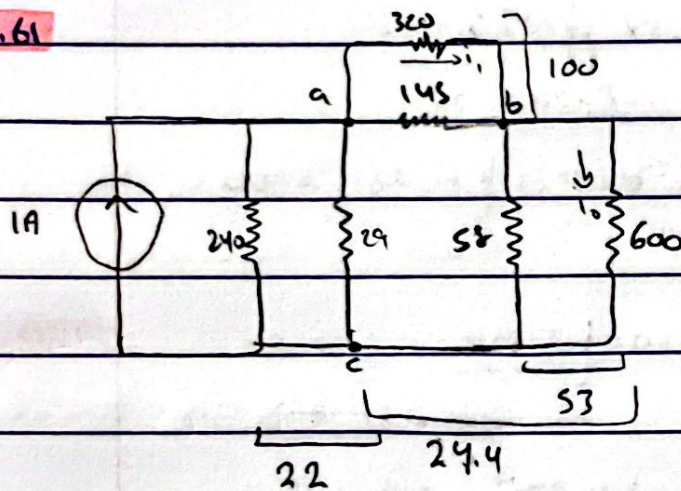
• $V_2 =$

نقطة 5 و 20

$$5i_1 + 20i_1 = 5 \times (0.2) + 20$$

$$= 21 \text{ V}$$

3.61



$$R_a = \frac{2400}{20} = 145 \Omega$$

$$R_b = \frac{2400}{50} = 58 \Omega$$

$$R_c = \frac{2400}{100} = 24 \Omega$$

$i_b =$

Q(6):- $\frac{V_x - 24}{100} + \frac{V_x}{25} + 40 \times 10^{-3} = 0$ (nodal)

$$\frac{V_x}{100} - \frac{24}{100} + \frac{4V_x}{100} + 40 \times 10^{-3} = 0$$

$$\frac{V_x}{20} = \left(\frac{24}{100} - 40 \times 10^{-3} \right) \times 20$$

$$\therefore V_x = 4V = V_o$$

Mesh:- $-24 + 20I_1 + 80I_1 + 25(I_1 + 40 \times 10^{-3}) = 0$

$$-24 + 100I_1 + 25I_1 = 1 = 0$$

$$25 = 125I_1, \therefore I_1 = 0.2 \text{ A}$$

$$\therefore V_o = 25(0.2 - 40 \times 10^{-3}) = 4 \text{ V}$$

Q(9):- $-2 + \frac{V_x}{50} + \frac{V_x - 45}{1} = 0, \frac{51V_x}{50} = 47$

$$\therefore V_x = 46$$

$$\therefore \text{Pot } 2 \text{ A} = 2 \times 46 = 92 \text{ W} \text{ delivers}$$

Q(11):-

$$V_1 \Rightarrow \frac{V_1 - 128}{5} + \frac{V_1}{60} + \frac{V_1 - V_2}{4} = 0, \frac{21V_1}{5} + \frac{V_1}{60} + \frac{13V_1}{4} - \frac{V_2}{4} = \frac{128}{5}$$

$$\frac{25V_1}{60} - \frac{V_2}{4} = \frac{128}{5} \Rightarrow 0.4166V_1 - 0.25V_2 = 25.6 / 1.45$$

$$V_2 \Rightarrow \frac{V_2 - V_1}{4} + \frac{V_2}{80} + \frac{V_2 - 320}{10} = 0, \frac{20 \cdot \frac{V_2 - V_1}{4} - \frac{V_1}{4} + \frac{V_2}{80} - \frac{V_2}{10} = 32$$

$$\frac{29V_2}{80} - \frac{1}{4}V_1 = 32 \Rightarrow 0.3625V_2 - 0.25V_1 = 32$$

$$\rightarrow 0.6757V_1 - 0.3625V_2 = 37.12$$

$$+ 0.3625V_2 - 0.25V_1 = 32$$

$$= 0.4232V_1 = 69.12 \therefore V_1 = 162 \text{ V}$$

$$\therefore V_2 = 260 \text{ V}$$

$$a) \quad i_a \Rightarrow \frac{128 - 162}{5} = -6.8 \text{ A} \quad i_c \Rightarrow \frac{162 - 200}{4} = -9.5 \text{ A}$$

$$i_b = \frac{162}{60} = 2.7 \text{ A} \quad i_d \Rightarrow \frac{200}{80} = 2.5 \text{ A}$$

$$i_e = \frac{200 - 320}{10} = -12 \text{ A}$$

$$b) \quad -1.68(128) = 870.4 \text{ W} \quad , \quad V_{12}(320) = -3640 \text{ W}$$

Q(K):-

$$V_1 \Rightarrow V_1 - 125 + \frac{V_1 - V_2}{6} = 0$$

$$\frac{V_1}{24} + \frac{20V_1}{24} + \frac{4V_1}{24} - \frac{V_2}{6} = 125 \quad , \quad 1.2083V_1 - 0.1666V_2 = 125 / 0.1379$$

$$= 0.1666V_1 - 0.02797V_2 = 17.23$$

$$V_2 \Rightarrow \frac{V_2 - V_1}{6} + \frac{V_2}{2} + \frac{V_2 - V_3}{12} = 0$$

$$\frac{2V_2}{12} - \frac{V_1}{6} + \frac{6V_2}{12} + \frac{V_2}{12} - \frac{V_3}{12} = 0 \quad , \quad 0.75V_2 - 0.1666V_1 - 0.0833V_3 = 0$$

$$V_3 \Rightarrow \frac{V_3 - V_2}{12} + \frac{V_3}{24} + \frac{V_3 + 125}{1} = 0$$

$$\frac{2V_3}{24} - \frac{V_2}{12} + \frac{V_3}{24} + \frac{24V_3}{24} = -125 \quad , \quad 1.125V_3 - 0.0833V_2 = -125$$

$$\rightarrow 0.727V_2 - 0.0833V_3 = 17.23$$

$$1.125V_3 - 0.0833V_2 = -125 / 0.074$$

\Rightarrow

$$0.727V_2 - 0.0833V_3 = 17.23$$

$$+ \quad 0.0833V_3 - 6.125V_2 = 9.255$$

$$\Rightarrow 0.72083V_2 = 7.975 \quad \therefore V_2 = 11 \text{ V}$$

$$V_3 = -110 \text{ V}$$

$$V_4 = 104 \text{ V}$$

$$\begin{aligned}
 a) \quad & \cdot I_1 \Rightarrow 125 - 104 = 21 \text{ A} \quad \cdot I_4 \Rightarrow \frac{104 - 11}{6} = 15.5 \text{ A} \\
 & \cdot I_2 \Rightarrow \frac{11}{2} = 5.5 \text{ A} \quad \cdot I_5 \Rightarrow \frac{11 - 110}{2} = 10.08 \text{ A} \\
 & \cdot I_3 \Rightarrow -110 + 125 = 15 \text{ A} \quad \cdot I_6 \Rightarrow \frac{104 - 110}{24} = 8.9 \text{ A}
 \end{aligned}$$

$$b) \quad \text{del} \Rightarrow (125 \times -21) + (125 \times -15) = -4500 \text{ W}$$

