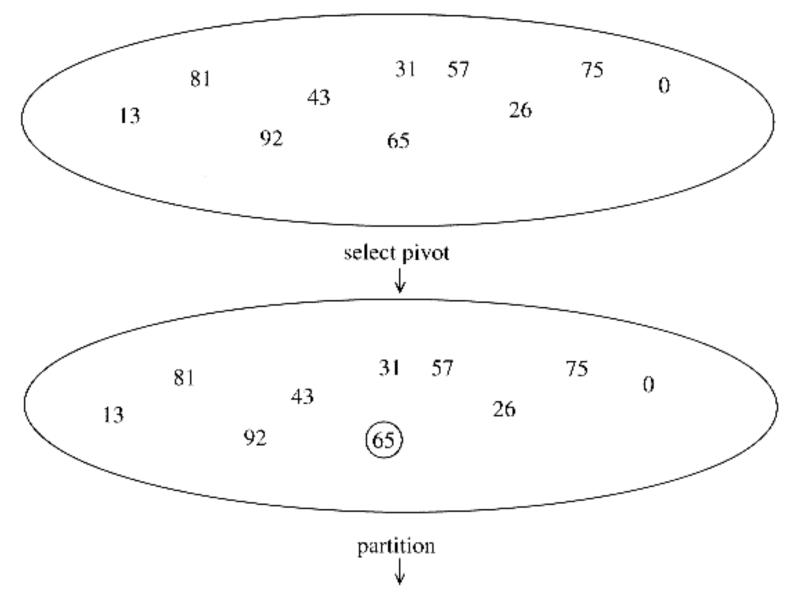


Sorting

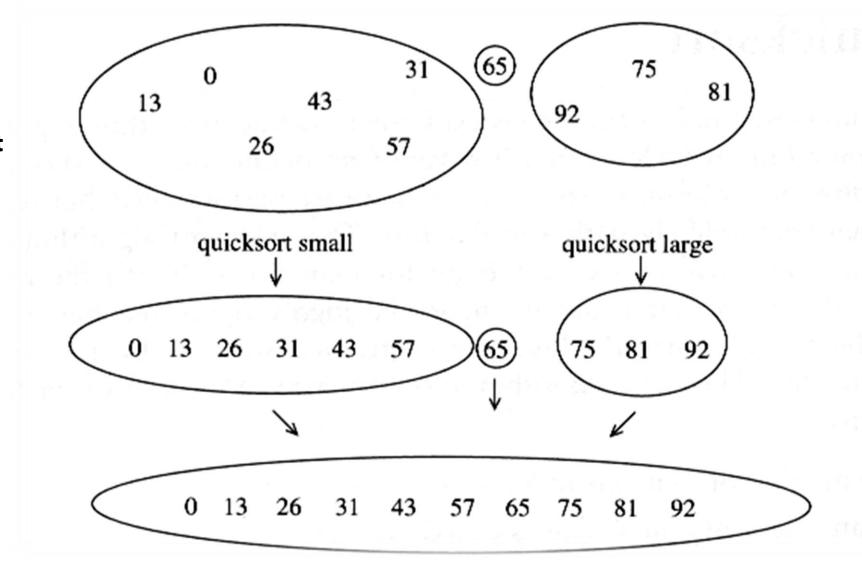
Dr. Abdallah Karakra

Computer Science Department
COMP242

Quick_sort



- 1. Choose the pivot randomly
- 2. Use the first element as pivot
- 3. Use the last element as pivot
- 4. Median-of-three partitioning



if (A[left]>A[center])
 swap (A[left],A[center])
if (A[left]>A[right])
 swap (A[left],A[right])
if (A[center]>A[right])
swap (A[center],A[right])

Swap (A[center], A[right-1])

How it works

While (Left>right)
moves i right, skipping over elements smaller than the pivot
moves j left, skipping over elements greater than the pivot

When both I && j have stopped swap (A[i], A[j])

```
if (A[left]>A[center])
  swap (A[left],A[center])
if (A[left]>A[right])
  swap (A[left],A[right])
if (A[center]>A[right])
swap (A[center],A[right])
```

