

Chapter 12

Simple Linear Regression

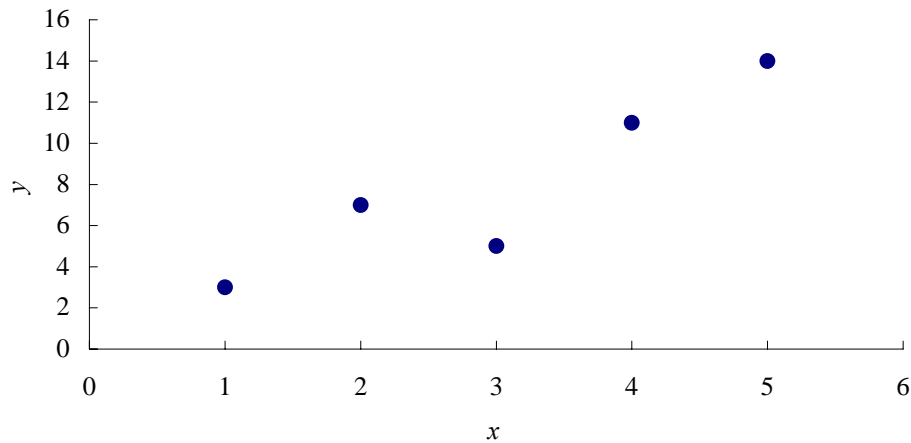
Learning Objectives

1. Understand how regression analysis can be used to develop an equation that estimates mathematically how two variables are related.
2. Understand the differences between the regression model, the regression equation, and the estimated regression equation.
3. Know how to fit an estimated regression equation to a set of sample data based upon the least-squares method.
4. Be able to determine how good a fit is provided by the estimated regression equation and compute the sample correlation coefficient from the regression analysis output.
5. Understand the assumptions necessary for statistical inference and be able to test for a significant relationship.
6. Know how to develop confidence interval estimates of y given a specific value of x in both the case of a mean value of y and an individual value of y .
7. Learn how to use a residual plot to make a judgement as to the validity of the regression assumptions.
8. Know the definition of the following terms:
 - independent and dependent variable
 - simple linear regression
 - regression model
 - regression equation and estimated regression equation
 - scatter diagram
 - coefficient of determination
 - standard error of the estimate
 - confidence interval
 - prediction interval
 - residual plot

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Solutions:

1 a.



- b. There appears to be a positive linear relationship between x and y .
- c. Many different straight lines can be drawn to provide a linear approximation of the relationship between x and y ; in part (d) we will determine the equation of a straight line that “best” represents the relationship according to the least squares criterion.

$$d. \quad \bar{x} = \frac{\sum x_i}{n} = \frac{15}{5} = 3 \quad \bar{y} = \frac{\sum y_i}{n} = \frac{40}{5} = 8$$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 26 \quad \sum (x_i - \bar{x})^2 = 10$$

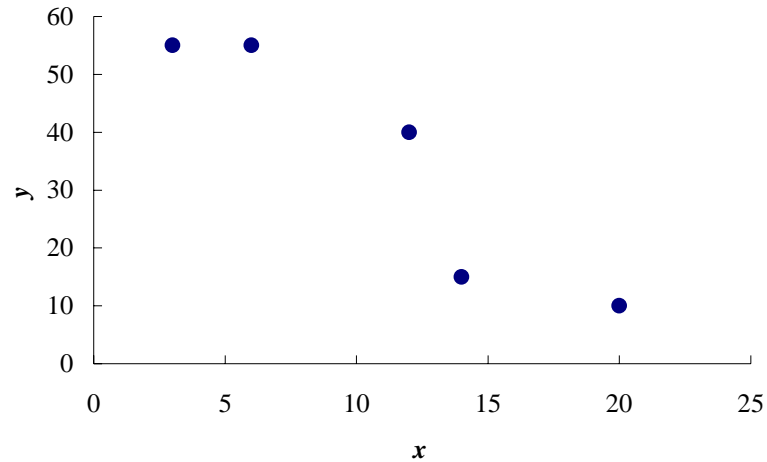
$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{26}{10} = 2.6$$

$$b_0 = \bar{y} - b_1 \bar{x} = 8 - (2.6)(3) = 0.2$$

$$\hat{y} = 0.2 + 2.6x$$

e. $\hat{y} = 0.2 + 2.6(4) = 10.6$

2. a.



- b. There appears to be a negative linear relationship between x and y .
- c. Many different straight lines can be drawn to provide a linear approximation of the relationship between x and y ; in part (d) we will determine the equation of a straight line that “best” represents the relationship according to the least squares criterion.

$$d. \quad \bar{x} = \frac{\sum x_i}{n} = \frac{55}{5} = 11 \quad \bar{y} = \frac{\sum y_i}{n} = \frac{175}{5} = 35$$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = -540 \quad \sum (x_i - \bar{x})^2 = 180$$

$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{-540}{180} = -3$$

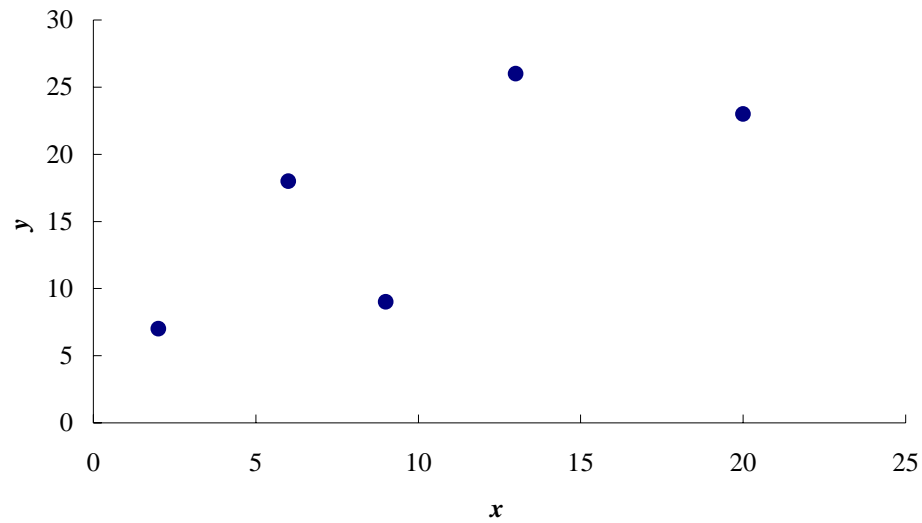
$$b_0 = \bar{y} - b_1\bar{x} = 35 - (-3)(11) = 68$$

$$\hat{y} = 68 - 3x$$

e. $\hat{y} = 68 - 3(10) = 38$

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3. a.



b. $\bar{x} = \frac{\sum x_i}{n} = \frac{50}{5} = 10$ $\bar{y} = \frac{\sum y_i}{n} = \frac{83}{5} = 16.6$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 171 \quad \sum (x_i - \bar{x})^2 = 190$$

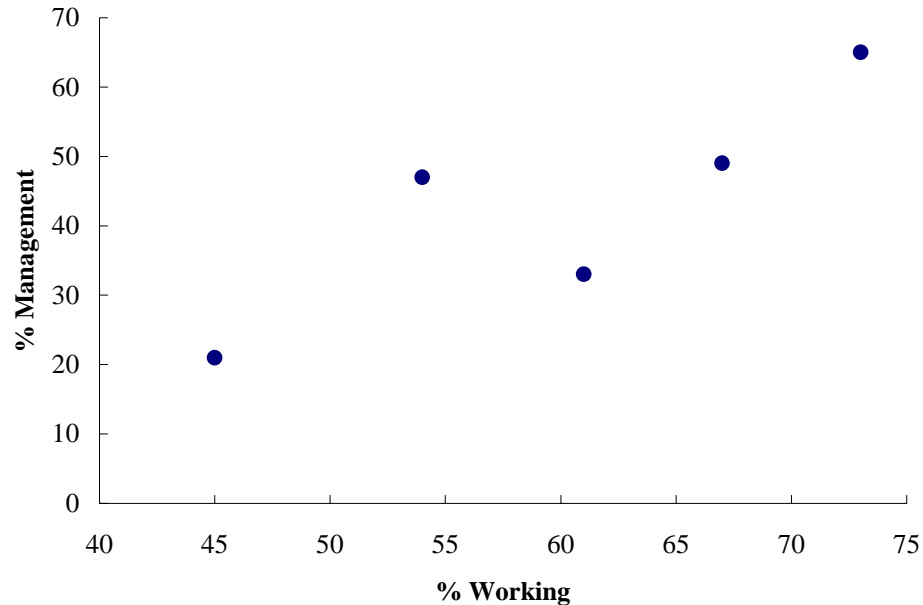
$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{171}{190} = 0.9$$

$$b_0 = \bar{y} - b_1\bar{x} = 16.6 - (0.9)(10) = 7.6$$

$$\hat{y} = 7.6 + 0.9x$$

c. $\hat{y} = 7.6 + 0.9(6) = 13$

4. a.



- b. There appears to be a positive linear relationship between the percentage of women working in the five companies (x) the percentage of management jobs held by women in that company (y)
- c. Many different straight lines can be drawn to provide a linear approximation of the relationship between x and y ; in part (d) we will determine the equation of a straight line that “best” represents the relationship according to the least squares criterion.

$$d. \quad \bar{x} = \frac{\sum x_i}{n} = \frac{300}{5} = 60 \quad \bar{y} = \frac{\sum y_i}{n} = \frac{215}{5} = 43$$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 624 \quad \sum (x_i - \bar{x})^2 = 480$$

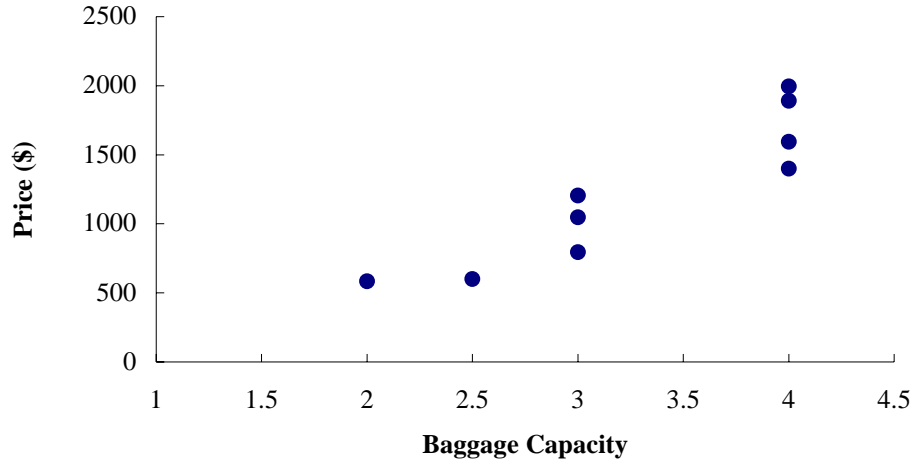
$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{624}{480} = 1.3$$

$$\hat{y} = -35 + 1.3x$$

e. $\hat{y} = -35 + 1.3x = -35 + 1.3(60) = 43\%$

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5. a.



b. Let x = baggage capacity and y = price (\$).