$$\begin{aligned}
 \text{abs} \Rightarrow & 441 + 60.5 + 225 + 1441.5 + 1219.2768 + 1901.04 \\
 & 5288.3168 \text{ W}
 \end{aligned}$$

there is something wrong with calculation

$$Q(47):- \quad V_b \Rightarrow -3 + \frac{V_b}{200} + \frac{V_b + 510}{10} + \frac{V_b - 80}{20} = 0$$

$$i_b = \frac{V_b - 80}{20}$$

$$\rightarrow 3 = \frac{V_b}{200} + \frac{V_b}{10} + \frac{1}{2} \left(\frac{V_b - 80}{20} \right) + \frac{V_b}{20} - 4 = 0$$

$$7 = \frac{11 V_b}{200} + \frac{1}{40} V_b - 2 + \frac{V_b}{20} - 0$$

$$9 = \frac{26 V_b}{200} + \frac{V_b}{20} \quad \Rightarrow 9 = \frac{36 V_b}{200}$$

$$a) \quad \Rightarrow V_b = 50 \text{ V}$$

$$\Rightarrow i_b = \frac{50 - 80}{20} = -1.5 \text{ A}$$

$$\Rightarrow \text{sid} = -7.5 \text{ V} \quad , \quad i_{ab} = \frac{50 - 75}{10} = 4.25 \text{ A}$$

$$b) \quad \Rightarrow P = 7.5 (4.25) = 31.875 \text{ W}$$

$$\begin{aligned}
 V &= iR \\
 P &= IV \\
 &= \frac{V^2}{R}
 \end{aligned}
 \quad \cdot P_3 = -3 \times 50 = 150 \text{ W} \quad , \quad P_{30} = -15 \times 50 = -750 \text{ W}$$

$$\Rightarrow 270 \text{ W} \quad a)$$

Q(2):-

$$V_1 \Rightarrow -5i_0 + \frac{V_1}{20} + \frac{V_1 - V_2}{5} = 0, \quad i_0 = \frac{V_1}{40}$$

$$-5 \times \frac{V_1}{40} + \frac{V_1}{20} + \frac{4V_1 - V_2}{20} = 0$$

$$\frac{-V_2}{5} + \frac{5V_1}{20} - \frac{V_2}{5} = 0$$

$$-0.325V_1 + 0.25V_2 = 0 \quad / 4.4 \quad (2)$$

$$V_2 \Rightarrow \frac{V_2 - V_1}{5} + \frac{V_2}{40} + \frac{V_2 - V_3}{10} = 0$$

$$5 \times \frac{V_2}{40} - \frac{V_1}{5} + \frac{V_2}{40} + \frac{4V_2 - V_3}{40} - \frac{V_3}{10} = 0$$

$$\frac{13V_2}{40} - \frac{V_1}{5} - \frac{V_3}{10} = 0$$

$$0.325V_2 - 0.2V_1 - 0.1V_3 = 0 \quad / 5.5 \quad (1)$$

$$V_3 \Rightarrow \frac{V_3 - V_2}{10} + \frac{V_3 - 11.5i_0}{5} + \frac{V_3 - 96}{4} = 0$$

$$\left(\frac{V_3}{10}\right) - \frac{V_2}{10} + \left(\frac{V_3}{5}\right) - 11.5 \times \frac{V_1}{40} + \left(\frac{V_3}{4}\right) - \frac{96}{4} = 0$$

$$0.55V_3 - 0.1575V_2 = 24$$

$$\rightarrow 1.7875V_2 - 1.1V_1 - 0.55V_3 = 0$$

$$+ 0.55V_3 - 0.1575V_2 = 24$$

$$1.63V_2 - 1.1V_1 = 24$$

$$+ -1.43V_2 + 1.1V_1 = 0$$

$$\Rightarrow 0.2V_2 = 24 \quad \therefore V_2 = 120 \text{ V}$$

$$\therefore V_3 = 78 \text{ V}$$

$$\therefore V_1 = 156 \text{ V}$$

a)

$$P_{s10} \Rightarrow 156 \times 5i_0, \quad i_0 = \frac{120}{40} = 3A$$

$$156 \times 15 = 2340W$$

$$P_{u,50} \Rightarrow (11.5 \times 3)(8.7) \quad \frac{1}{2}I = 8.7A$$

$$= +300.15W$$

$$P_{a6} \Rightarrow (96)(-4.5) \quad I = -4.5A$$

$$= -432W$$

$$b) \quad \Sigma P_{del} = 432 + 2340 = 2772W$$

Q(28):-

$$V_1 = 4V$$

$$V_2 = -2V_x \quad \checkmark$$

$$V_x = V_2 - V_1 = -2V_x - 4$$

$$V_0 \Rightarrow 7 + \frac{V_0}{3} + \frac{V_0 - V_2}{1} = 0$$

$$V_x = -2V_x - 4$$

$$7 + \frac{V_0}{3} + V_0 + 2V_x = 0$$

$$\therefore V_x = -\frac{4}{3} \checkmark$$

$$7 + \frac{V_0}{3} + \frac{3}{3}V_0 + 2\left(-\frac{4}{3}\right) = 0$$

$$7 + \frac{4}{3}V_0 = \frac{8}{3} = 0$$

$$\frac{8}{3} - \frac{21}{3} = -\frac{4}{3}V_0$$

$$-\frac{13}{3} = -\frac{4}{3}V_0$$

$$V_0 = -\frac{13}{4} \checkmark$$

Q(30) :-

$$V_4 = 3.125 V_2, \quad V_0 = \frac{V_2 - V_3}{1} = V_2 - V_3$$
$$V_2 = 20 \text{ V} = 20 - V_3$$

$$V_1 \Rightarrow \frac{V_1}{20} + \frac{V_1 - V_2}{2} + \frac{V_4 - V_3}{4} + \frac{V_4}{60} + 3.125 V_0 = 0$$

$$\frac{11V_1}{20} = 10 + \frac{3.125V_0}{4} - \frac{V_3}{4} + \frac{3.125V_0}{60} + 3.125V_0 = 0$$

$$0.55V_1 = 10 + 3.9453 V_0 - 0.25V_3 = 0$$

$$0.55V_1 + 3.9453(20 - V_3) - 0.25V_3 = 0$$

$$0.55V_1 + 78.906 - 3.9453V_3 - 0.25V_3 = 0$$

$$0.55V_1 - 4.1953 V_3 = -78.906$$

$$V_3 \Rightarrow \frac{V_3 - V_2}{1} + \frac{V_3 - V_4}{4} + \frac{V_3}{40} = 0$$

$$V_3 - 20 + \frac{V_3}{4} - \frac{3.125V_0}{4} + \frac{V_3}{40} = 0$$

$$1.235V_3 - 0.78125(20 - V_3) = 20$$

$$2.05625 V_3 - 15.625 = 20$$

$$V_3 =$$

Q(33):-

(mesh)