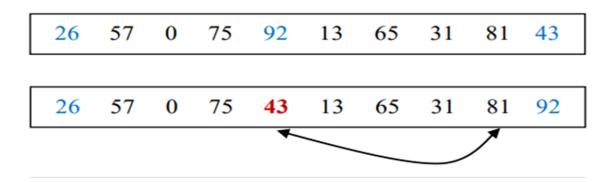
Swap (A[center],A[right-1])

Dr. Abdallah Karakra

26 57 0 75 92 13 65 31 81 43

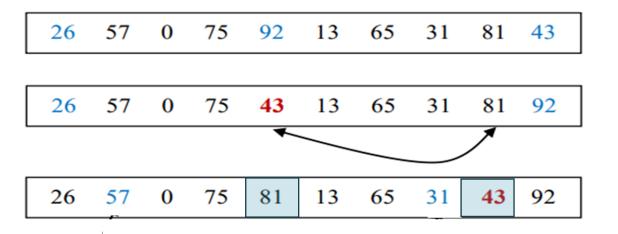
```
if (A[left]>A[center])
  swap (A[left],A[center])
if (A[left]>A[right])
  swap (A[left],A[right])
if (A[center]>A[right])
swap (A[center],A[right])
```

Swap (A[center],A[right-1])



```
if (A[left]>A[center])
  swap (A[left],A[center])
if (A[left]>A[right])
  swap (A[left],A[right])
if (A[center]>A[right])
  swap (A[center],A[right])
```

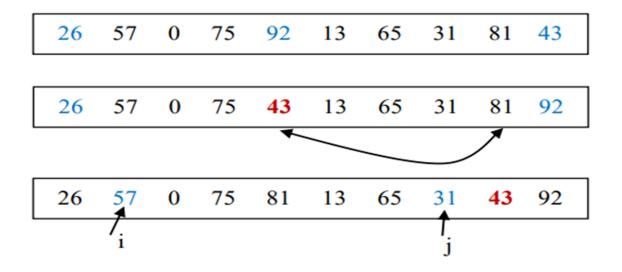
Swap (A[center],A[right-1])



While (Left<right)

moves i right, skipping over elements smaller than the pivot moves j left, skipping over elements greater than the pivot

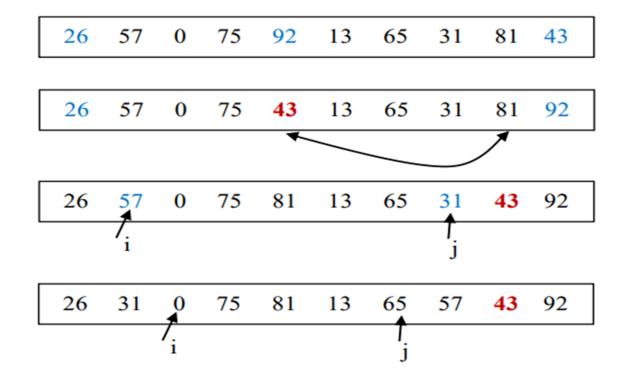
When both i && j have stopped swap (A[i], A[j])



While (Left<right)

moves i right, skipping over elements smaller than the pivot moves j left, skipping over elements greater than the pivot

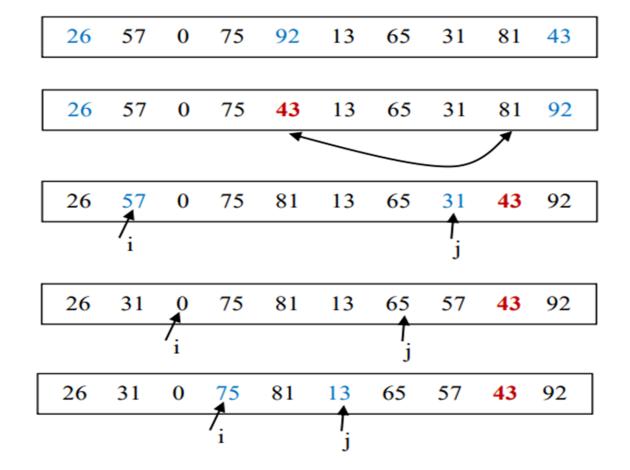
When both i && j have stopped swap (A[i], A[j])



While (Left<right)

moves i right, skipping over elements smaller than the pivot moves j left, skipping over elements greater than the pivot