There appears to be a positive linear relationship between x and y .

c. Many different straight lines can be drawn to provide a linear approximation of the relationship between x and y ; in part (d) we will determine the equation of a straight line that “best” represents the relationship according to the least squares criterion.

$$d. \quad \bar{x} = \frac{\sum x_i}{n} = \frac{29.5}{9} = 3.277778 \quad \bar{y} = \frac{\sum y_i}{n} = \frac{11,110}{9} = 1234.444444$$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 2909.888891 \quad \sum (x_i - \bar{x})^2 = 4.555559$$

$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{2909.888891}{4.555559} = 638.755615$$

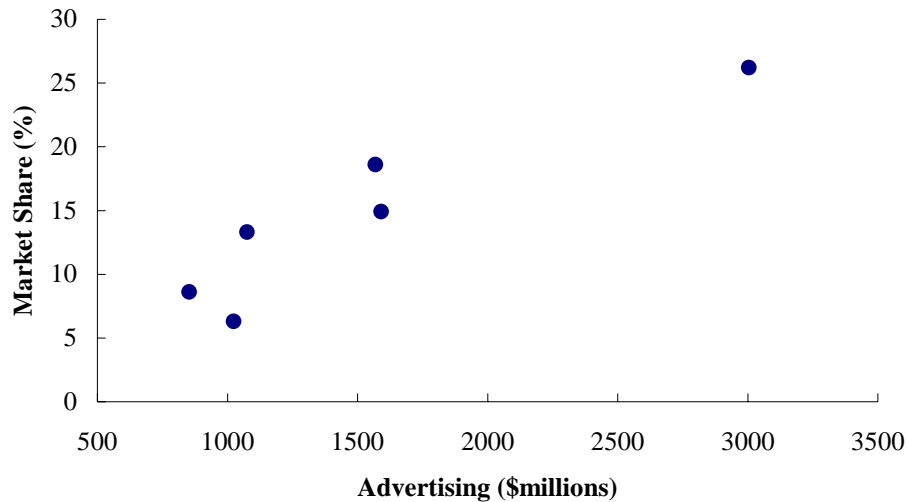
$$b_0 = \bar{y} - b_1 \bar{x} = 1234.4444 - (638.7561)(3.2778) = -859.254658$$

$$\hat{y} = -859.26 + 638.76x$$

e. A one point increase in the baggage capacity rating will increase the price by approximately \$639.

$$f. \quad \hat{y} = -859.26 + 638.76x = -859.26 + 638.76(3) = \$1057$$

6. a.



b. There appears to be a positive linear relationship between advertising expenditure and market share.

$$c. \quad \bar{x} = \frac{\sum x_i}{n} = \frac{9114}{6} = 1519 \quad \bar{y} = \frac{\sum y_i}{n} = \frac{87.9}{6} = 14.65$$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 26,127.3 \quad \sum (x_i - \bar{x})^2 = 3,098,044$$

$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{26,127.3}{3,098,044} = .00843348$$

$$b_0 = \bar{y} - b_1 \bar{x} = 14.65 - (.00843348)(1519) = 1.8395$$

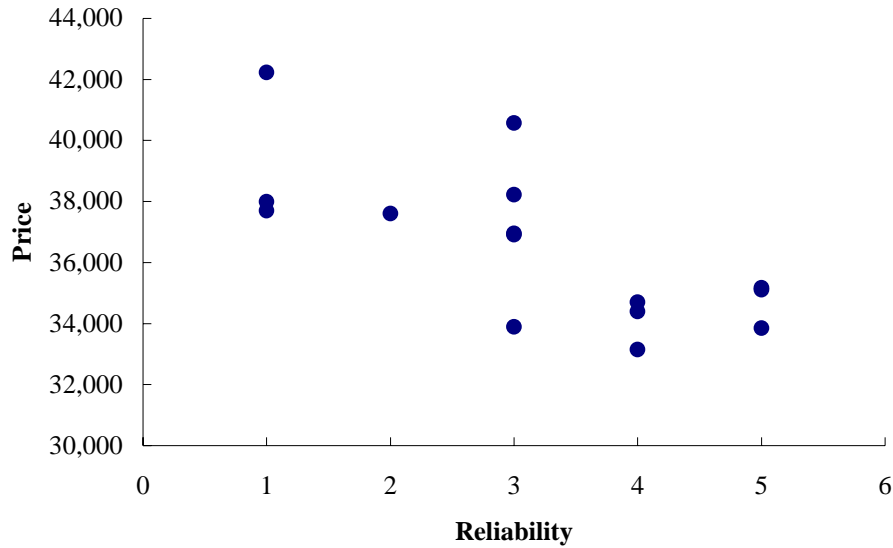
$$\hat{y} = 1.8395 + .0084x$$

d. A one unit increase in advertising expenditure will increase the market share by .0084. Because advertising expenditure is measure in \$million, an increase of \$100 million would increase the market share by .84%.

$$e. \quad \hat{y} = 1.8395 + .0084x = 1.8395 + .0084(1200) = 11.9 \text{ or } 11.9\%$$

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7. a.



b. $\bar{x} = \Sigma x_i / n = 47 / 15 = 3.1333$ $\bar{y} = \Sigma y_i / n = 548,434 / 15 = 36,562.2667$

$$\Sigma(x_i - \bar{x})(y_i - \bar{y}) = -36,086.5333 \quad \Sigma(x_i - \bar{x})^2 = 27.7333$$

$$b_1 = \frac{\Sigma(x_i - \bar{x})(y_i - \bar{y})}{\Sigma(x_i - \bar{x})^2} = \frac{-36,086.5333}{27.7333} = -1301.1987$$

$$b_0 = \bar{y} - b_1\bar{x} = 36,562.2667 - (-1301.1987)(3.1333) = 40,639.3126$$

$$\hat{y} = 40,639 - 1301.2x$$

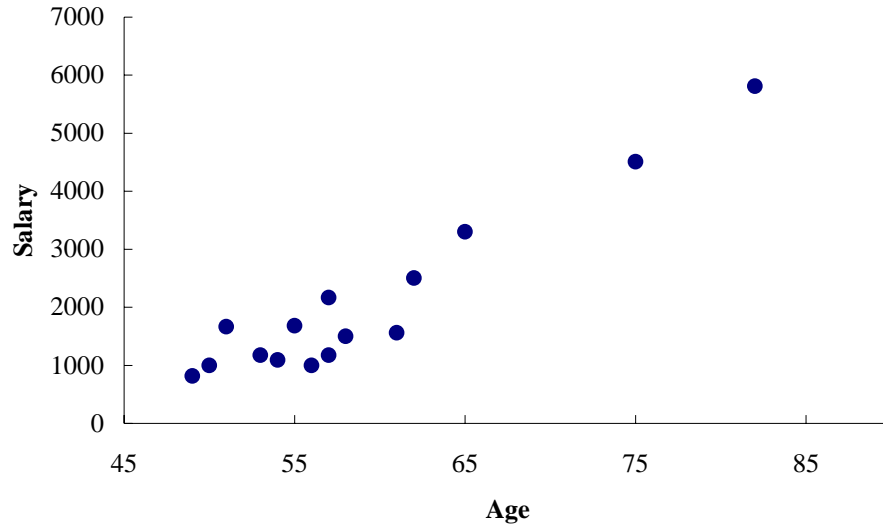
- c. The scatter diagram and the slope of the estimated regression equation indicate a negative linear relationship between reliability and price. Thus, it appears that higher reliable cars actually cost less. Although this result may surprise you, it may be due to the fact that higher priced cars have more options that may increase the likelihood of problems.

- d. A car with a good reliability rating corresponds to $x = 3$.

$$\hat{y} = 40,639 - 1301.2x = 40,639 - 1301.2(3) = 36,735.40$$

Thus, the estimate of the price of an upscale sedan with a good reliability rating is approximately \$36,735.

8. a.



b. There appears to be a positive linear relationship between age and salary.

$$c. \quad \bar{x} = \frac{\sum x_i}{n} = \frac{885}{15} = 59 \quad \bar{y} = \frac{\sum y_i}{n} = \frac{30,939}{15} = 2062.6$$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 175,265 \quad \sum (x_i - \bar{x})^2 = 1174$$

$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{175,265}{1174} = 149.2888$$

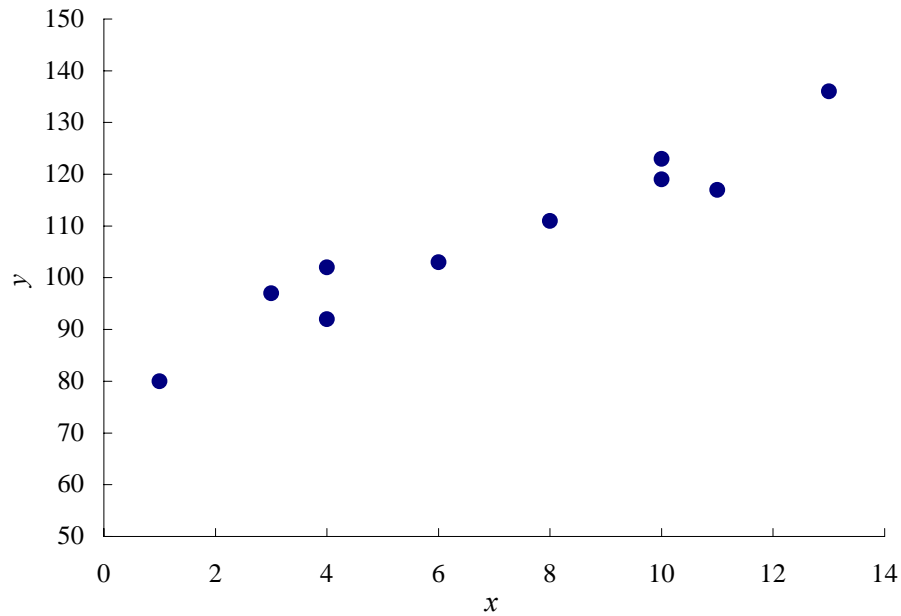
$$b_0 = \bar{y} - b_1 \bar{x} = 2062.6 - (149.2888)(59) = -6745.44$$

$$\hat{y} = -6745.44 + 149.29x$$

$$e. \quad \hat{y} = -6745.44 + 149.29x = -6745.44 + 149.29(72) = \$4003$$

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9. a.



b. $\bar{x} = \frac{\sum x_i}{n} = \frac{70}{10} = 7$ $\bar{y} = \frac{\sum y_i}{n} = \frac{1080}{10} = 108$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 568 \quad \sum (x_i - \bar{x})^2 = 142$$

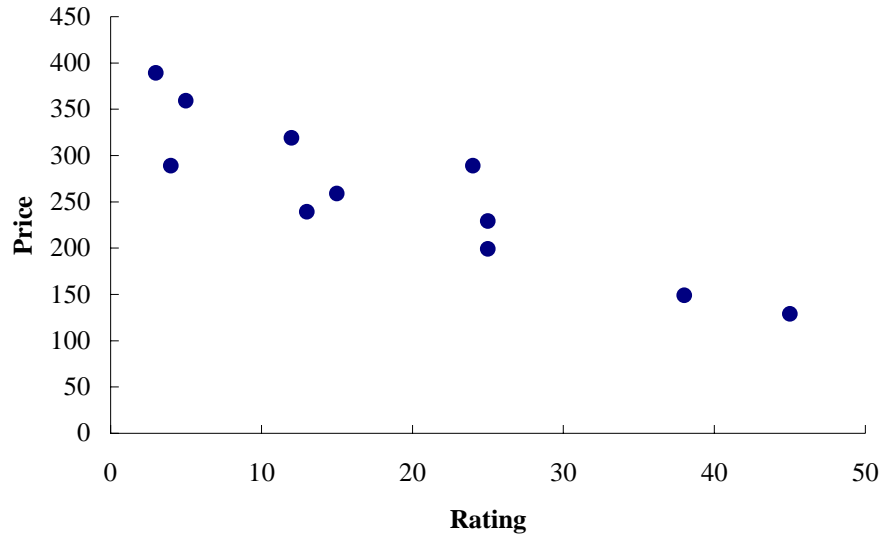
$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{568}{142} = 4$$

$$b_0 = \bar{y} - b_1\bar{x} = 108 - (4)(7) = 80$$

$$\hat{y} = 80 + 4x$$

c. $\hat{y} = 80 + 4x = 80 + 4(9) = 116$

10. a.



