

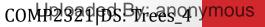


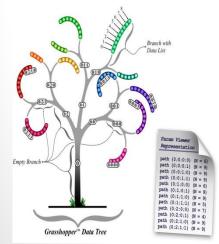
Faculty of Engineering and Technology Computer Science Department COMP2321

Data Structures

Chapter 4 Trees Splay Tree and B Tree







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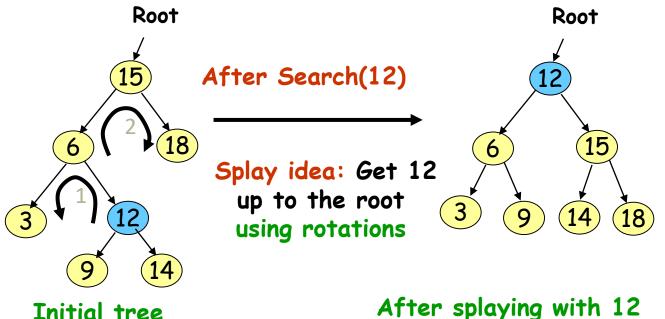
Splay Trees

- Splay Tree is binary search tree (BSTs) that:
 - Are not perfectly balanced all the time
 - It assumes that recently accessed nodes are most likely to visit them again.
 - Allow search and insertion operations to try to balance the tree so that future operations may run faster
- Based on the heuristic:
 - If X is accessed once, it is likely to be accessed again.
 - After node X is accessed, perform "splaying" operations to bring X up to the root of the tree.
 - Do this in a way that leaves the tree more or less balanced as a whole.

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Motivating Example





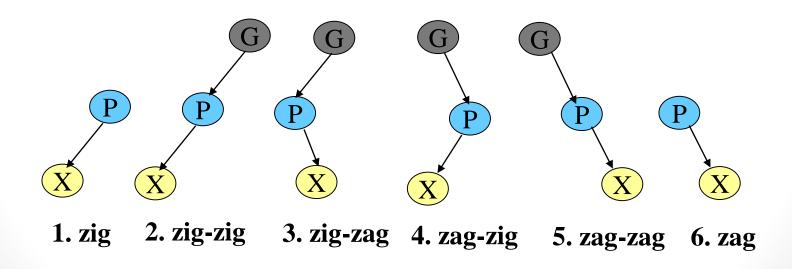
After splaying with 12

- Not only splaying with 12 makes the tree **balanced**, subsequent accesses for 12 will take O(1) time.
- Active (recently accessed) nodes will move towards the root and **inactive** nodes will slowly move further from the root

Splay Tree Terminology: operations



- Let X be a **non-root** node, i.e., has at least 1 ancestor.
- Let P be its parent node.
- Let G be its grandparent node (if it exists)
- Consider a path from G to X:
 - Each time we go left, we say that we "zig"
 - Each time we go **right**, we say that we "**zag**"
- There are 6 possible cases:



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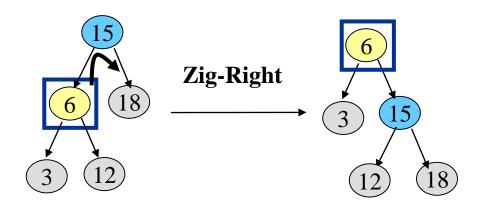


Splay Tree Operations

- When node X is accessed, apply one of six rotation operations:
 - Single Rotations (X has a P but no G)
 - zig, zag
 - Double Rotations (X has both a P and a G)
 - zig-zig, zig-zag
 - zag-zig, zag-zag

Splay Trees: Zig Operation

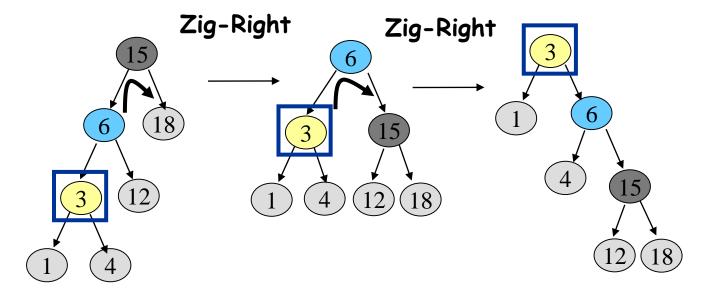
- "Zig" is just a single rotation, as in an AVL tree
- Suppose 6 was the node that was accessed (e.g. using Search)



- "Zig-Right" moves 6 to the root.
- Can access 6 faster next time: O(1)
- Notice that this is simply a right rotation in AVL tree terminology.