$$I_1 \Rightarrow -128 + 5I_1 + 60(I_1 - I_2) = 0$$

$$65I_1 - 60I_2 = 128$$

$$I_2 \Rightarrow 60I_2 - 60I_1 + 4I_2 + 80I_2 - 80I_3 = 0$$

$$144I_2 - 60I_1 - 80I_3 = 0$$

$$I_3 \Rightarrow 80I_3 - 80I_2 + 10I_3 + 320 = 0$$

$$90I_3 - 80I_2 = -320$$

$$\Rightarrow 65I_1 - 60I_2 = 128$$

$$-60I_1 + 144I_2 - 80I_3 = 0 \quad / 1.08333$$

$$\rightarrow 65I_1 - 60I_2 = 128$$

$$+ \quad -60I_1 + 156I_2 - 86.6667I_3 = 0$$

$$96I_2 - 86.6667I_3 = 128$$

$$\Rightarrow 96I_2 - 86.6667I_3 = 128$$

$$-80I_1 + 90I_3 = -320 \quad / 1.2$$

$$\rightarrow 96I_2 - 86.6667I_3 = 128$$

$$+ \quad -96I_2 + 108I_3 = 384$$

$$21.333I_3 = 256$$

$$\Rightarrow I_3 = -12A, \quad I_2 = -9.5A, \quad I_1 = -6.8A$$

a)

$$\Rightarrow I_b = -6.8 + 9.5 = 2.7A$$

$$I_d = -9.5 + 12 = 2.5A$$

$$b) P_{320} = (320)(-12) = \underline{-3840 \text{ W}}$$

$$P_{128} = -(128)(-68) = 8704 \text{ W}$$

Q(14):-

$$\bar{I}_1 \Rightarrow -125 + \bar{I}_1 + 6\bar{I}_1 - 6\bar{I}_3 + 2\bar{I}_1 - 2\bar{I}_2 = 0$$

$$9\bar{I}_1 - 2\bar{I}_2 - 6\bar{I}_3 = 125$$

$$\bar{I}_2 \Rightarrow -125 + 2\bar{I}_2 - 2\bar{I}_1 + 12\bar{I}_1 - 12\bar{I}_3 + \bar{I}_2 = 0$$

$$15\bar{I}_2 - 2\bar{I}_1 - 12\bar{I}_3 = 125$$

$$\bar{I}_3 \Rightarrow \frac{42\bar{I}_3}{6} - \frac{6\bar{I}_1}{6} - \frac{12\bar{I}_2}{6} = \frac{0}{6}$$

$$= 7\bar{I}_3 - \bar{I}_1 - 2\bar{I}_2 = 0$$

$$\bar{I}_1 = 23.76 \text{ A} \quad \bar{I}_2 = 18.43 \text{ A} \quad \bar{I}_3 = 8.66 \text{ A}$$

$$i_2 = 23.76 - 18.43 = 5.33 \text{ A}$$

$$a) i_4 = 23.76 - 8.66 = 15.10 \text{ A}$$

$$i_5 = 18.43 - 8.66 = 9.77 \text{ A}$$

$$b) \text{del} \Rightarrow -(125)(23.76) + (-125)(18.43) = -5273.75$$

$$\text{abs} \Rightarrow 5273.75 \text{ W}$$

Q(40):-

$$I_1 \Rightarrow -660 + 5I_1 + 15I_1 - 15I_2 + 10I_1 - 10I_2 = 0$$

$$30I_1 - 10I_2 - 15I_2 = 660 \quad /5$$

$$I_2 \Rightarrow -20(\textcircled{I_1}) + 10I_2 - 10I_1 + 50I_2 - 50I_3 = 0$$

$$-20(I_2 - I_3)$$

$$-20I_2 + 20I_3 + 60I_2 - 10I_1 - 50I_3 = 0$$

$$-10I_1 + 40I_2 - 30I_3 = 0 \quad /5$$

$$I_3 \Rightarrow -15I_1 - 50I_2 + 90I_3 = 0 \quad /5$$

$$\Rightarrow 6I_1 - 2I_2 - 3I_3 = 132$$

$$-2I_1 + 8I_2 - 6I_3 = 0 \quad /2$$

$$-3I_1 - 10I_2 + 18I_3 = 0$$

$$\begin{array}{r} \rightarrow 6I_1 - 2I_2 - 3I_3 = 132 \\ - \end{array}$$

$$-I_1 + 4I_2 - 3I_3 = 0$$

$$7I_1 - 6I_2 = 132$$

$$I_1 = 42 \text{ A} \quad , \quad I_2 = 27 \text{ A} \quad , \quad I_3 = 22 \text{ A}$$

$$I_0 = 5 \text{ A}$$

$$\Rightarrow P = (-20 \times 5)(27) = 2700 \text{ W}$$

Ex 40:-

$$I_1 \Rightarrow -40 + 425 I_1 - 300 I_D = 0$$

$$425 I_1 - 300 I_D = 40$$

$$I_2 \Rightarrow -500 I_D + 250 I_2 = 0$$

$$250 I_2 = 500 I_D$$

$$\boxed{I_2 = 2 I_D}$$

$$I_D \Rightarrow 400 I_D - 300 I_1 = 0$$

$$400 I_D = 300 I_1$$

$$\Rightarrow \boxed{4 I_D = 3 I_1}$$

$$\bullet I_D = \frac{3}{4} I_1$$

$$\bullet I_2 = 2 I_D = 2 \cdot \frac{3}{4} I_1 = \frac{3}{2} I_1$$

$$\rightarrow 425 I_1 - 300 \cdot \frac{3}{4} I_1 = 40$$

$$425 I_1 - 225 I_1 = 40 \Rightarrow I_1 = 0.2 \text{ A}, I_D = 0.15 \text{ A}$$

$$I_2 = 0.3 \text{ A}$$

$$P = (-0.3)(500)(0.15) = -22.5 \text{ W}$$

Q(47):-

$$i_0 = I_1 - I_2$$

$$I_1 \Rightarrow -30 + 30I_1 - 3I_2 - 20I_1 = 0$$

$$30I_1 - 20I_1 - 3I_2 = 30$$

$$I_2 \Rightarrow -30 + 27I_2 - 20I_1 - 5I_2 = 0$$

$$-20I_1 + 27I_2 - 5I_2 = 30$$

$$I_3 \Rightarrow 5I_2 + 53I_3 - 3I_1 - 5I_2 = 0$$

$$-3I_1 - 5I_2 + 5I_3 + 53(I_1 - I_2) = 0$$

$$(111) \quad 50I_1 - 58I_2 + 5I_3 = 0$$

$$\therefore I_1 = 152, \quad I_2 = 60A, \quad I_3 = 110A, \quad i_0 = -8A$$

$$\Rightarrow P = (110)(53)(-8) = -46640W$$

Q(48):-

$$I_1 \Rightarrow -50 + 2I_1 + 4I_2 - 4I_3 + 9i_0 = 0$$

$$6I_1 - 4I_2 + 9i_0 = 50, \quad 6I_1 + 5I_2 = 50$$

$$I_2 \Rightarrow -9i_0 + 4I_2 - 4I_1 + 5I_2 + 20I_1 - 20I_3 = 0$$

$$-9I_1 + 9I_2 - 4I_1 + 20I_2 - 20I_3 = 0$$

$$-4I_1 + 20I_2 - 20I_3 = 0$$

$$I_3 \Rightarrow I_3 = -1.7V_0 = -1.7(2I_1)$$

$$= -3.4I_1$$

$$\Rightarrow 6I_1 + 5I_2 = 50$$

$$6I_1 + 8I_2 = 50$$

$$64I_1 + 20I_2 = 0 / 4$$

$$16I_1 + 5I_2 = 0$$

$$-10I_1 = 50 \quad \therefore I_1 = -5A$$

$$I_1 = 16A = I_0$$

$$I_2 = 17A$$

$$\Rightarrow P_{50} = (-50)(-5) = +250 \text{ W}$$

$$\checkmark P_{910} = (-144)(16 - 5) = -3024 \text{ W}$$

$$\boxed{I_2 - I_1}$$

$$\checkmark P_{1.700} = (1.7 \times 20 - 5)(20)(16 - 17) = (17 \times -20) = -340 \text{ W}$$

$$\therefore \Sigma P_{del} = 3364 \text{ W.}$$

(min)