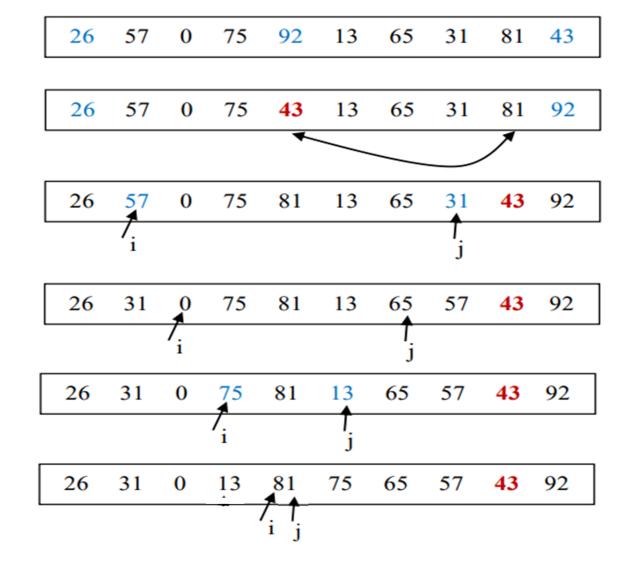
When both i && j have stopped swap (A[i], A[j])



While (Left<right)

moves i right, skipping over elements smaller than the pivot moves j left, skipping over elements greater than the pivot

When both i && j have stopped swap (A[i], A[j])

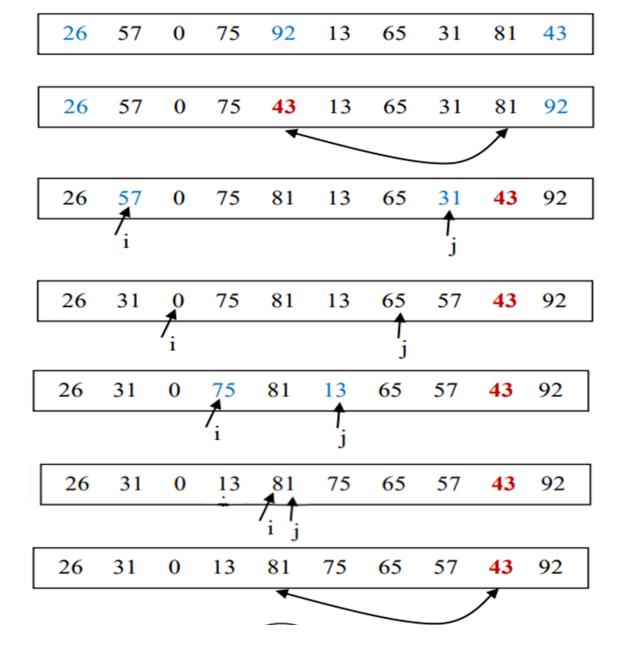


While (Left<right)

moves i right, skipping over elements smaller than the pivot moves j left, skipping over elements greater than the pivot

When both i && j have stopped swap (A[i], A[j])

swap (A[i], A[right-1])

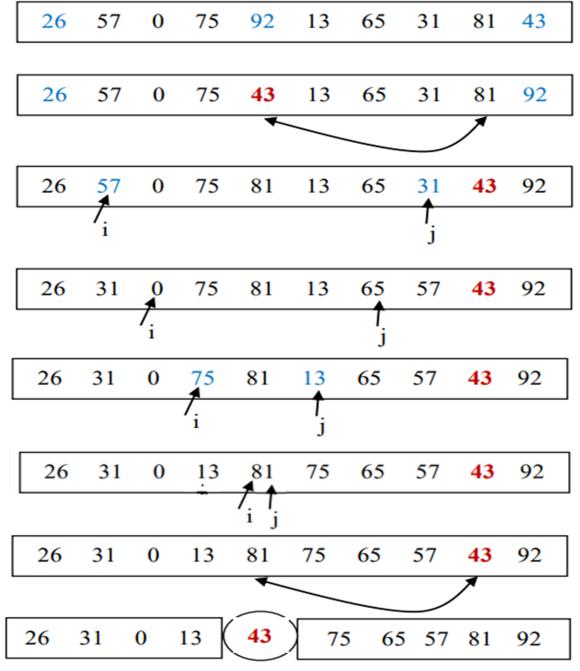


While (Left<right)

moves i right, skipping over elements smaller than the pivot moves j left, skipping over elements greater than the pivot