- b. The scatter diagram and the slope of the estimated regression equation indicate a negative linear relationship between rating and price. Thus, it appears that sleeping bags with a lower temperature rating cost more than sleeping bags with a higher temperature rating. In other words, it costs more to stay warmer.

c. $\bar{x} = \Sigma x_i / n = 209 / 11 = 19$ $\bar{y} = \Sigma y_i / n = 2849 / 11 = 259$

$$\Sigma(x_i - \bar{x})(y_i - \bar{y}) = -10,090 \quad \Sigma(x_i - \bar{x})^2 = 1912$$

$$b_1 = \frac{\Sigma(x_i - \bar{x})(y_i - \bar{y})}{\Sigma(x_i - \bar{x})^2} = \frac{-10,090}{1912} = -5.2772$$

$$b_0 = \bar{y} - b_1\bar{x} = 259 - (-5.2772)(19) = 359.2668$$

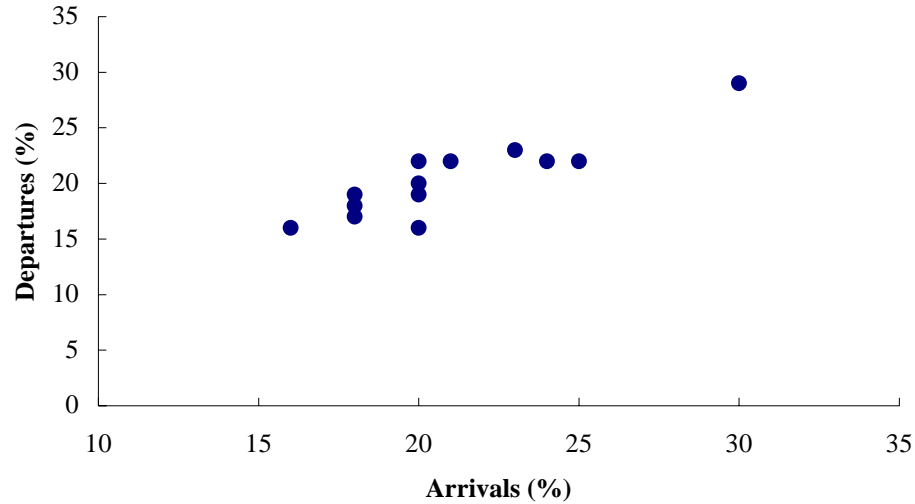
$$\hat{y} = 359.2668 - 5.2772x$$

d. $\hat{y} = 359.2668 - 5.2772x = 359.2668 - 5.2772(20) = 253.72$

Thus, the estimate of the price of sleeping bag with a temperature rating of 20 is approximately \$254.

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11. a.



- b. There appears to be a positive linear relationship between the variables.
 c. Let x = percentage of late arrivals and y = percentage of late departures.

$$\bar{x} = \frac{\sum x_i}{n} = \frac{273}{13} = 21 \quad \bar{y} = \frac{\sum y_i}{n} = \frac{265}{13} = 20.3846$$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 142 \quad \sum (x_i - \bar{x})^2 = 166$$

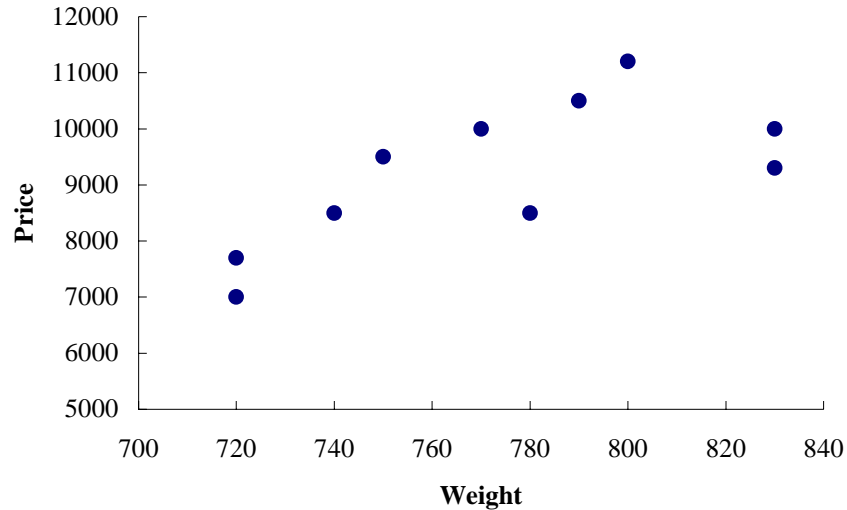
$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{142}{166} = .8554$$

$$b_0 = \bar{y} - b_1 \bar{x} = 20.3846 - (.8554)(21) = 2.4212$$

$$\hat{y} = 2.42 + .86x$$

- d. A one percent increase in the percentage of late arrivals will increase the percentage of late arrivals by .86 or slightly less than one percent.
 e. $\hat{y} = 2.42 + .86x = 2.42 + .86(22) = 21.34\%$

12. a.



b. The scatter diagram indicates a positive linear relationship between weight and price. Thus, it appears that PWC's that weigh more have a higher price.

c. $\bar{x} = \Sigma x_i / n = 7730 / 10 = 773$ $\bar{y} = \Sigma y_i / n = 92,200 / 10 = 9220$

$$\Sigma(x_i - \bar{x})(y_i - \bar{y}) = 332,400 \quad \Sigma(x_i - \bar{x})^2 = 14,810$$

$$b_1 = \frac{\Sigma(x_i - \bar{x})(y_i - \bar{y})}{\Sigma(x_i - \bar{x})^2} = \frac{332,400}{14,810} = 22.4443$$

$$b_0 = \bar{y} - b_1\bar{x} = 9220 - (22.4443)(773) = -8129.4439$$

$$\hat{y} = -8129.4439 + 22.4443x$$

d. $\hat{y} = -8129.4439 + 22.4443x = -8129.4439 + 22.4443(750) = 8703.78$

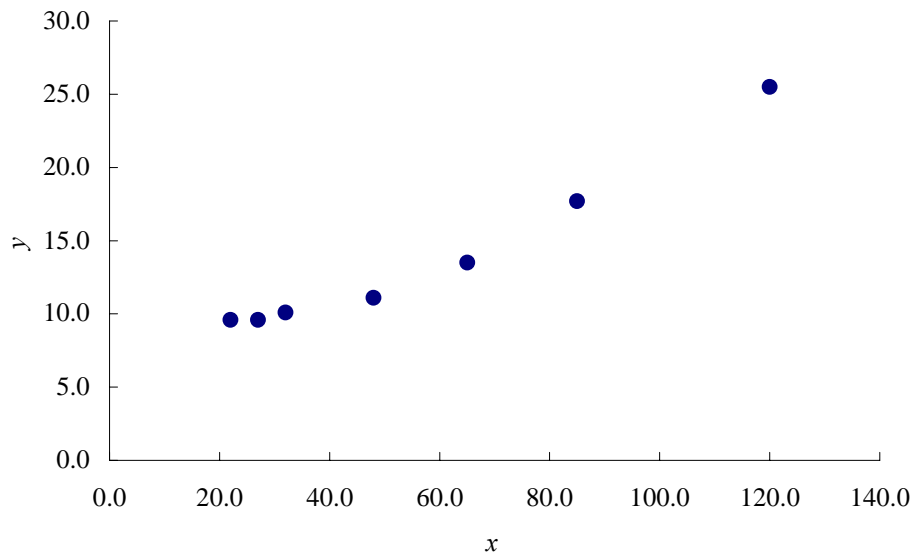
Thus, the estimate of the price of Jet Ski with a weight of 750 pounds is approximately \$8704.

e. No. The relationship between weight and price is not deterministic.

f. The weight of the Kawasaki SX-R 800 is so far below the lowest weight for the data used to develop the estimated regression equation that we would not recommend using the estimated regression equation to predict the price for this model.

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13. a.



b. $\bar{x} = \frac{\sum x_i}{n} = \frac{399}{7} = 57$ $\bar{y} = \frac{\sum y_i}{n} = \frac{97.1}{7} = 13.8714$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 1233.7 \quad \sum (x_i - \bar{x})^2 = 7648$$

$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{1233.7}{7648} = 0.1613$$

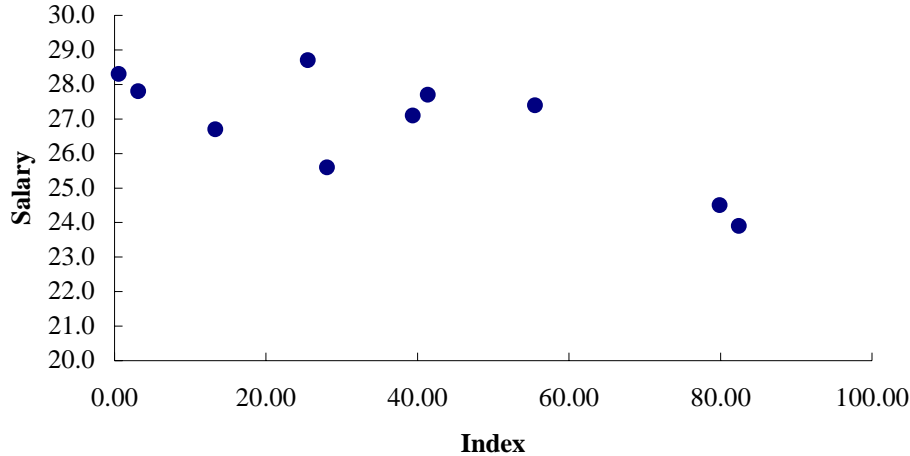
$$b_0 = \bar{y} - b_1 \bar{x} = 13.8714 - (0.1613)(57) = 4.6773$$

$$\hat{y} = 4.68 + 0.16x$$

c. $\hat{y} = 4.68 + 0.16x = 4.68 + 0.16(52.5) = 13.08$ or approximately \$13,080.

The agent's request for an audit appears to be justified.