Q(13):-

$$\bullet -6 + \frac{V_1}{40} + \frac{V_1 - V_2}{8} = 0$$

$$\bullet -1 + \frac{V_2}{120} + \frac{V_2 - V_1}{8} + \frac{-V_2}{80} = 0$$

$$\therefore V_1 = 120 \text{ V}, \quad V_2 = 96 \text{ V.}$$

Q(14):-

$$\bullet \frac{V_1 - 40}{4} + \frac{V_1}{40} + \frac{V_1 - V_2}{2} = 0$$

$$\bullet \frac{V_2 - V_1}{2} = 28 + \frac{V_2 - V_3}{4} = 0$$

$$\bullet 28 + \frac{V_3}{2} + \frac{V_3 - V_2}{4} = 0$$

a) $\therefore V_1 = 60 \text{ V}, \quad V_2 = 73 \text{ V}, \quad V_3 = -15 \text{ V.}$

$$b) \quad I = \frac{(60 - 40)}{4} = 5A$$

$$P = (5)(40) = 200W$$

Q(19):-

$$20m + \frac{V_1}{1k} + \frac{V_1 - V_2}{1250} = 0$$

$$i_D = \frac{V_2 - V_1}{1250}$$

$$\frac{V_1 - V_1}{1250} + \frac{V_2}{4k} + \frac{V_1}{2k} + \frac{V_2 - 2500 i_D}{200} = 0$$

$$\therefore V_1 = 60V, \quad V_2 = 160V, \quad I_D = 80mA$$

$$a) \quad P_{20m\Omega} = (20 \times 10^{-3})(60) = 1.2W \text{ abs.}$$

$$P_{2500\Omega} = \frac{12500 i_D}{200} \frac{160 - 2500(80 \times 10^{-3})}{200} = -40W \text{ del.}$$

\therefore it's $-40W$ del.

$$b) \quad P_{1k} = \frac{(60)^2}{1000} = 3.6W$$

$$P_{2k} = \frac{(160)^2}{2000} = 12.8W$$

$$P_{1250} = \frac{(160 - 60)^2}{1250} = 8W$$

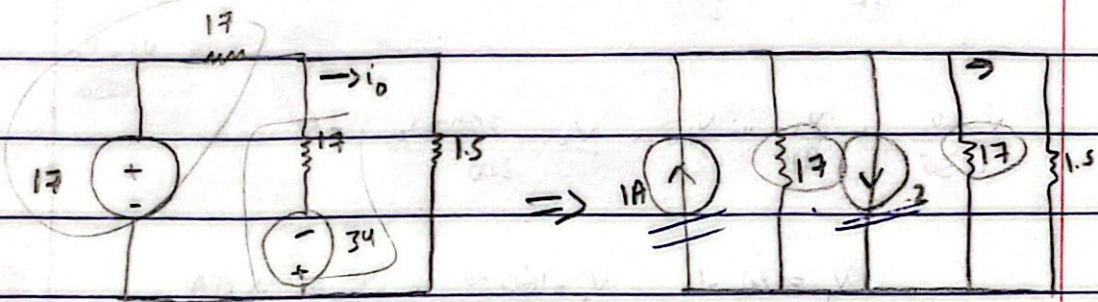
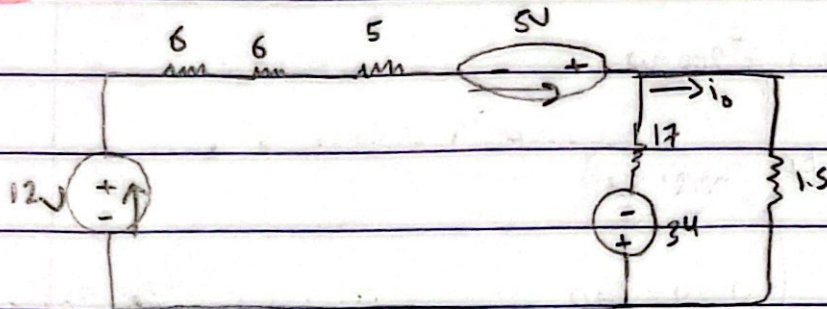
$$P_{200} = \frac{(160 - (2500(80 \times 10^{-3})))^2}{200} = 8W$$

$$P_{4k} = \frac{(160)^2}{4000} = 6.4W$$

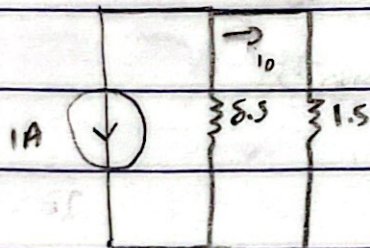
$$\therefore \text{it's} = 3.6 + 8 + 6.4 + 12.8 + 8 + 1.2$$

$$= 40W$$

Q(62):-



a)



$$\therefore i_o = \frac{8.5}{8.5 + 1.5} \times 1 = -0.85 \text{ A}$$

b)

$$6(I_1 - 2) + 6I_1 + 5(I_1 - 1) + 17(I_1 - I_2) - 34 = 0$$

$$6I_1 - 12 + 6I_1 + 5I_1 - 5 + 17I_1 - 17I_2 - 34 = 0$$

$$34I_1 - 17I_2 = 51$$

$$34 + 17(I_2 - I_1) + 1.5I_2 = 0$$

$$34 + 17I_2 - 17I_1 + 1.5I_2 = 0$$

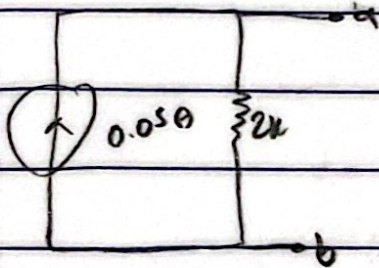
$$-17I_1 + 18.5I_2 = -34$$

$$\therefore i_o = -0.85 \text{ A}$$

Q(65):-

$$R_N = R_{th} = 4k // 2k \\ = 2k \Omega$$

$$CD \Rightarrow \frac{(4 // 2)k (75 \times 10^{-3})}{2k} = 0.05 A$$



• we can solve it by mesh too.