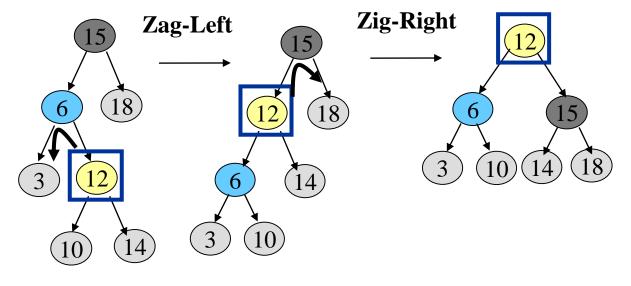
Splay Trees: Zig-Zig Operation

- "Zig-Zig" consists of two single rotations of the same type
- Suppose 3 was the node that was accessed (e.g., using Search)



- Due to "zig-zig" splaying, 3 has bubbled to the top!
- Note: Parent-Grandparent is rotated first.

Suppose 12 was the node that was accessed (e.g., using Search)



- Due to "zig-zag" splaying, 12 has bubbled to the top!
- Notice that this is simply an LR imbalance correction in AVL tree terminology (first a left rotation, then a right rotation)

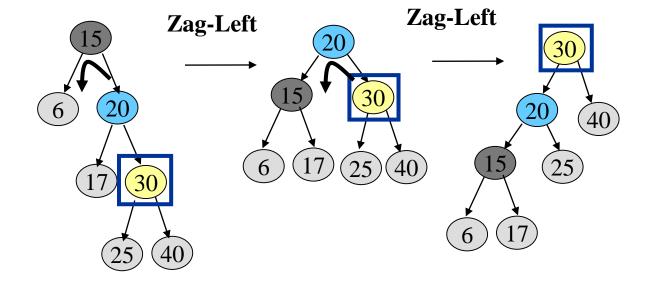
Splay Trees: Zag-Zig Operation "Zag-Zig" consists of two rotations of the opposite type Suppose 17 was the node that was accessed (e.g., using Search) Zag-Left **Zig-Right** 6 6 16 18

- Due to "zag-zig" splaying, 17 has bubbled to the top!
- Notice that this is simply an RL imbalance correction in AVL tree terminology (first a right rotation, then a left rotation)

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- "Zag-Zag" consists of two single rotations of the same type
- Suppose 30 was the node that was accessed (e.g., using Search)



- Due to "zag-zag" splaying, 30 has bubbled to the top!
- Note: Parent-Grandparent is rotated first.

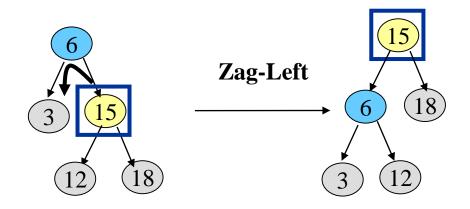
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Splay Trees: Zag Operation

- "Zag" is just a single rotation, as in an AVL tree
- Suppose 15 was the node that was accessed (e.g., using Search)

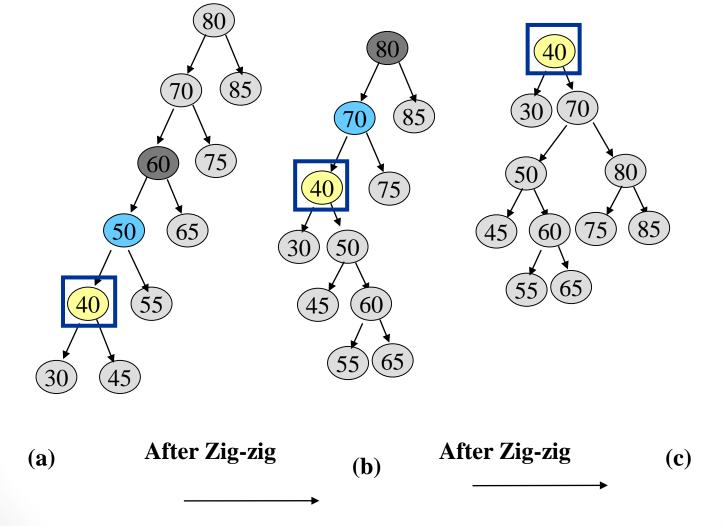


- "Zag-Left" moves 15 to the root.
- Can access 15 faster next time: O(1)
- Notice that this is simply a left rotation in AVL tree terminology

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Splay Trees: Example – 40 is accessed