14. a.



b. Let x = cost of living index and y = starting salary (\$1000s)

$$\bar{x} = \frac{\sum x_i}{n} = \frac{369.16}{10} = 36.916 \quad \bar{y} = \frac{\sum y_i}{n} = \frac{267.7}{10} = 26.77$$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = -311.9592 \quad \sum (x_i - \bar{x})^2 = 7520.4042$$

$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{-311.9592}{7520.4042} = -.0415$$

$$b_0 = \bar{y} - b_1\bar{x} = 26.77 - (-.0415)(36.916) = 28.30$$

$$\hat{y} = 28.30 - .0415x$$

c. $\hat{y} = 28.30 - .0415x = 28.30 - .0415(50) = 26.2$

15. a. The estimated regression equation and the mean for the dependent variable are:

$$\hat{y}_i = 0.2 + 2.6x_i \quad \bar{y} = 8$$

The sum of squares due to error and the total sum of squares are

$$SSE = \sum (y_i - \hat{y}_i)^2 = 12.40 \quad SST = \sum (y_i - \bar{y})^2 = 80$$

$$\text{Thus, } SSR = SST - SSE = 80 - 12.4 = 67.6$$

b. $r^2 = SSR/SST = 67.6/80 = .845$

The least squares line provided a very good fit; 84.5% of the variability in y has been explained by the least squares line.

c. $r_{xy} = \sqrt{.845} = +.9192$

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16. a. The estimated regression equation and the mean for the dependent variable are:

$$\hat{y}_i = 68 - 3x \quad \bar{y} = 35$$

The sum of squares due to error and the total sum of squares are

$$SSE = \sum(y_i - \hat{y}_i)^2 = 230 \quad SST = \sum(y_i - \bar{y})^2 = 1850$$

$$\text{Thus, } SSR = SST - SSE = 1850 - 230 = 1620$$

b. $r^2 = SSR/SST = 1620/1850 = .876$

The least squares line provided an excellent fit; 87.6% of the variability in y has been explained by the estimated regression equation.

c. $r_{xy} = \sqrt{.876} = -.936$

Note: the sign for r is negative because the slope of the estimated regression equation is negative. ($b_1 = -3$)

17. The estimated regression equation and the mean for the dependent variable are:

$$\hat{y}_i = 7.6 + .9x \quad \bar{y} = 16.6$$

The sum of squares due to error and the total sum of squares are

$$SSE = \sum(y_i - \hat{y}_i)^2 = 127.3 \quad SST = \sum(y_i - \bar{y})^2 = 281.2$$

$$\text{Thus, } SSR = SST - SSE = 281.2 - 127.3 = 153.9$$

$$r^2 = SSR/SST = 153.9/281.2 = .547$$

We see that 54.7% of the variability in y has been explained by the least squares line.

$$r_{xy} = \sqrt{.547} = +.740$$

18. a. The estimated regression equation and the mean for the dependent variable are:

$$\hat{y} = 1790.5 + 581.1x \quad \bar{y} = 3650$$

The sum of squares due to error and the total sum of squares are

$$SSE = \sum(y_i - \hat{y}_i)^2 = 85,135.14 \quad SST = \sum(y_i - \bar{y})^2 = 335,000$$

$$\text{Thus, } SSR = SST - SSE = 335,000 - 85,135.14 = 249,864.86$$

b. $r^2 = SSR/SST = 249,864.86/335,000 = .746$

We see that 74.6% of the variability in y has been explained by the least squares line.

c. $r_{xy} = \sqrt{.746} = +.8637$

19. The estimated regression equation and the mean for the dependent variable are:

$$\hat{y}_i = 40,639 - 1301.2x \quad \bar{y} = 36,562.27$$

The sum of squares due to error and the total sum of squares are

$$SSE = \sum (y_i - \hat{y}_i)^2 = 47,116,828 \quad SST = \sum (y_i - \bar{y})^2 = 94,072,519$$

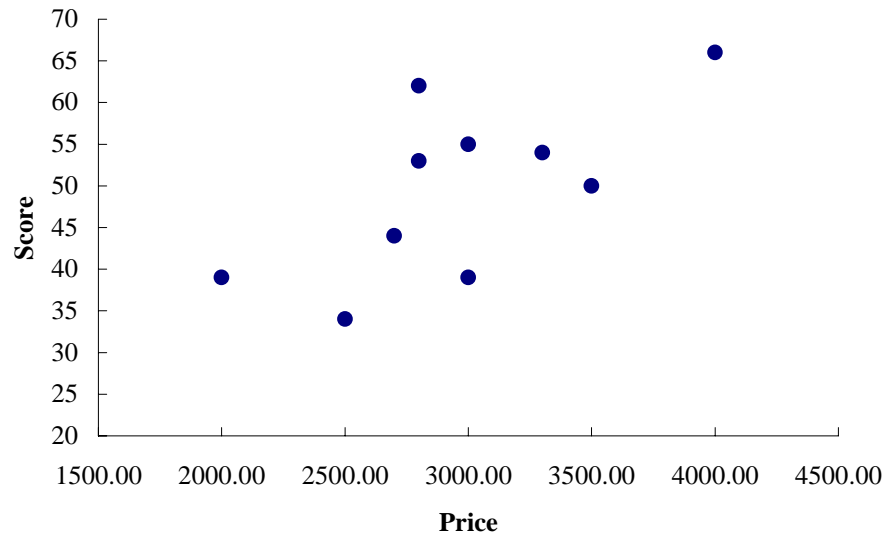
$$\text{Thus, } SSR = SST - SSE = 94,072,519 - 47,116,828 = 46,955,691$$

$$r^2 = SSR/SST = 46,955,691/94,072,519 = .4991$$

We see that 49.91% of the variability in y has been explained by the least squares line.

$$r_{xy} = \sqrt{.4991} = -.71$$

20. a.



The scatter diagram indicates a positive linear relationship between price and score.

$$\bar{x} = \sum x_i / n = 29,600 / 10 = 2960 \quad \bar{y} = \sum y_i / n = 496 / 10 = 49.6$$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 34,840 \quad \sum (x_i - \bar{x})^2 = 2,744,000$$

$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{34,840}{2,744,000} = .012697$$

$$b_0 = \bar{y} - b_1 \bar{x} = 49.6 - (.012697)(2960) = 12.0169$$

$$\hat{y} = 12.0169 + .0127x$$

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- b. The sum of squares due to error and the total sum of squares are

$$SSE = \sum (y_i - \hat{y}_i)^2 = 540.0446 \quad SST = \sum (y_i - \bar{y})^2 = 982.4$$

$$\text{Thus, } SSR = SST - SSE = 982.4 - 540.0446 = 442.3554$$

$$r^2 = SSR/SST = 442.3554/982.4 = .4503$$

The fit provided by the estimated regression equation is not that good; only 45.03% of the variability in y has been explained by the least squares line.

- c. $\hat{y} = 12.0169 + .0127x = 12.0169 + .0127(3200) = 52.66$

The estimate of the overall score for a 42-inch plasma television is approximately 53.

$$21. \text{ a. } \bar{x} = \frac{\sum x_i}{n} = \frac{3450}{6} = 575 \quad \bar{y} = \frac{\sum y_i}{n} = \frac{33,700}{6} = 5616.67$$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 712,500 \quad \sum (x_i - \bar{x})^2 = 93,750$$

$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{712,500}{93,750} = 7.6$$

$$b_0 = \bar{y} - b_1\bar{x} = 5616.67 - (7.6)(575) = 1246.67$$

$$\hat{y} = 1246.67 + 7.6x$$

- b. \$7.60

- c. The sum of squares due to error and the total sum of squares are:

$$SSE = \sum (y_i - \hat{y}_i)^2 = 233,333.33 \quad SST = \sum (y_i - \bar{y})^2 = 5,648,333.33$$

$$\text{Thus, } SSR = SST - SSE = 5,648,333.33 - 233,333.33 = 5,415,000$$

$$r^2 = SSR/SST = 5,415,000/5,648,333.33 = .9587$$

We see that 95.87% of the variability in y has been explained by the estimated regression equation.

- d. $\hat{y} = 1246.67 + 7.6x = 1246.67 + 7.6(500) = \5046.67

22. a. Let x = speed (ppm) and y = price (\$)

$$\bar{x} = \frac{\sum x_i}{n} = \frac{149.9}{10} = 14.99 \quad \bar{y} = \frac{\sum y_i}{n} = \frac{10,221}{10} = 1022.1$$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 34,359.810 \quad \sum (x_i - \bar{x})^2 = 291.3890$$

$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{34,359.810}{291.3890} = 117.917320$$

$$b_0 = \bar{y} - b_1\bar{x} = 1022.1 - (117.917320)(14.99) = -745.480627$$

$$\hat{y} = -745.480627 + 117.917320x$$

- b. The sum of squares due to error and the total sum of squares are:

$$SSE = \sum(y_i - \hat{y}_i)^2 = 1,678,294 \quad SST = \sum(y_i - \bar{y})^2 = 5,729,911$$

$$\text{Thus, } SSR = SST - SSE = 5,729,911 - 1,678,294 = 4,051,617$$

$$r^2 = SSR/SST = 4,051,617/5,729,911 = 0.7071$$

Approximately 71% of the variability in price is explained by the speed.

c. $r_{xy} = \sqrt{.7071} = +.84$

It reflects a linear relationship that is between weak and strong.

23. a. $s^2 = MSE = SSE / (n - 2) = 12.4 / 3 = 4.133$

b. $s = \sqrt{MSE} = \sqrt{4.133} = 2.033$

c. $\sum(x_i - \bar{x})^2 = 10$

$$s_{b_1} = \frac{s}{\sqrt{\sum(x_i - \bar{x})^2}} = \frac{2.033}{\sqrt{10}} = 0.643$$

d. $t = \frac{b_1}{s_{b_1}} = \frac{2.6}{.643} = 4.044$

Using t table (3 degrees of freedom), area in tail is between .01 and .025

p -value is between .02 and .05

Using Excel or Minitab, the p -value corresponding to $t = 4.04$ is .0272.

Because $p\text{-value} \leq \alpha$, we reject $H_0: \beta_1 = 0$

e. $MSR = SSR / 1 = 67.6$

$$F = MSR / MSE = 67.6 / 4.133 = 16.36$$

Using F table (1 degree of freedom numerator and 3 denominator), p -value is between .025 and .05

Using Excel or Minitab, the p -value corresponding to $F = 16.36$ is .0272.

Because $p\text{-value} \leq \alpha$, we reject $H_0: \beta_1 = 0$

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Source of Variation	Sum of Squares	Degrees of Freedom	Mean Square	<i>F</i>	<i>p</i> -value
Regression	67.6	1	67.6	16.36	.0272
Error	12.4	3	4.133		
Total	80.0	4			

24. a. $s^2 = \text{MSE} = \text{SSE}/(n - 2) = 230/3 = 76.6667$

b. $s = \sqrt{\text{MSE}} = \sqrt{76.6667} = 8.7560$

c. $\Sigma(x_i - \bar{x})^2 = 180$

$$s_{b_1} = \frac{s}{\sqrt{\Sigma(x_i - \bar{x})^2}} = \frac{8.7560}{\sqrt{180}} = 0.6526$$

d. $t = \frac{b_1}{s_{b_1}} = \frac{-3}{.653} = -4.59$

Using *t* table (3 degrees of freedom), area in tail is between .005 and .01; *p*-value is between .01 and .02

Using Excel or Minitab, the *p*-value corresponding to *t* = -4.59 is .0193.

Because *p*-value $\leq \alpha$, we reject H_0 : $\beta_1 = 0$

e. $\text{MSR} = \text{SSR}/1 = 1620$

$$F = \text{MSR}/\text{MSE} = 1620/76.6667 = 21.13$$

Using *F* table (1 degree of freedom numerator and 3 denominator), *p*-value is between .01 and .025

Using Excel or Minitab, the *p*-value corresponding to *F* = 21.13 is .0193.

Because *p*-value $\leq \alpha$, we reject H_0 : $\beta_1 = 0$

Source of Variation	Sum of Squares	Degrees of Freedom	Mean Square	<i>F</i>	<i>p</i> -value
Regression	230	1	230	21.13	.0193
Error	1620	3	76.6667		
Total	1850	4			

25. a. $s^2 = \text{MSE} = \text{SSE}/(n - 2) = 127.3/3 = 42.4333$

$$s = \sqrt{\text{MSE}} = \sqrt{42.4333} = 6.5141$$

b. $\Sigma(x_i - \bar{x})^2 = 190$

$$s_{b_1} = \frac{s}{\sqrt{\Sigma(x_i - \bar{x})^2}} = \frac{6.5141}{\sqrt{190}} = 0.4726$$

$$t = \frac{b_1}{s_{b_1}} = \frac{.9}{.4726} = 1.90$$

Using t table (3 degrees of freedom), area in tail is between .05 and .10

p -value is between .10 and .20

Using Excel or Minitab, the p -value corresponding to $t = 1.90$ is .1530.

Because $p\text{-value} > \alpha$, we cannot reject $H_0: \beta_1 = 0$; x and y do not appear to be related.

c. $MSR = SSR/1 = 153.9/1 = 153.9$

$$F = MSR/MSE = 153.9/42.4333 = 3.63$$

Using F table (1 degree of freedom numerator and 3 denominator), p -value is greater than .10

Using Excel or Minitab, the p -value corresponding to $F = 3.63$ is .1530.