Q(66):-

$$I_1 = 4A$$

$$\Rightarrow -60 + 10(I_1 - 4) + 40(I_1 - I_2) = 0$$

$$-60 + 50I_1 - 40 - 40I_2 = 0$$

$$100 = 50I_1 - 40I_2 \Rightarrow 5I_1 - 4I_2 = 10$$

$$\Rightarrow 40(I_2 - I_1) + 8(I_2 - 4) = 0$$

$$40I_2 - 40I_1 + 8I_2 - 32 = 0$$

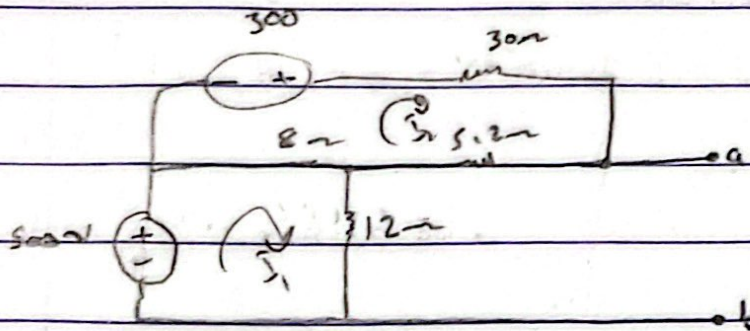
$$32 = 48I_2 - 40I_1 \Rightarrow 6I_2 - 5I_1 = 4$$

$$\Rightarrow \begin{array}{l} 5I_1 - 4I_2 = 10 \\ + \quad -I_1 + 6I_2 = 4 \end{array} \quad \begin{array}{l} 2I_2 = 14 \\ \boxed{I_2 = 7A = I_{th}} \end{array}$$

$$\Rightarrow R_{th} = R_N = (10 // 40) + 8 = 16 \Omega$$

Q(63):-

we start with source transformation:-



$$\Rightarrow -500 + 20\bar{I}_1 - 8\bar{I}_2 = 0.$$

$$20\bar{I}_1 - 8\bar{I}_2 = 500 \quad \Rightarrow \quad 4\bar{I}_1 - 1.6\bar{I}_2 = 100.$$

$$\Rightarrow -300 + 35.2\bar{I}_2 + 8\bar{I}_2 - 8\bar{I}_1 = 0.$$

$$43.2\bar{I}_2 - 8\bar{I}_1 = 300 \quad \Rightarrow \quad 21.6\bar{I}_2 - 4\bar{I}_1 = 150.$$

$$\therefore 20\bar{I}_2 = 250$$

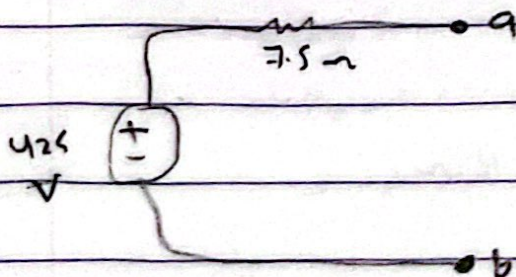
$$\therefore \bar{I}_2 = 12.5 \text{ A.}$$

$$\therefore 4\bar{I}_1 - 1.6 \times 12.5 = 100.$$

$$\therefore \bar{I}_1 = 30 \text{ A.}$$

$$\Rightarrow V_{th} = 5.2(12.5) + 12(30) = 425 \text{ V}$$

$$R_{th} = (12 \parallel 12) + 5.2 \parallel 30 = 7.5 \Omega$$



Q (74):-

$$\begin{aligned} \text{mesh } \Rightarrow -100 + 2500 i_1 + 625 (i_1 + 10^{-3} V_2) &= 0 \\ 100 &= 2500 i_1 + 625 i_1 + 10^{-3} V_2 (625) \\ 100 &= 3125 i_1 + 0.625 V_2 \\ 100 &= 3125 i_1 + 0.625 (6000 i_1) \\ 100 &= 3125 i_1 + 3750 i_1 \\ 100 &= 6875 i_1 + 3750 (0.5) i_1 \\ \boxed{i_1 = 0.02 \text{ A}} \end{aligned}$$

$$\begin{aligned} \Rightarrow -5000 i_1 + 4000 i_2 + 6000 i_3 &= 0 \\ -5000 i_1 + 10000 i_3 &= 0 \\ i_3 = \frac{5000 i_1}{10000} = 0.5 i_1 \end{aligned}$$

$$\boxed{i_3 = 0.01}$$

$$\Rightarrow V_{2c} = V_{s.c} = V_2 = 6000 \times 0.01 = \underline{\underline{60 \text{ V}}}$$

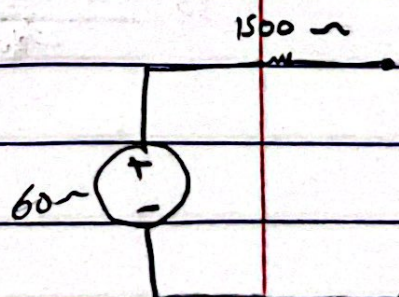
$$\bullet \quad V = IR$$

$$5000 i_1 = 4000 i_{s.c}$$

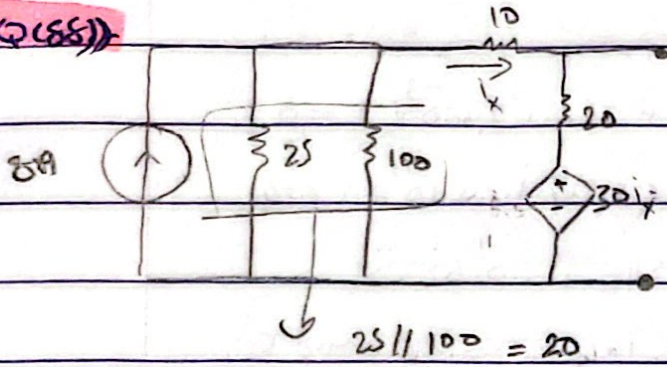
$$\therefore i_{s.c} = \frac{5000 i_1}{4000} \Rightarrow 0.04 \text{ A}$$

$$\bullet \quad i_1 = \frac{100}{2500 + 625} = 0.032 \text{ A}$$

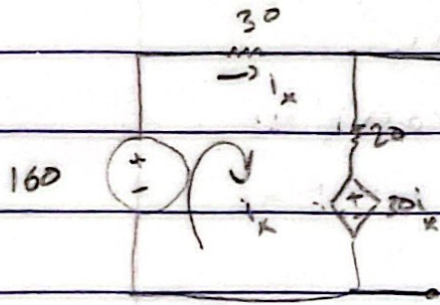
$$\therefore R_{Th} = \frac{60}{0.04} = 1500 \Omega$$