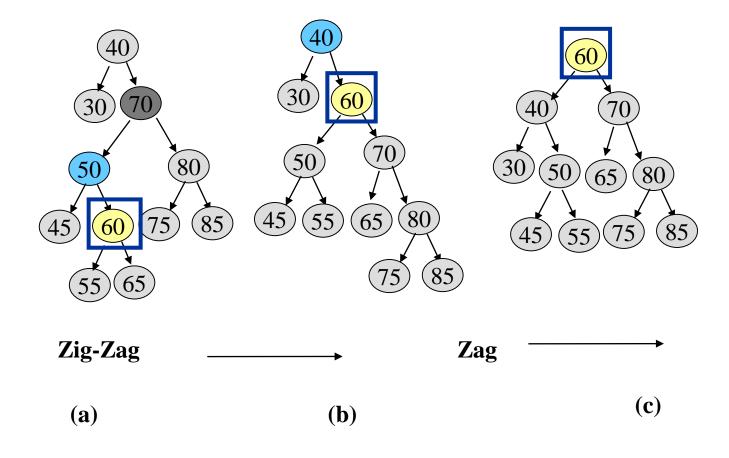


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Splay Trees: Example – 60 is accessed



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Splaying during other operations



- Splaying can be done not just after Search, but also after other operations such as Insert/Delete.
- Insert X: After inserting X at a leaf node (as in a regular BST), splay X up to the root
- Delete X: Do a Search on X and get X up to the root. Delete X at the root and move the largest item in its left sub-tree, i.e, its predecessor, to the root using splaying.
- <u>Note on Search X</u>: If X was not found, splay the leaf node that the Search ended up with to the root.

Any sequence of M operations on a splay tree of size N takes O(M log N) time.

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Exercise: Do it by yourself

- Insert the keys 4,9,3,7,5,6 in that order into an empty splay tree.
- A. Delete 9
- B. Find 3
- Insert the keys 1, 2, ..., 7 in that order into an empty splay tree.

What happens when you access "7"?

Hint: ensure your solution by using this website https://www.cs.usfca.edu/~galles/visualization/SplayTree.html

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B-Trees

DEF: A B-Tree of order m is an m-way tree such that

- 1. All leaf nodes are at the same level.
- 2. All non-leaf nodes (except the root) have at most m and at least m/2 children.
- The number of keys is one less than the number of children for non-leaf nodes and at most m-1 and at least m/2 for leaf nodes.
- 4. The root may have as few as 2 children unless the tree is the root alone.



Example for m = 5

DEF: A B-Tree of order 5 is an 5-way tree such that

- 1. All leaf nodes are at the same level.
- 2. All non-leaf nodes (except the root) have at most 5 and at least 2 children.
- The number of keys is one less than the number of children for non-leaf nodes and at most 4 and at least 2 for leaf nodes.
- 4. The root may have as few as 2 children unless the tree is the root alone.



Creating a B-tree of order 5

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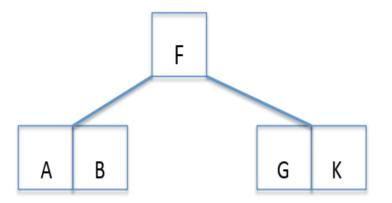
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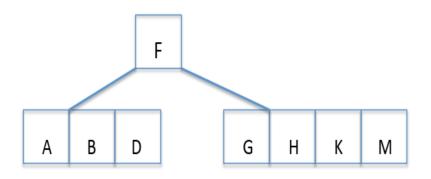


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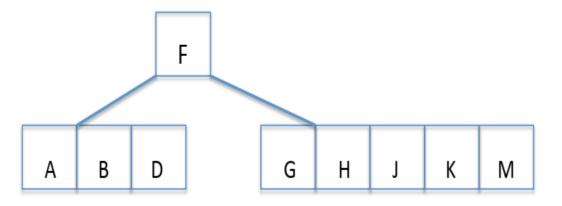
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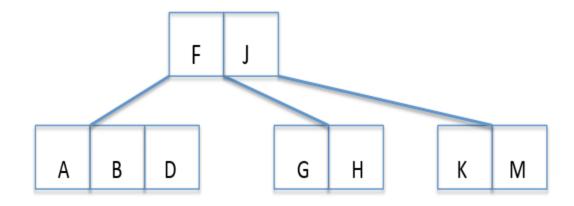