Because $p\text{-value} > \alpha$, we cannot reject $H_0: \beta_1 = 0$; x and y do not appear to be related.

26. a. In solving exercise 18, we found $SSE = 85,135.14$

$$s^2 = MSE = SSE/(n - 2) = 85,135.14/4 = 21,283.79$$

$$s = \sqrt{MSE} = \sqrt{21,283.79} = 145.89$$

$$\Sigma(x_i - \bar{x})^2 = 0.74$$

$$s_{b_1} = \frac{s}{\sqrt{\Sigma(x_i - \bar{x})^2}} = \frac{145.89}{\sqrt{0.74}} = 169.59$$

$$t = \frac{b_1}{s_{b_1}} = \frac{581.1}{169.59} = 3.43$$

Using t table (4 degrees of freedom), area in tail is between .01 and .025

p -value is between .02 and .05

Using Excel or Minitab, the p -value corresponding to $t = 3.43$ is .0266.

Because $p\text{-value} \leq \alpha$, we reject $H_0: \beta_1 = 0$

b. $MSR = SSR/1 = 249,864.86/1 = 249,864.86$

$$F = MSR/MSE = 249,864.86/21,283.79 = 11.74$$

Using F table (1 degree of freedom numerator and 4 denominator), p -value is between .025 and .05

Using Excel or Minitab, the p -value corresponding to $F = 11.74$ is .0266.

Because $p\text{-value} \leq \alpha$, we reject $H_0: \beta_1 = 0$

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c.

Source of Variation	Sum of Squares	Degrees of Freedom	Mean Square	<i>F</i>	<i>p</i> -value
Regression	249864.86	1	249864.86	11.74	.0266
Error	85135.14	4	21283.79		
Total	335000	5			

$$27. \text{ a. } \bar{x} = \frac{\sum x_i}{n} = \frac{37}{10} = 3.7 \quad \bar{y} = \frac{\sum y_i}{n} = \frac{1654}{10} = 165.4$$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 315.2 \quad \sum (x_i - \bar{x})^2 = 10.1$$

$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{315.2}{10.1} = 31.2079$$

$$b_0 = \bar{y} - b_1 \bar{x} = 165.4 - (31.2079)(3.7) = 49.9308$$

$$\hat{y} = 49.9308 + 31.2079x$$

$$\text{b. } SSE = \sum (y_i - \hat{y}_i)^2 = 2487.66 \quad SST = \sum (y_i - \bar{y})^2 = 12,324.4$$

$$\text{Thus, } SSR = SST - SSE = 12,324.4 - 2487.66 = 9836.74$$

$$MSR = SSR/1 = 9836.74$$

$$MSE = SSE/(n - 2) = 2487.66/8 = 310.96$$

$$F = MSR / MSE = 9836.74/310.96 = 31.63$$

Using *F* table (1 degree of freedom numerator and 8 denominator), *p*-value is less than .01

Using Excel or Minitab, the *p*-value corresponding to *F* = 31.63 is .001.

Because *p*-value $\leq \alpha$, we reject $H_0: \beta_1 = 0$

Upper support and price are related.

$$\text{c. } r^2 = SSR/SST = 9,836.74/12,324.4 = .80$$

The estimated regression equation provided a good fit; we should feel comfortable using the estimated regression equation to estimate the price given the upper support rating.

$$\text{d. } \hat{y} = 49.93 + 31.21(4) = 174.77$$

28. The sum of squares due to error and the total sum of squares are

$$SSE = \sum (y_i - \hat{y}_i)^2 = 12,953.09 \quad SST = \sum (y_i - \bar{y})^2 = 66,200$$

$$\text{Thus, } SSR = SST - SSE = 66,200 - 12,953.09 = 53,246.91$$

$$s^2 = MSE = SSE / (n - 2) = 12,953.09 / 9 = 1439.2322$$

$$s = \sqrt{\text{MSE}} = \sqrt{1439.2322} = 37.9372$$

We can use either the t test or F test to determine whether temperature rating and price are related.

We will first illustrate the use of the t test.

Note: from the solution to exercise 10 $\sum(x_i - \bar{x})^2 = 1912$

$$s_{b_1} = \frac{s}{\sqrt{\sum(x_i - \bar{x})^2}} = \frac{37.9372}{\sqrt{1912}} = .8676$$

$$t = \frac{b_1}{s_{b_1}} = \frac{-5.2772}{.8676} = -6.0825$$

Using t table (9 degrees of freedom), area in tail is less than .005; p -value is less than .01

Using Excel or Minitab, the p -value corresponding to $t = -6.0825$ is .000.

Because $p\text{-value} \leq \alpha$, we reject H_0 : $\beta_1 = 0$

Because we can reject H_0 : $\beta_1 = 0$ we conclude that temperature rating and price are related.

Next we illustrate the use of the F test.

$$\text{MSR} = \text{SSR} / 1 = 53,246.91$$

$$F = \text{MSR} / \text{MSE} = 53,246.91 / 1439.2322 = 37.00$$

Using F table (1 degree of freedom numerator and 9 denominator), p -value is less than .01

Using Excel or Minitab, the p -value corresponding to $F = 37.00$ is .000.

Because $p\text{-value} \leq \alpha$, we reject H_0 : $\beta_1 = 0$

Because we can reject H_0 : $\beta_1 = 0$ we conclude that temperature rating and price are related.

The ANOVA table is shown below.

Source of Variation	Sum of Squares	Degrees of Freedom	Mean Square	F	p -value
Regression	53,246.91	1	53,246.91	37.00	.000
Error	12,953.09	9	1439.2322		
Total	66,200	10			

$$29. \quad \text{SSE} = \sum(y_i - \hat{y}_i)^2 = 233,333.33 \quad \text{SST} = \sum(y_i - \bar{y})^2 = 5,648,333.33$$

$$\text{Thus, SSR} = \text{SST} - \text{SSE} = 5,648,333.33 - 233,333.33 = 5,415,000$$

$$\text{MSE} = \text{SSE} / (n - 2) = 233,333.33 / (6 - 2) = 58,333.33$$

$$\text{MSR} = \text{SSR} / 1 = 5,415,000$$

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$$F = MSR / MSE = 5,415,000 / 58,333.25 = 92.83$$

Source of Variation	Sum of Squares	Degrees of Freedom	Mean Square	<i>F</i>	<i>p</i> -value
Regression	5,415,000.00	1	5,415,000	92.83	.0006
Error	233,333.33	4	58,333.33		
Total	5,648,333.33	5			

Using *F* table (1 degree of freedom numerator and 4 denominator), *p*-value is less than .01

Using Excel or Minitab, the *p*-value corresponding to *F* = 92.83 is .0006.

Because *p*-value ≤ α , we reject $H_0: \beta_1 = 0$. Production volume and total cost are related.

30. $SSE = \sum (y_i - \hat{y}_i)^2 = 1,678,294$ $SST = \sum (y_i - \bar{y})^2 = 5,729,911$

$$\text{Thus, } SSR = SST - SSE = 5,729,911 - 1,678,294 = 4,051,617$$

$$s^2 = MSE = SSE / (n - 2) = 1,678,294 / 8 = 209,786.8$$

$$s = \sqrt{209,786.8} = 458.02$$

$$\sum (x_i - \bar{x})^2 = 291.3890$$

$$s_{b_1} = \frac{s}{\sqrt{\sum (x_i - \bar{x})^2}} = \frac{458.02}{\sqrt{291.3890}} = 26.83$$

$$t = \frac{b_1}{s_{b_1}} = \frac{117.9173}{26.83} = 4.39$$

Using *t* table (1 degree of freedom numerator and 8 denominator), area in tail is less than .005

p-value is less than .01

Using Excel or Minitab, the *p*-value corresponding to *t* = 4.39 is .002.

Because *p*-value ≤ α , we reject $H_0: \beta_1 = 0$

There is a significant relationship between *x* and *y*.

31. $SSE = 540.04$ and $SST = 982.40$

$$\text{Thus, } SSR = SST - SSE = 982.40 - 540.04 = 442.36$$

$$s^2 = MSE = SSE / (n - 2) = 540.04 / 8 = 67.5050$$

$$s = \sqrt{MSE} = \sqrt{67.5050} = 8.216$$

$$MSR = SSR / 1 = 442.36$$

$$F = MSR / MSE = 442.36 / 67.5050 = 6.55$$

Using F table (1 degree of freedom numerator and 8 denominator), p -value is between .025 and .05

Using Excel or Minitab, the p -value corresponding to $F = 6.55$ is .034.

Because $p\text{-value} \leq \alpha$, we reject $H_0: \beta_1 = 0$

Conclusion: price and overall score are related

32. a. $s = 2.033$

$$\bar{x} = 3 \quad \Sigma(x_i - \bar{x})^2 = 10$$

$$s_{\hat{y}_p} = s \sqrt{\frac{1}{n} + \frac{(x_p - \bar{x})^2}{\Sigma(x_i - \bar{x})^2}} = 2.033 \sqrt{\frac{1}{5} + \frac{(4-3)^2}{10}} = 1.11$$

b. $\hat{y} = 0.2 + 2.6x = 0.2 + 2.6(4) = 10.6$

$$\hat{y}_p \pm t_{\alpha/2} s_{\hat{y}_p}$$

$$10.6 \pm 3.182 (1.11) = 10.6 \pm 3.53$$

or 7.07 to 14.13

c. $s_{\text{ind}} = s \sqrt{1 + \frac{1}{n} + \frac{(x_p - \bar{x})^2}{\Sigma(x_i - \bar{x})^2}} = 2.033 \sqrt{1 + \frac{1}{5} + \frac{(4-3)^2}{10}} = 2.32$

d. $\hat{y}_p \pm t_{\alpha/2} s_{\text{ind}}$

$$10.6 \pm 3.182 (2.32) = 10.6 \pm 7.38$$

or 3.22 to 17.98

33. a. $s = 8.7560$

b. $\bar{x} = 11 \quad \Sigma(x_i - \bar{x})^2 = 180$

$$s_{\hat{y}_p} = s \sqrt{\frac{1}{n} + \frac{(x_p - \bar{x})^2}{\Sigma(x_i - \bar{x})^2}} = 8.7560 \sqrt{\frac{1}{5} + \frac{(8-11)^2}{180}} = 4.3780$$

$$\hat{y} = 68 - 3x = 68 - 3(8) = 44$$

$$\hat{y}_p \pm t_{\alpha/2} s_{\hat{y}_p}$$

$$44 \pm 3.182 (4.3780) = 44 \pm 13.93$$

or 30.07 to 57.93

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$$c. \quad s_{\text{ind}} = s \sqrt{1 + \frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum(x_i - \bar{x})^2}} = 8.7560 \sqrt{1 + \frac{1}{5} + \frac{(8-11)^2}{180}} = 9.7895$$

$$d. \quad \hat{y}_p \pm t_{\alpha/2} s_{\text{ind}}$$

$$44 \pm 3.182(9.7895) = 44 \pm 31.15$$

or 12.85 to 75.15

$$34. \quad s = 6.5141$$

$$\bar{x} = 10 \quad \sum(x_i - \bar{x})^2 = 190$$

$$s_{\hat{y}_p} = s \sqrt{\frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum(x_i - \bar{x})^2}} = 6.5141 \sqrt{\frac{1}{5} + \frac{(12-10)^2}{190}} = 3.0627$$

$$\hat{y} = 7.6 + .9x = 7.6 + .9(12) = 18.40$$

$$\hat{y}_p \pm t_{\alpha/2} s_{\hat{y}_p}$$

$$18.40 \pm 3.182(3.0627) = 18.40 \pm 9.75$$

or 8.65 to 28.15

$$s_{\text{ind}} = s \sqrt{1 + \frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum(x_i - \bar{x})^2}} = 6.5141 \sqrt{1 + \frac{1}{5} + \frac{(12-10)^2}{190}} = 7.1982$$

$$\hat{y}_p \pm t_{\alpha/2} s_{\text{ind}}$$

$$18.40 \pm 3.182(7.1982) = 18.40 \pm 22.90$$

or -4.50 to 41.30

35. a. Note: some of the values shown were computed in exercises 18 and 26.