Q(55)



$$25 \parallel 100 = 20$$

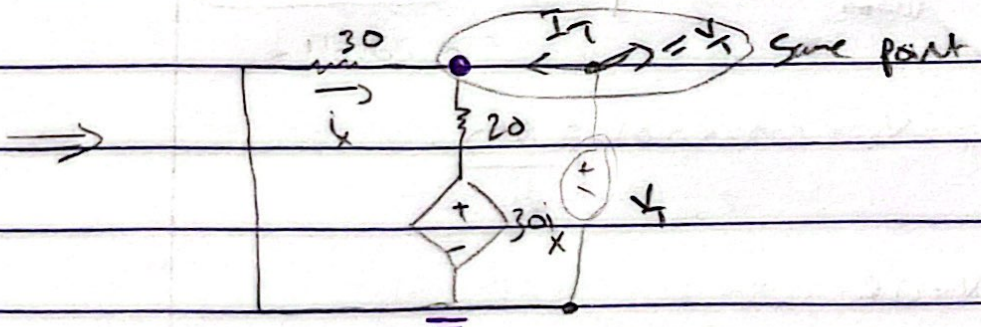
KVL \Rightarrow

$$-160 + 30i_x + 30i_x + 30i_x = 0$$

$$160 = 90i_x$$

$$i_x = 2 \text{ A}$$

$$\Rightarrow V_{1x} = 50(2) = 100 \text{ V}$$



$$\frac{V_1}{30} + \frac{V_1 - 30i_x}{20} - I_T = 0$$

$$\frac{V_1}{30} + \frac{V_1 - 30(-V_1/30)}{20} = I_T \Rightarrow \frac{V_1}{30} + \frac{V_1 + \frac{30V_1}{30}}{20} = I_T$$

$$\frac{V_1}{30} + \frac{2V_1}{10} = I_T$$

$$\frac{I_T}{V_1} = \frac{1}{30} + \frac{1}{10} = 0.1333$$

$$R_{Th} = 7.5 \Omega$$

$$\Rightarrow P_{max} = \left(\frac{V_{th}}{R_{th} + R_L} \right)^2 R_L = 250$$

$$= \left(\frac{100}{7.5 + R_L} \right)^2 R_L = \frac{10000}{56.25 + R_L^2 + 15R_L} \quad R_L = 250$$

$$0.025 = \frac{R_L}{\cancel{X}}$$

$$0.025R_L^2 + 0.375R_L + 1.40625 = R_L$$

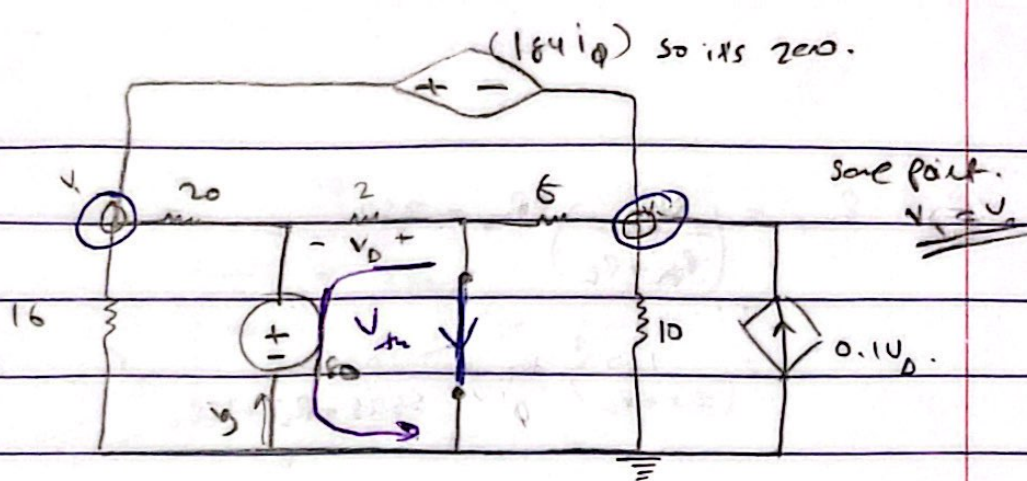
$$0.025R_L^2 - 0.625R_L + 1.40625 = 0$$

$$R_L^2 - 25R_L + 56.25 = 0$$

$$(R_L - 22.5)(R_L - 2.5)$$

$$\therefore R_L = 22.5 / +2.5$$

Q(89):-



a)

nodal:-

$$\frac{V_1}{16} + \frac{V_1 - 180}{20} + \frac{V_1}{10} + \frac{V_2 - 180}{10} - 0.1V_D = 0$$

$$\frac{V_1}{16} + \frac{V_1}{20} = 9 + \frac{V_1}{10} + \frac{V_1}{10} - 0.1V_D = 0$$

$$0.1V_D = \frac{(V_1 - 180) \times 2}{10}$$

$$= \frac{V_1}{5} - 36$$

$$= 0.2V_1 - 36$$

$$0.3125V_1 - 27 - 0.1(0.2V_1 - 36) = 0$$

$$0.3125V_1 - 27 - 0.02V_1 + 3.6 = 0$$

$$0.2925V_1 = 23.4$$

$$V_1 = 80V$$

$$V_D = -20V$$

$$V_2 = V_D = 180 + V_D$$

$$= 180 - 20 = 160V$$

$$\Rightarrow \frac{V_1}{16} + \frac{V_1 - 180}{20} + \frac{V_2}{8} + \frac{V_2}{10} - 0.1V_D = 0$$

$$V_1 - V_2 = 184 i_\phi$$

$$V_1 = V_2 + 184 i_\phi$$

$$i_\phi = \frac{V_2 + 180}{8} = 90 + 0.125V_2$$

$$\Rightarrow \frac{V_1}{16} + \frac{V_1}{20} = 9 + \frac{V_2}{8} + \frac{V_2}{10} - 0.1(-180) = 0$$

$$= 0.1125V_1 - 9 + 0.225V_2 + 18 = 0 \Rightarrow 0.1125V_1 + 0.225V_2 = -9$$

$$\Rightarrow V_1 = V_2 + 184(0.125V_2 + 90)$$

$$= V_2 + 23V_2 + 16560$$

$$\Rightarrow 0.1125(24V_2 + 16560) + 0.225V_2 = -9$$

$$2.7V_2 + 1863 + 0.225V_2 = -9$$

$$2.925V_2 = -1872$$

$$\boxed{V_2 = -640 \text{ V}}$$

$$V_1 = 24V_2 + 16560 = 24(-640) + 16560$$

$$\boxed{V_1 = 1200 \text{ V}}$$

$$\Rightarrow i_q = I_{sc} = 90 + 0.125(-640)$$

$$\underline{\underline{= 10 \text{ A}}}$$

$$\therefore R_{th} = \frac{V_{oc}}{I_{sc}} = \frac{160}{10} = 16 \Omega = R_o = R_L$$

$$b) P_{max} = \frac{(160)^2}{(16)(4)} = 400 \text{ W}$$

$$c) \text{ the voltage at } R_o = \frac{16}{16+16} \cdot 160 = 80 \text{ V} \Rightarrow \text{from maximum power}$$

we should have i_g

$$\frac{V_1}{16} + \frac{V_1 - 180}{20} + \frac{V_2 - 80}{8} + \frac{V_2}{10} + 0.1(80 - 180) = 0$$