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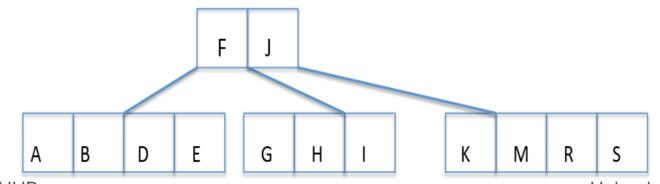
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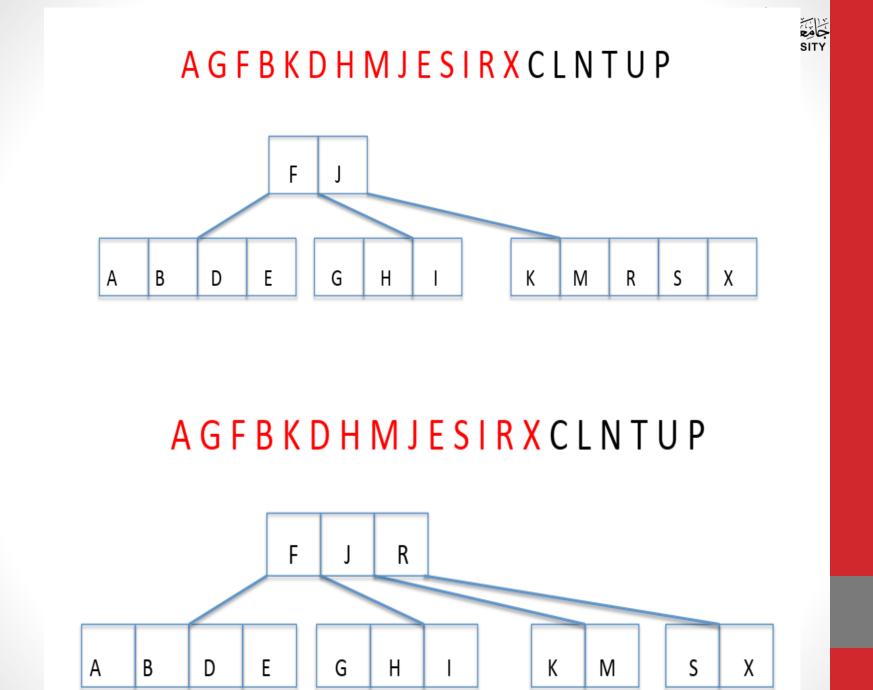


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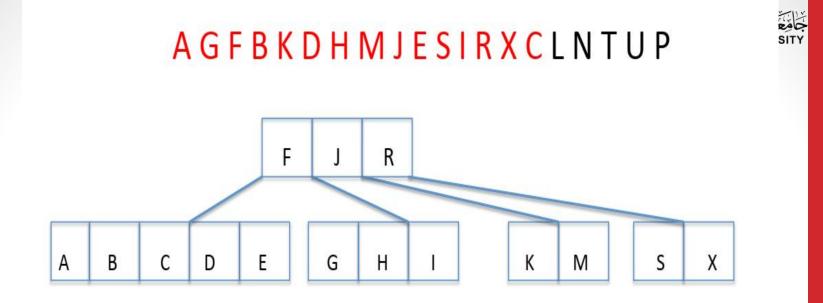
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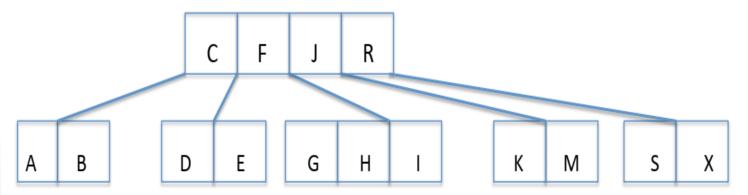