$$s = 145.89$$

$$\bar{x} = 3.2 \quad \sum(x_i - \bar{x})^2 = 0.74$$

$$s_{\hat{y}_p} = s \sqrt{\frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum(x_i - \bar{x})^2}} = 145.89 \sqrt{\frac{1}{6} + \frac{(3-3.2)^2}{0.74}} = 68.54$$

$$\hat{y} = 1790.5 + 581.1x = 1790.5 + 581.1(3) = 3533.8$$

$$\hat{y}_p \pm t_{\alpha/2} s_{\hat{y}_p}$$

$$3533.8 \pm 2.776(68.54) = 3533.8 \pm 190.27$$

or \$3343.53 to \$3724.07

$$b. \quad s_{\text{ind}} = s \sqrt{1 + \frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum(x_i - \bar{x})^2}} = 145.89 \sqrt{1 + \frac{1}{6} + \frac{(3 - 3.2)^2}{0.74}} = 161.19$$

$$\hat{y}_p \pm t_{\alpha/2} s_{\text{ind}}$$

$$3533.8 \pm 2.776 (161.19) = 3533.8 \pm 447.46$$

$$\text{or } \$3086.34 \text{ to } \$3981.26$$

$$36. \quad a. \quad \hat{y} = 359.2668 - 5.2772x = 359.2668 - 5.2772(30) = 200.95 \text{ or approximately } \$201.$$

$$b. \quad s = 37.9372$$

$$\bar{x} = 19 \quad \sum(x_i - \bar{x})^2 = 1912$$

$$s_{\hat{y}_p} = s \sqrt{\frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum(x_i - \bar{x})^2}} = 37.9372 \sqrt{\frac{1}{11} + \frac{(30 - 19)^2}{1912}} = 14.90$$

$$\hat{y}_p \pm t_{\alpha/2} s_{\hat{y}_p}$$

$$200.95 \pm 2.262 (14.90) = 200.95 \pm 33.70$$

$$\text{or } 167.25 \text{ to } 234.65$$

$$c. \quad s_{\text{ind}} = s \sqrt{1 + \frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum(x_i - \bar{x})^2}} = 37.9372 \sqrt{1 + \frac{1}{11} + \frac{(30 - 19)^2}{1912}} = 40.76$$

$$\hat{y}_p \pm t_{\alpha/2} s_{\text{ind}}$$

$$200.95 \pm 2.262 (40.76) = 200.95 \pm 92.20$$

$$\text{or } 108.75 \text{ to } 293.15$$

- d. As expected, the prediction interval is much wider than the confidence interval. This is due to the fact that it is more difficult to predict the results for one new model with a temperature rating of 30 F° than it is to estimate the mean for all models with a temperature rating of 30 F°.

$$37. \quad a. \quad \bar{x} = 57 \quad \sum(x_i - \bar{x})^2 = 7648$$

$$s^2 = 1.88 \quad s = 1.37$$

$$s_{\hat{y}_p} = s \sqrt{\frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum(x_i - \bar{x})^2}} = 1.37 \sqrt{\frac{1}{7} + \frac{(52.5 - 57)^2}{7648}} = 0.52$$

$$\hat{y}_p \pm t_{\alpha/2} s_{\hat{y}_p}$$

$$\hat{y} = 4.68 + 0.16x = 4.68 + 0.16(52.5) = 13.08$$

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$$13.08 \pm 2.571 (.52) = 13.08 \pm 1.34$$

or 11.74 to 14.42 or \$11,740 to \$14,420

b. $s_{\text{ind}} = 1.47$

$$13.08 \pm 2.571 (1.47) = 13.08 \pm 3.78$$

or 9.30 to 16.86 or \$9,300 to \$16,860

c. Yes, \$20,400 is much larger than anticipated.

d. Any deductions exceeding the \$16,860 upper limit could suggest an audit.

38. a. $\hat{y} = 1246.67 + 7.6(500) = \5046.67

b. $\bar{x} = 575 \quad \Sigma(x_i - \bar{x})^2 = 93,750$

$$s^2 = \text{MSE} = 58,333.33 \quad s = 241.52$$

$$s_{\text{ind}} = s \sqrt{1 + \frac{1}{n} + \frac{(x_p - \bar{x})^2}{\Sigma(x_i - \bar{x})^2}} = 241.52 \sqrt{1 + \frac{1}{6} + \frac{(500 - 575)^2}{93,750}} = 267.50$$

$$\hat{y}_p \pm t_{\alpha/2} s_{\text{ind}}$$

$$5046.67 \pm 4.604 (267.50) = 5046.67 \pm 1231.57$$

or \$3815.10 to \$6278.24

c. Based on one month, \$6000 is not out of line since \$3815.10 to \$6278.24 is the prediction interval. However, a sequence of five to seven months with consistently high costs should cause concern.

39. a. Let x = miles of track and y = weekday ridership in thousands.

$$\bar{x} = \frac{\Sigma x_i}{n} = \frac{203}{7} = 29 \quad \bar{y} = \frac{\Sigma y_i}{n} = \frac{309}{7} = 44.1429$$

$$\Sigma(x_i - \bar{x})(y_i - \bar{y}) = 1471 \quad \Sigma(x_i - \bar{x})^2 = 838$$

$$b_1 = \frac{\Sigma(x_i - \bar{x})(y_i - \bar{y})}{\Sigma(x_i - \bar{x})^2} = \frac{1471}{838} = 1.7554$$

$$b_0 = \bar{y} - b_1 \bar{x} = 44.1429 - (1.7554)(29) = -6.76$$

$$\hat{y} = -6.76 + 1.755x$$

b. $\text{SST} = 3620.9 \quad \text{SSE} = 1038.7 \quad \text{SSR} = 2582.1$

$$r^2 = \text{SSR}/\text{SST} = 2582.1/3620.9 = .713$$

The estimated regression equation explained 71.3% of the variability in y ; a good fit.

c. $s^2 = \text{MSE} = 1038.7/5 = 207.7$

$$s = \sqrt{207.7} = 14.41$$

$$s_{\hat{y}_p} = s \sqrt{\frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum(x_i - \bar{x})^2}} = 14.41 \sqrt{\frac{1}{7} + \frac{(30 - 29)^2}{838}} = 5.47$$

$$\hat{y} = -6.76 + 1.755x = -6.76 + 1.755(30) = 45.9$$

$$\hat{y}_p \pm t_{\alpha/2} s_{\hat{y}_p}$$

$$45.9 \pm 2.571(5.47) = 45.9 \pm 14.1$$

or 31.8 to 60

d. $s_{\text{ind}} = s \sqrt{1 + \frac{1}{n} + \frac{(x_p - \bar{x})^2}{\sum(x_i - \bar{x})^2}} = 14.41 \sqrt{1 + \frac{1}{7} + \frac{(30 - 29)^2}{838}} = 15.41$

$$\hat{y}_p \pm t_{\alpha/2} s_{\text{ind}}$$

$$45.9 \pm 2.571(15.41) = 45.9 \pm 39.6$$

or 6.3 to 85.5

The prediction interval is so wide that it would not be of much value in the planning process. A larger data set would be beneficial.

40. a. 9

b. $\hat{y} = 20.0 + 7.21x$

c. 1.3626

d. $\text{SSE} = \text{SST} - \text{SSR} = 51,984.1 - 41,587.3 = 10,396.8$

$$\text{MSE} = 10,396.8/7 = 1,485.3$$

$$F = \text{MSR} / \text{MSE} = 41,587.3 / 1,485.3 = 28.00$$

Using F table (1 degree of freedom numerator and 7 denominator), p -value is less than .01

Using Excel or Minitab, the p -value corresponding to $F = 28.00$ is .0011.

Because $p\text{-value} \leq \alpha$, we reject H_0 : $B_1 = 0$.

e. $\hat{y} = 20.0 + 7.21(50) = 380.5$ or \$380,500

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41. a. $\hat{y} = 6.1092 + .8951x$

b. $t = \frac{b_1 - B_1}{s_{b_1}} = \frac{.8951 - 0}{.149} = 6.01$

Using the t table (8 degrees of freedom), area in tail is less than .005
 p -value is less than .01

Using Excel or Minitab, the p -value corresponding to $t = 6.01$ is .0003.

Because $p\text{-value} \leq \alpha$, we reject $H_0: B_1 = 0$

c. $\hat{y} = 6.1092 + .8951(25) = 28.49$ or \$28.49 per month

42 a. $\hat{y} = 80.0 + 50.0x$

b. 30

c. $F = \text{MSR} / \text{MSE} = 6828.6/82.1 = 83.17$

Using F table (1 degree of freedom numerator and 28 denominator), p -value is less than .01

Using Excel or Minitab, the p -value corresponding to $F = 83.17$ is .000.

Because $p\text{-value} < \alpha = .05$, we reject $H_0: B_1 = 0$.

Branch office sales are related to the salespersons.

d. $\hat{y} = 80 + 50(12) = 680$ or \$680,000

43. a. The Minitab output is shown below:

The regression equation is
Price = 4.98 + 2.94 Weight

Predictor	Coef	SE Coef	T	P
Constant	4.979	3.380	1.47	0.154
Weight	2.9370	0.2934	10.01	0.000

S = 8.457 R-Sq = 80.7% R-Sq(adj) = 79.9%

Analysis of Variance

Source	DF	SS	MS	F	P
Regression	1	7167.9	7167.9	100.22	0.000
Residual Error	24	1716.6	71.5		
Total	25	8884.5			

Predicted Values for New Observations

New Obs	Fit	SE Fit	95.0% CI	95.0% PI
1	34.35	1.66	(30.93, 37.77)	(16.56, 52.14)

b. The p -value = .000 < $\alpha = .05$ (t or F); significant relationship

c. $r^2 = .807$. The least squares line provided a very good fit.

- d. The 95% confidence interval is 30.93 to 37.77.
- e. The 95% prediction interval is 16.56 to 52.14.
44. a/b. The scatter diagram shows a linear relationship between the two variables.
- c. The Minitab output is shown below:

The regression equation is

Rental\$ = 37.1 - 0.779 Vacancy%

Predictor	Coef	SE Coef	T	P
Constant	37.066	3.530	10.50	0.000
Vacancy%	-0.7791	0.2226	-3.50	0.003

S = 4.889 R-Sq = 43.4% R-Sq(adj) = 39.8%

Analysis of Variance

Source	DF	SS	MS	F	P
Regression	1	292.89	292.89	12.26	0.003
Residual Error	16	382.37	23.90		
Total	17	675.26			

Predicted Values for New Observations

New Obs	Fit	SE Fit	95.0% CI	95.0% PI
1	17.59	2.51	(12.27, 22.90)	(5.94, 29.23)
2	28.26	1.42	(25.26, 31.26)	(17.47, 39.05)

Values of Predictors for New Observations

New Obs	Vacancy%
1	25.0
2	11.3

- d. Since the p -value = 0.003 is less than $\alpha = .05$, the relationship is significant.
- e. $r^2 = .434$. The least squares line does not provide a very good fit.
- f. The 95% confidence interval is 12.27 to 22.90 or \$12.27 to \$22.90.
- g. The 95% prediction interval is 17.47 to 39.05 or \$17.47 to \$39.05.