$$V_1 = V_2 + 184 i_q \quad i_q = \frac{80 - 180}{16} = -5 \text{ A}$$

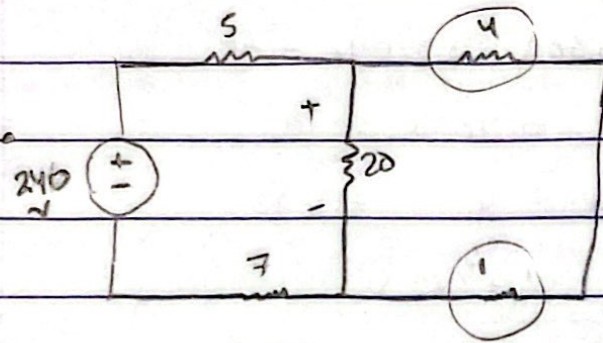
$$V_1 = V_2 + 920$$

$$V_1 = 640 \text{ V}, V_2 = -280 \text{ V}$$

$$\Rightarrow i_g = \frac{180 - 80}{20} + \frac{180 - 640}{20} = -27 \text{ A}$$

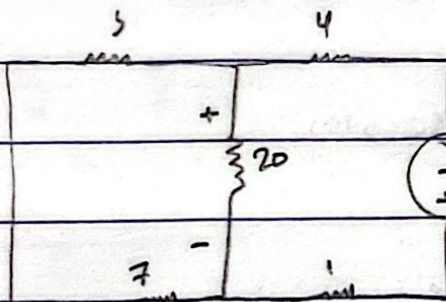
$$P = 27 \cdot 180 = 4860 \text{ W}$$

Q(96):-



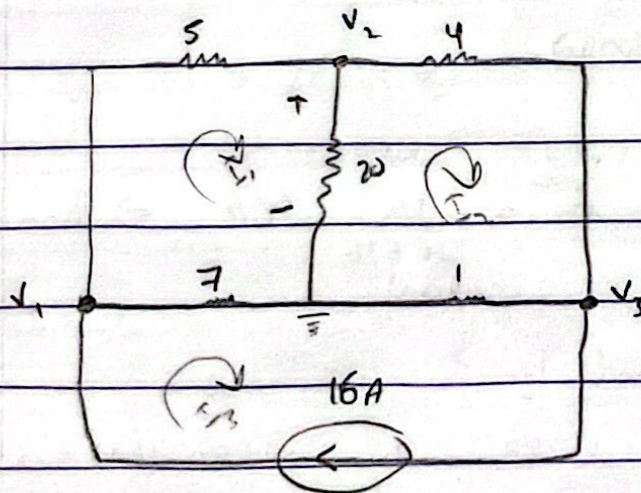
$$4 + 1 = 5 \Omega$$

$$1) \frac{20 \parallel 5}{(20 \parallel 5) + 12} \cdot 240 = 60V$$



$$5 + 7 = 12$$

$$2) \frac{(12 \parallel 20)}{(12 \parallel 20) + 5} \cdot -64 = -50.4V$$



$$\frac{V_1 - V_2}{5} + \frac{V_1}{7} - 16 = 0$$

$$\Rightarrow 0.34V_1 - 0.2V_2 = 16$$

$$\frac{V_2 - V_1}{5} + \frac{V_2 - V_3}{4} + \frac{V_2}{20} = 0$$

$$\Rightarrow 0.5V_2 - 0.2V_1 - 0.25V_3 = 0$$

$$\frac{V_2 - V_1}{4} + \frac{V_3}{1} + 16 = 0$$

$$\Rightarrow 1.25V_3 - 0.25V_2 = -16$$

$$\Rightarrow 2.5V_2 - V_1 - 1.25V_3 = 0$$

$$\Rightarrow 2.5V_2 - V_1 - 1.25V_3 = 0$$

$$+ \quad 1.25V_3 - 0.25V_2 = -16$$

$$2.25V_2 - V_1 = -16 \quad / \quad 0.34$$

$$\Rightarrow 0.765V_2 - 0.34V_1 = 5.44$$

$$+ \quad 0.2V_2 - 0.34V_1 = 16$$

$$0.969V_2 = 21.44$$

$$\therefore V_2 = 22.2 = 13$$

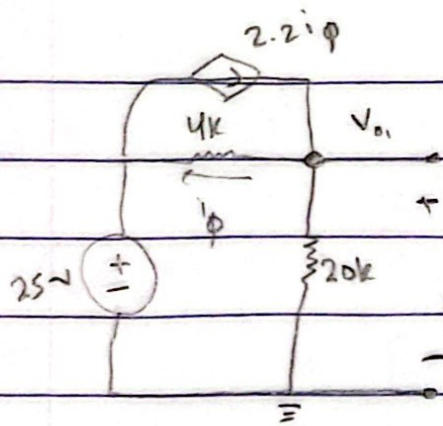
• Something wrong in calculation of V_2

$$\therefore V_0 = 1 + 2 + 3$$

$$= 60 - 50.4 + \underline{16.4}$$

$$= 26 \text{ V}$$

Q(44):-



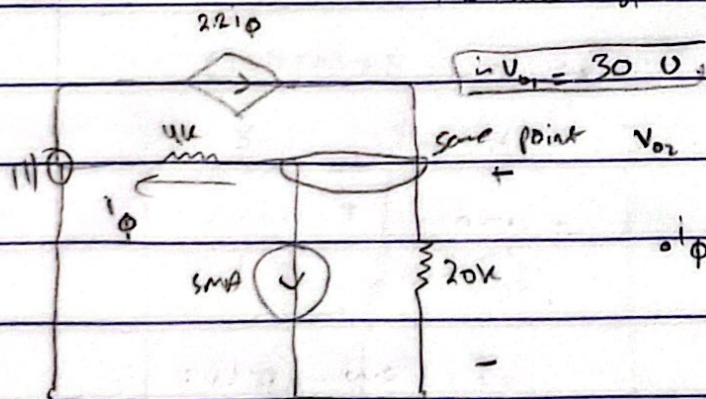
$$i_\phi = \frac{V_o1 - 25}{4000}$$

$$V_o1 \Rightarrow \frac{V_o1 - 25}{4000} + \frac{V_o1}{20000} - 2.2 i_\phi = 0$$

$$= \frac{V_o1}{4000} - \frac{25}{4000} + \frac{V_o1}{20000} - 2.2 \left(\frac{V_o1 - 25}{4000} \right) = 0$$

$$3 \times 10^{-4} V_o1 - 6.25 \times 10^{-3} - 5.5 \times 10^{-4} V_o1 + 0.01375 = 0$$

$$+ 2.5 \times 10^{-4} V_o1 = -7.5 \times 10^{-3}$$



$$i_\phi = \frac{V_o2}{4000}$$

$$V_o2 \Rightarrow \frac{V_o2}{4000} + \frac{V_o2}{20000} + 5 \times 10^{-3} - 2.2 \left(\frac{V_o2}{4000} \right) = 0$$