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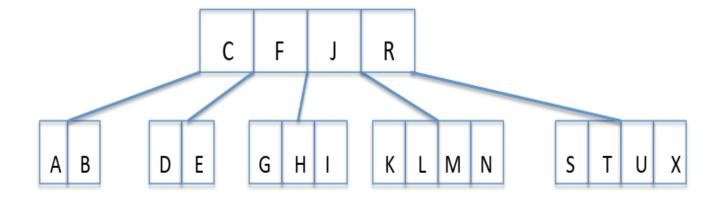
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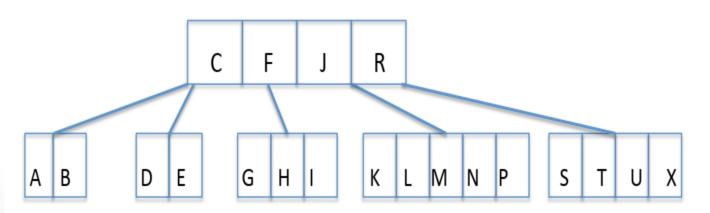
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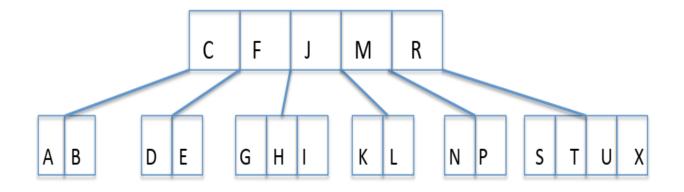
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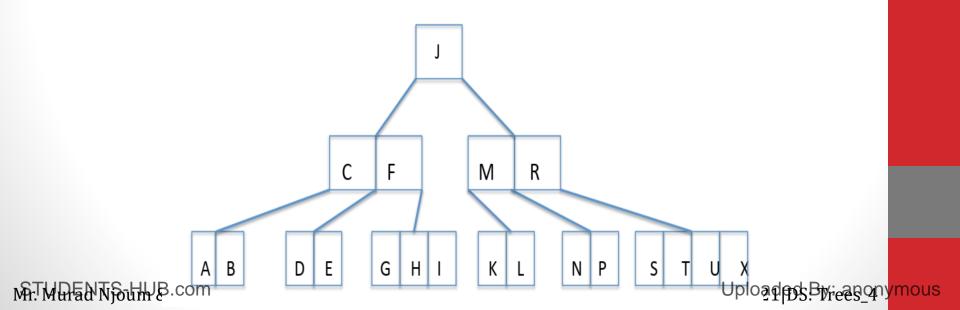
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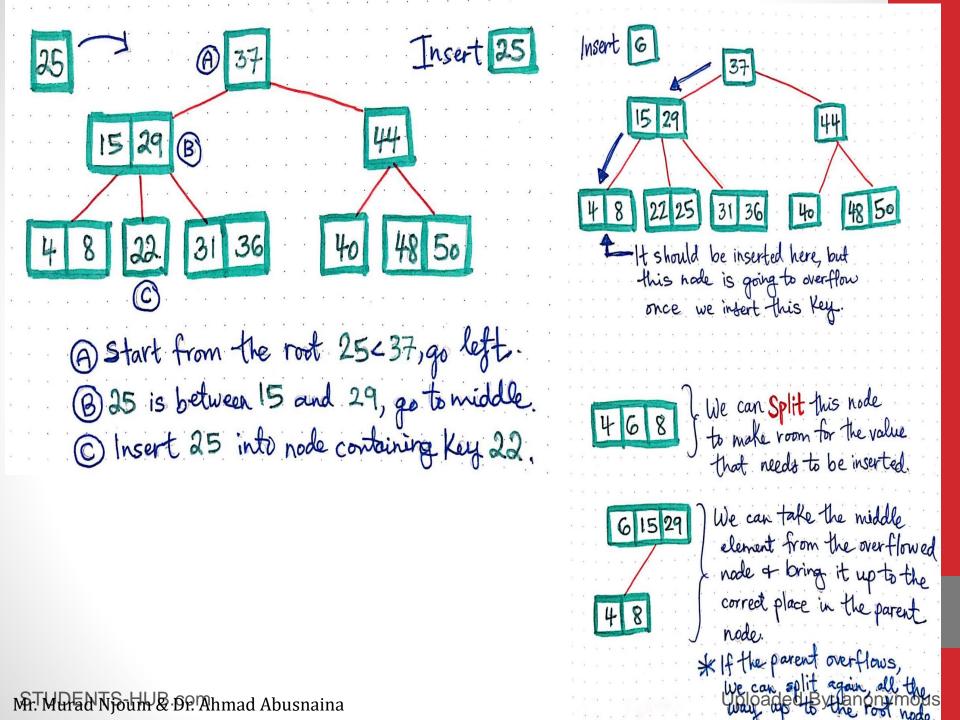
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Homework:

Insert the following elements 10,20,40,50,60,70,80,30,35,5,15,60 in a B-Tree of order M=4

Solution using <u>https://www.cs.usfca.edu/~galles/vi</u> <u>sualization/BTree.html</u>

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Homework : Insert the following elements 9,0,8,1,7,2,6,3,5,4, in a B-Tree of order M=3,

Solution using <u>https://www.cs.usfca.edu/~galles/vi</u> <u>sualization/BTree.html</u>

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THANK YOU

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