45. a. $\bar{x} = \frac{\sum x_i}{n} = \frac{70}{5} = 14$ $\bar{y} = \frac{\sum y_i}{n} = \frac{76}{5} = 15.2$

$$\sum (x_i - \bar{x})(y_i - \bar{y}) = 200 \quad \sum (x_i - \bar{x})^2 = 126$$

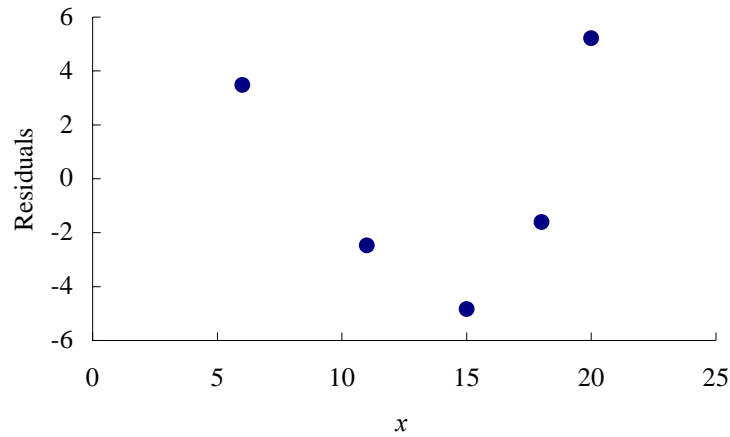
$$b_1 = \frac{\sum (x_i - \bar{x})(y_i - \bar{y})}{\sum (x_i - \bar{x})^2} = \frac{200}{126} = 1.5873$$

$$b_0 = \bar{y} - b_1 \bar{x} = 15.2 - (1.5873)(14) = -7.0222$$

$$\hat{y} = -7.02 + 1.59x$$

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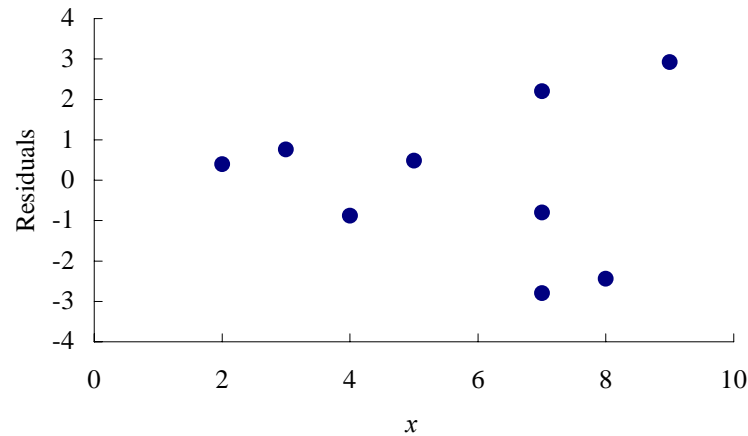
- b. The residuals are 3.48, -2.47, -4.83, -1.6, and 5.22
- c.



With only 5 observations it is difficult to determine if the assumptions are satisfied. However, the plot does suggest curvature in the residuals that would indicate that the error term assumptions are not satisfied. The scatter diagram for these data also indicates that the underlying relationship between x and y may be curvilinear.

46. a. $\hat{y} = 2.32 + .64x$

b.



The assumption that the variance is the same for all values of x is questionable. The variance appears to increase for larger values of x .

47. a. Let x = advertising expenditures and y = revenue

$$\hat{y} = 29.4 + 1.55x$$

b. $SST = 1002$ $SSE = 310.28$ $SSR = 691.72$

$$MSR = SSR / 1 = 691.72$$

$$MSE = SSE / (n - 2) = 310.28 / 5 = 62.0554$$

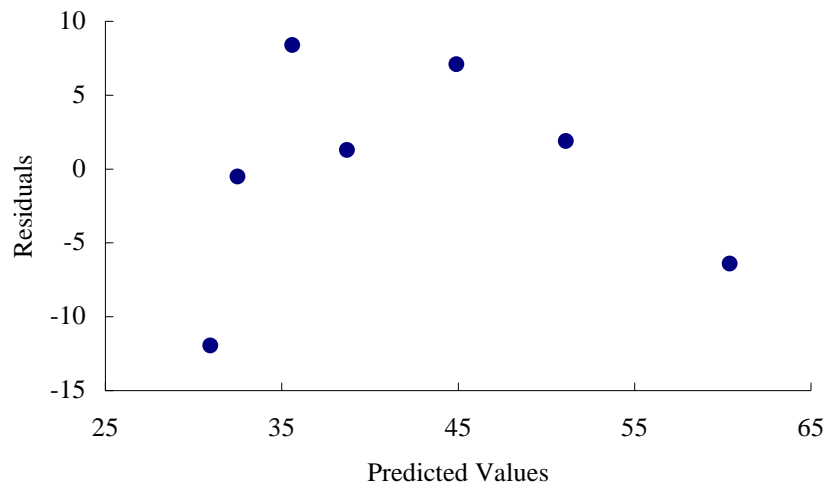
$$F = MSR / MSE = 691.72 / 62.0554 = 11.15$$

Using F table (1 degree of freedom numerator and 5 denominator), p -value is between .01 and .025

Using Excel or Minitab, the p -value corresponding to $F = 11.15$ is .0206.

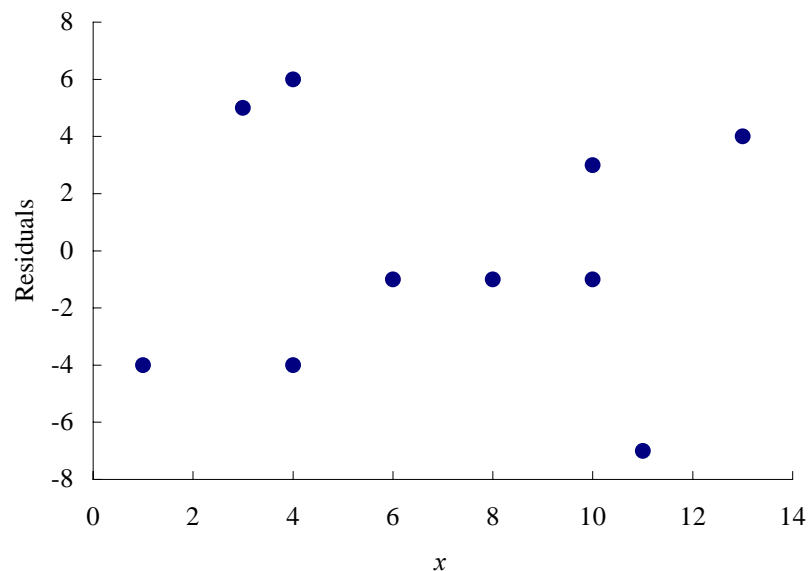
Because $p\text{-value} \leq \alpha = .05$, we conclude that the two variables are related.

c.



d. The residual plot leads us to question the assumption of a linear relationship between x and y . Even though the relationship is significant at the .05 level of significance, it would be extremely dangerous to extrapolate beyond the range of the data.

48. a. $\hat{y} = 80 + 4x$



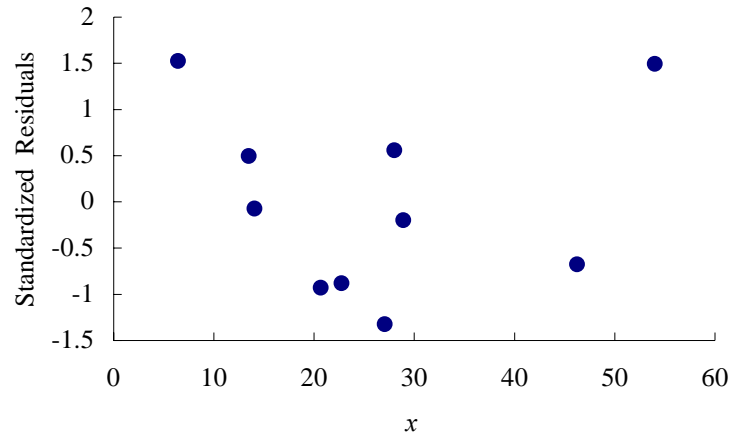
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- b. The assumptions concerning the error term appear reasonable.

49. a. Let x = return on investment (ROE) and y = price/earnings (P/E) ratio.

$$\hat{y} = -32.13 + 3.22x$$

- b.



- c. There is an unusual trend in the residuals. The assumptions concerning the error term appear questionable.

50. a. The Minitab output is shown below:

The regression equation is
 Price = 9.26 + 0.711 Shares

Predictor	Coef	SE Coef	T	P
Constant	9.265	1.099	8.43	0.000
Shares	0.7105	0.1474	4.82	0.001

S = 1.419 R-Sq = 74.4% R-Sq(adj) = 71.2%

Analysis of Variance

Source	DF	SS	MS	F	P
Regression	1	46.784	46.784	23.22	0.001
Residual Error	8	16.116	2.015		
Total	9	62.900			

- b. Since the p -value corresponding to $F = 23.22 = .001 < \alpha = .05$, the relationship is significant.

- c. $r^2 = .744$; a good fit. The least squares line explained 74.4% of the variability in Price.

- d. $\hat{y} = 9.26 + .711(6) = 13.53$

51. a. The Minitab output is shown below:

The regression equation is
Options = - 3.83 + 0.296 Common

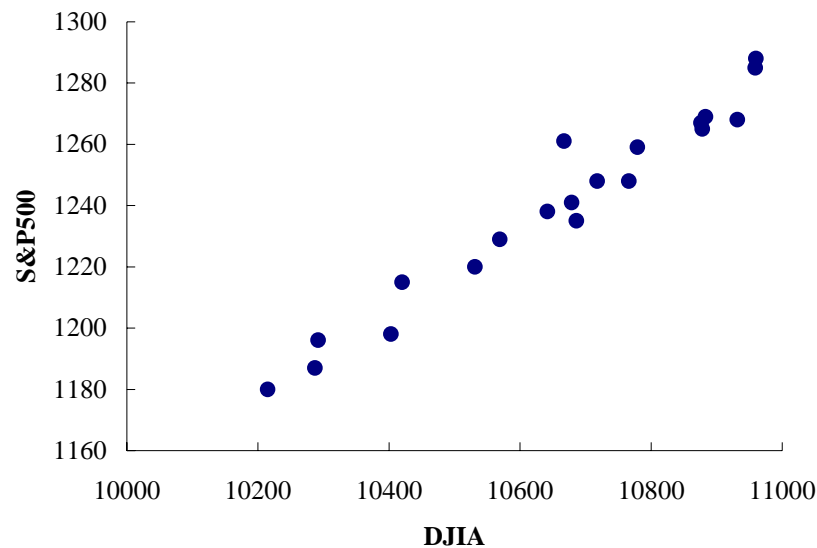
Predictor	Coef	SE Coef	T	P
Constant	-3.834	5.903	-0.65	0.529
Common	0.29567	0.02648	11.17	0.000

S = 11.04 R-Sq = 91.9% R-Sq(adj) = 91.2%
Analysis of Variance

Source	DF	SS	MS	F	P
Regression	1	15208	15208	124.72	0.000
Residual Error	11	1341	122		
Total	12	16550			

- b. $\hat{y} = -3.83 + 0.296(150) = 40.57$; approximately 40.6 million shares of options grants outstanding.
- c. $r^2 = .919$; a very good fit. The least squares line explained 91.9% of the variability in Options.

52. a.