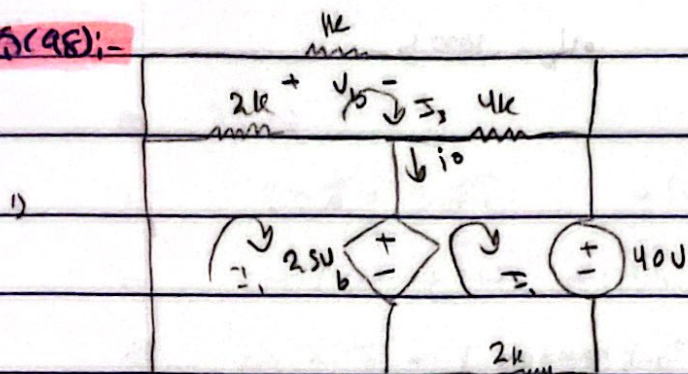
$$- 2.5 \times 10^{-4} V_o2 = -5 \times 10^{-3}$$

$$i_\phi = 20 \text{ V}$$

$$i_\phi = V_o1 + V_o2 = 30 + 20$$

$$= 50 \text{ V}$$

Q(98):-



$$V_b = 1000 i_3$$

$$2000(i_1 - i_3) + 25V_b = 0 \Rightarrow 2000i_1 - 2000i_3 + 25V_b = 0$$

$$2000i_1 - 2000i_3 + 25(1000i_3) = 0 \Rightarrow 2000i_1 + 500i_3 = 0$$

$$6000i_2 - 4000i_3 = 25V_b = -40 \Rightarrow 6000i_2 - 1500i_3 = -40$$

$$7000i_3 - 4000i_2 - 2000i_1 = 0$$

$$-2000i_1 - 4000i_2 + 7000i_3 = 0$$

$$+ 2000i_1 + 500i_3 = 0$$

$$-4000i_2 + 1500i_3 = 0$$

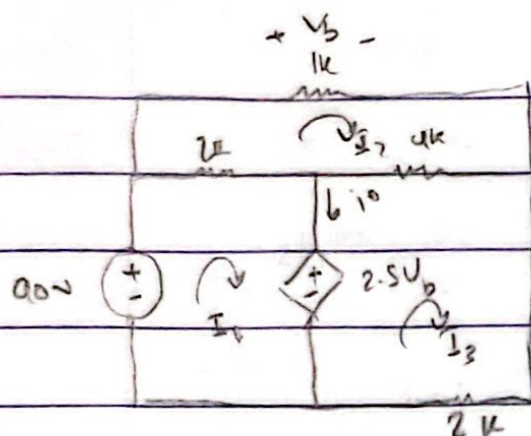
$$+ 6000i_2 - 1500i_3 = -40 \cdot 5$$

$$\rightarrow 30000i_2 - 7500i_3 = 200$$

$$26000i_2 = -200$$

$$\therefore i_2 =$$

$$i^* = i_1 - i_2 = 17.895 \text{ A}$$



$$V_b = 1000 i_2$$

$$90 = 2000 i_1 - 2000 i_2 + 2.5(1000 i_2)$$

$$90 = 2000 i_1 + 500 i_2$$

$$7000 i_2 - 4000 i_2 - 2000 i_1 = 0$$

$$6000 i_2 - 4000 i_2 - 2.5(1000 i_2) = 0$$

$$6000 i_2 - 6500 i_2 = 0$$

$$\Rightarrow 2000 i_1 + 500 i_2 = 90$$

$$-2000 i_1 + 7000 i_2 - 4000 i_2 = 0$$

$$7500 i_2 - 4000 i_2 = 90 / 1.5$$

$$\Rightarrow 11250 i_2 - 6000 i_2 = 135$$

$$-6500 i_2 + 6000 i_2 = 0$$

$$4750 i_2 = 135$$

$$i_2 = 0.0284 \text{ A}$$

$$i_3 = 0.03078 \text{ A}$$

$$i_1 = 0.03865 \text{ A}$$

$$i = i_1 - i_3 = 7.87 \text{ mA}$$

$$I = 7.87 \text{ mA} + 17.893 = 25 \text{ mA}$$

Q(3):-

a) 25 N .

b) $400\pi = 2\pi f$. $\therefore f = 200 \text{ Hz}$.

c) $\text{rad/sec} = \omega = 1256.6 \text{ rad/sec}$.

d) $60 \times \frac{\pi}{180} = 1.047 \text{ rad}$.

e) 60°

f) $\frac{1}{200} = 5 \text{ msec}$.

g) $v = 25 \cos(400\pi t + 60^\circ)$.

$$\cos^{-1} 0 = 400\pi t + 60^\circ$$

$$90 - 60 = 400\pi t \quad (90 - 60) / 400\pi = t$$

$$\therefore t = 6.02387 \times 10^{-3} \text{ s}$$

$$\Rightarrow \frac{\pi}{2} - \frac{\pi}{3} = 400\pi t$$

$$\frac{\pi}{6} = 400\pi t$$

$$\frac{1}{2400} = t = 4.166 \times 10^{-3}$$

h) $25 \cos(400\pi [t - 0.005] + \frac{\pi}{3})$ quite more right so (-)

$$25 \cos(400\pi t - \frac{\pi}{3} + \frac{\pi}{3}) = 25 \cos(400\pi t)$$

i)

Q(6):-

$$V_m = \sqrt{2} V_{rms} = \sqrt{2} \cdot 240 \\ = 339.41 \text{ V}$$

Q(7):-

$$\begin{aligned} & -\sin \frac{+90}{-90} \cos \\ & \sin \frac{-90}{180} \\ & (-\cos \frac{180}{180}) \end{aligned}$$

Q(11):-

a) $y = 30 \cos(200t - 160^\circ) + 15 \cos(200t + 70^\circ)$

$$= 30 \angle -160^\circ + 15 \angle 70^\circ$$

$$= -30 \angle 20^\circ + 15 \angle 70^\circ$$

$$= -28.19 + 10j + 5.13 + 14.09j$$

$$= -23.06 + 24.09j$$

$$= 26.19 \angle 134^\circ$$

$$30 \angle -160 + 15 \angle 70$$

$$-\sin (30)$$

$$-100 \angle -60^\circ$$

$$100 \angle 120$$

$$-28.19 + 10j + 5.13 + 14.09j$$

$$-23.06 + 24.09j$$

Q(w):-

$$\begin{aligned} \text{a) } Z &= \frac{300}{6} \angle 78^\circ - 33^\circ \\ &= 50 \angle 45^\circ \end{aligned} \quad \text{1 loop U by } 45^\circ$$

$$\text{b) } 3\pi f = 5000\pi$$

$$\Rightarrow f = 2500 \text{ Hz} \Rightarrow T = 4 \times 10^{-4} \text{ sec.}$$

$$= 400 \mu\text{sec.}$$

$$\frac{45^\circ}{360^\circ} \times 400 \mu = 50 \mu\text{sec}$$

Q(12):

$$(5 + j8 + 10 \parallel -j20) + (8 + j16) \parallel (40 - j80)$$

$$(15 + j8 \parallel -j20) + (8 + j16) \parallel (40 - j80)$$

$$\frac{-j20(15 + j8)}{15 + j8 - j20} + \frac{(8 + j16)(40 - j80)}{8 + j16 + 40 - j80}$$

$$= \frac{-300j + 160}{15 - 12j} +$$

and so on

$$I_{1c} = 32.02 \angle 38.66^\circ$$

Q(14):

$$V_0 = 60 \cos(6000t - 90^\circ)$$

$$\frac{50 \parallel -25j}{2j + (50 \parallel -25j)} \Rightarrow \frac{-1250j}{50 - 25j} \Rightarrow \frac{25j + \frac{-1250j}{50 - 25j}}{50 - 25j}$$

$$\Rightarrow \frac{1250 \angle -90}{55.9 \angle -26.56} = 22.36 \angle -63.44 = 9.997 + 20j$$

$$\Rightarrow \frac{22.36 \angle -63.44}{9.997 + 5j} = \frac{22.36 \angle -63.44}{11.177 \angle 26.57}$$

$$= 2 \angle -90^\circ$$

$$\approx 2 \angle -90^\circ \approx 60 \angle -90^\circ$$

$$= 120 \angle -180^\circ$$