- b. The Minitab output is shown below:

The regression equation is
S&P500 = - 182 + 0.133 DJIA

Predictor	Coef	SE Coef	T	P
Constant	-182.11	71.83	-2.54	0.021
DJIA	0.133428	0.006739	19.80	0.000

S = 6.89993 R-Sq = 95.6% R-Sq(adj) = 95.4%

Analysis of Variance

Source	DF	SS	MS	F	P
Regression	1	18666	18666	392.06	0.000
Residual Error	18	857	48		
Total	19	19523			

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- c. Using the F test, the p -value corresponding to $F = 392.06$ is .000. Because the p -value $\leq \alpha = .05$, we reject $H_0 : \beta_1 = 0$; there is a significant relationship.
- d. With $R\text{-Sq} = 95.6\%$, the estimated regression equation provided an excellent fit.
- e. $\hat{y} = -182.11 + .133428\text{DJIA} = -182.11 + .133428(11,000) = 1285.60$ or 1286.
- f. The DJIA is not that far beyond the range of the data. With the excellent fit provided by the estimated regression equation, we should not be too concerned about using the estimated regression equation to predict the S&P500.

53. The Minitab output is shown below:

The regression equation is
Expense = 10.5 + 0.953 Usage

Predictor	Coef	SE Coef	T	p
Constant	10.528	3.745	2.81	0.023
X	0.9534	0.1382	6.90	0.000

S = 4.250 R-sq = 85.6% R-sq(adj) = 83.8%

Analysis of Variance

SOURCE	DF	SS	MS	F	p
Regression	1	860.05	860.05	47.62	0.000
Residual Error	8	144.47	18.06		
Total	9	1004.53			

Fit Stdev.Fit 95% C.I. 95% P.I.
39.13 1.49 (35.69, 42.57) (28.74, 49.52)

- a. $\hat{y} = 10.5 + .953 \text{ Usage}$
- b. Since the p -value corresponding to $F = 47.62 = .000 < \alpha = .05$, we reject $H_0 : \beta_1 = 0$.
- c. The 95% prediction interval is 28.74 to 49.52 or \$2874 to \$4952
- d. Yes, since the expected expense is \$3913.

54. a. The Minitab output is shown below:

The regression equation is
Defects = 22.2 - 0.148 Speed

Predictor	Coef	SE Coef	T	P
Constant	22.174	1.653	13.42	0.000
Speed	-0.14783	0.04391	-3.37	0.028

S = 1.489 R-Sq = 73.9% R-Sq(adj) = 67.4%

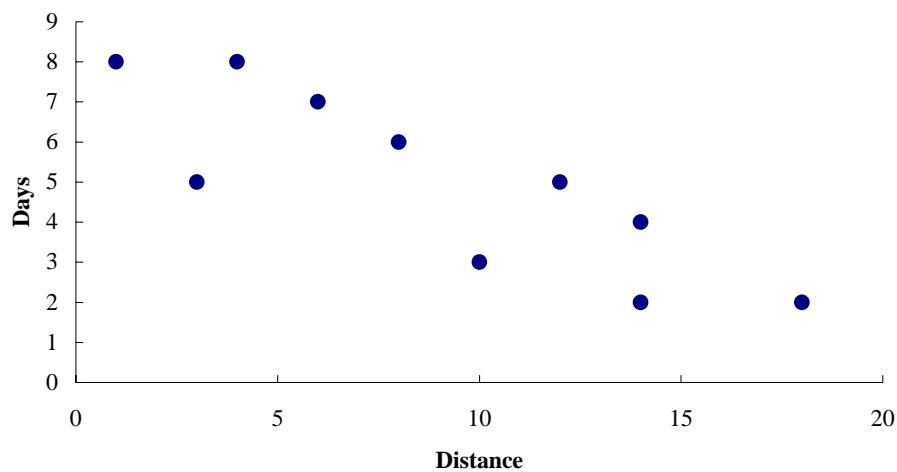
Analysis of Variance

Source	DF	SS	MS	F	P
Regression	1	25.130	25.130	11.33	0.028
Residual Error	4	8.870	2.217		
Total	5	34.000			

Predicted Values for New Observations

New Obs	Fit	SE Fit	95.0% CI	95.0% PI
1	14.783	0.896	(12.294, 17.271)	(9.957, 19.608)

- b. Since the p -value corresponding to $F = 11.33 = .028 < \alpha = .05$, the relationship is significant.
- c. $r^2 = .739$; a good fit. The least squares line explained 73.9% of the variability in the number of defects.
- d. Using the Minitab output in part (a), the 95% confidence interval is 12.294 to 17.271.
55. a.



There appears to be a negative linear relationship between distance to work and number of days absent.

- b. The MINITAB output is shown below:

The regression equation is
 Days = 8.10 - 0.344 Distance

Predictor	Coef	SE Coef	T	p
Constant	8.0978	0.8088	10.01	0.000
X	-0.34420	0.07761	-4.43	0.002

S = 1.289 R-sq = 71.1% R-sq(adj) = 67.5%

Analysis of Variance

SOURCE	DF	SS	MS	F	p
Regression	1	32.699	32.699	19.67	0.002
Residual Error	8	13.301	1.663		
Total	9	46.000			

Fit	Stdev.Fit	95% C.I.	95% P.I.
6.377	0.512	(5.195, 7.559)	(3.176, 9.577)

- c. Since the p -value corresponding to $F = 419.67$ is $.002 < \alpha = .05$. We reject $H_0: \beta_1 = 0$.
- d. $r^2 = .711$. The estimated regression equation explained 71.1% of the variability in y ; this is a reasonably good fit.

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- e. The 95% confidence interval is 5.195 to 7.559 or approximately 5.2 to 7.6 days.

56. a. The Minitab output is shown below:

The regression equation is
Cost = 220 + 132 Age

Predictor	Coef	SE Coef	T	p
Constant	220.00	58.48	3.76	0.006
X	131.67	17.80	7.40	0.000

S = 75.50 R-sq = 87.3% R-sq(adj) = 85.7%

Analysis of Variance

SOURCE	DF	SS	MS	F	p
Regression	1	312050	312050	54.75	0.000
Residual Error	8	45600	5700		
Total	9	357650			

Fit	Stdev.Fit	95% C.I.	95% P.I.
746.7	29.8	(678.0, 815.4)	(559.5, 933.9)

- b. Since the p -value corresponding to $F = 54.75$ is $.000 < \alpha = .05$, we reject $H_0: \beta_1 = 0$.
- c. $r^2 = .873$. The least squares line provided a very good fit.
- d. The 95% prediction interval is 559.5 to 933.9 or \$559.50 to \$933.90

57. a. The Minitab output is shown below:

The regression equation is
Points = 5.85 + 0.830 Hours

Predictor	Coef	SE Coef	T	p
Constant	5.847	7.972	0.73	0.484
X	0.8295	0.1095	7.58	0.000

S = 7.523 R-sq = 87.8% R-sq(adj) = 86.2%

Analysis of Variance

SOURCE	DF	SS	MS	F	p
Regression	1	3249.7	3249.7	57.42	0.000
Residual Error	8	452.8	56.6		
Total	9	3702.5			

Fit	Stdev.Fit	95% C.I.	95% P.I.
84.65	3.67	(76.19, 93.11)	(65.35, 103.96)

- b. Since the p -value corresponding to $F = 57.42$ is $.000 < \alpha = .05$, we reject $H_0: \beta_1 = 0$.
- c. 84.65 points
- d. The 95% prediction interval is 65.35 to 103.96

58. a. The Minitab output is shown below:

The regression equation is
Horizon = 0.275 + 0.950 S&P 500

Predictor	Coef	SE Coef	T	P
Constant	0.2747	0.9004	0.31	0.768
S&P 500	0.9498	0.3569	2.66	0.029

S = 2.664 R-Sq = 47.0% R-Sq(adj) = 40.3%

Analysis of Variance

Source	DF	SS	MS	F	P
Regression	1	50.255	50.255	7.08	0.029
Residual Error	8	56.781	7.098		
Total	9	107.036			

The market beta for Horizon is $b_1 = .95$

- b. Since the p -value = 0.029 is less than $\alpha = .05$, the relationship is significant.
- c. $r^2 = .470$. The least squares line does not provide a very good fit.
- d. Texas Instruments has higher risk with a market beta of 1.46.
59. a. The Minitab output is shown below:

The regression equation is
Audit% = - 0.471 + 0.000039 Income

Predictor	Coef	SE Coef	T	P
Constant	-0.4710	0.5842	-0.81	0.431
Income	0.00003868	0.00001731	2.23	0.038

S = 0.2088 R-Sq = 21.7% R-Sq(adj) = 17.4%

Analysis of Variance

Source	DF	SS	MS	F	P
Regression	1	0.21749	0.21749	4.99	0.038
Residual Error	18	0.78451	0.04358		
Total	19	1.00200			

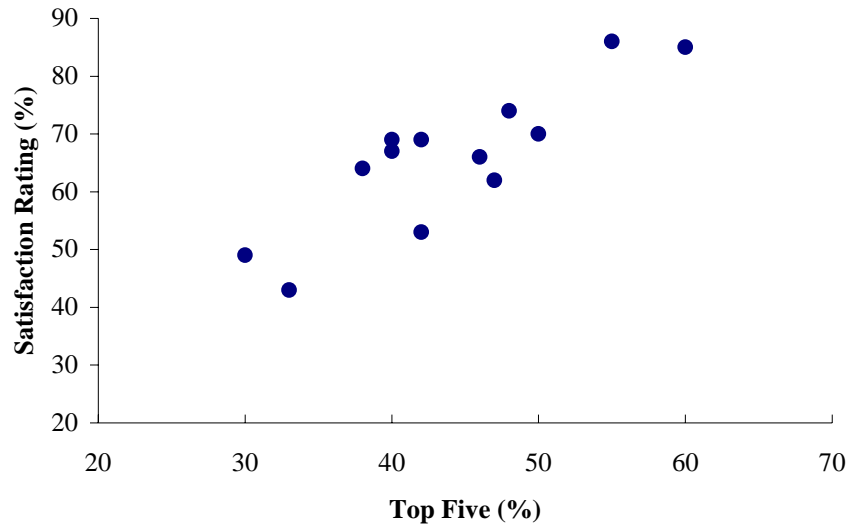
Predicted Values for New Observations

New Obs	Fit	SE Fit	95.0% CI	95.0% PI
1	0.8828	0.0523	(0.7729, 0.9927)	(0.4306, 1.3349)

- b. Since the p -value = 0.038 is less than $\alpha = .05$, the relationship is significant.
- c. $r^2 = .217$. The least squares line does not provide a very good fit.
- d. The 95% confidence interval is .7729 to .9927.

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60. a.



- b. There appears to be a positive linear relationship between the two variables.

A portion of the Minitab output for this problem follows.

The regression equation is

$$\text{Rating (\%)} = 9.4 + 1.29 \text{ Top Five (\%)}$$

Predictor	Coef	SE Coef	T	P
Constant	9.37	10.24	0.92	0.380
Top Five (%)	1.2875	0.2293	5.61	0.000

S = 6.62647 R-Sq = 74.1% R-Sq(adj) = 71.8%

Analysis of Variance

Source	DF	SS	MS	F	P
Regression	1	1383.9	1383.9	31.52	0.000
Residual Error	11	483.0	43.9		
Total	12	1866.9			

- c. $\hat{y} = 9.37 + 1.2875 \text{ Top Five (\%)}$
- d. Since the $p\text{-value} = .000 < \alpha = .05$, the relationship is significant.
- e. $r^2 = .741$; a good fit. The least squares line explained 74.1% of the variability in the satisfaction rating.
- f. $r_{xy} = \sqrt{r^2} = \sqrt{.741} = .86$