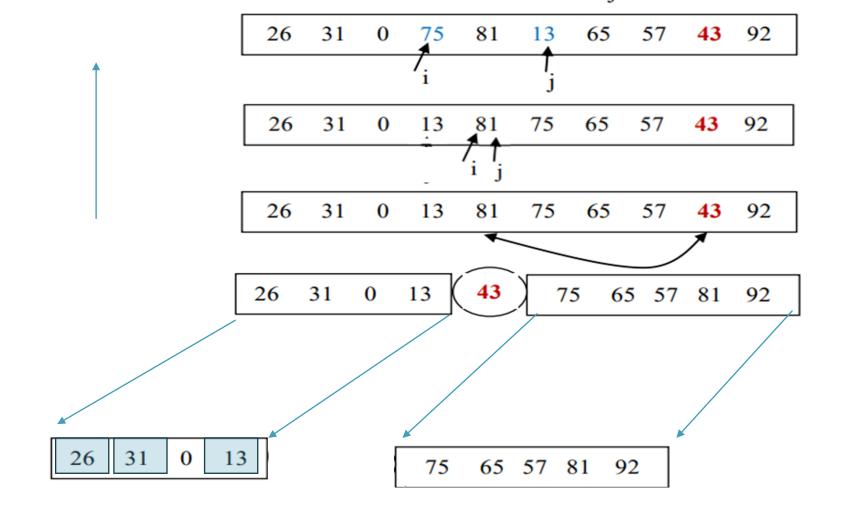
When both i && j have stopped swap (A[i], A[j])

swap (A[i], A[right-1])



if (A[left]>A[center])
 swap (A[left],A[center])
if (A[left]>A[right])
 swap (A[left],A[right])
if (A[center]>A[right])
swap (A[center],A[right])

Swap (A[center], A[right-1])



Quick sort

```
void q sort ( int [] A, int left, int right) {
      int i, j, pivot;
      if (left<right) {</pre>
                pivot=median3 (A,left,right);
                i=left;
                j=right-1;
                for (; ;) {
                      while (A[++i] < pivot);
                      while (A[--j]>pivot);
                         if (i<j)
                             swap (A[i], A[j])
                         else
                              break:
                swap (A[i],Aright-1]);
                q sort (A, left, i-1);
                q sort (A,i+1,right);
```

```
int median3 ( int [] A, int left, int right){
int center=(left+right)/2;
if (A[left]>A[center])
    swap (A[left],A[center])
 if (A[left]>A[right])
     swap (A[left],A[right])
   if (A[center]>A[right])
      swap (A[center], A[right])
   swap (A[center], A[right-1])
   return A[right-1]
```

Quick_sort

Worst case

Best case

$$T(n) = 2 T(n/2) + Cn$$
.

$$T(n) = O(n \log n)$$

> Average case

Insertion Sort

Example:

We color a sorted part in **green**, and an unsorted part in **black**. Here is an insertion sort step by step. We take an element from unsorted part and compare it with elements in sorted part, moving form right to left.

29, 20, 73, 34, 64

29, 20, 73, 34, 64

20, **29**, 73, 34, 64

20, **29**, **73**, 34, 64

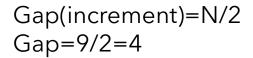
20, **29**, **34**, **73**, 64

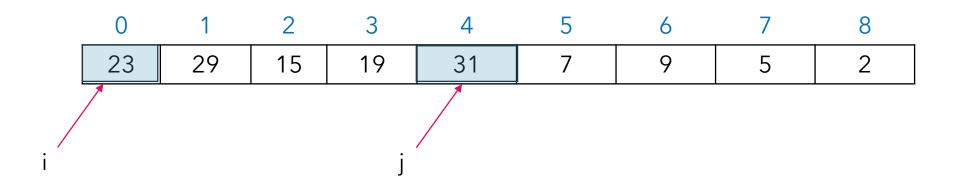
20, 29, 34, 64, 73

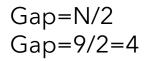
Case Study: Analysis Of Insertion Sort

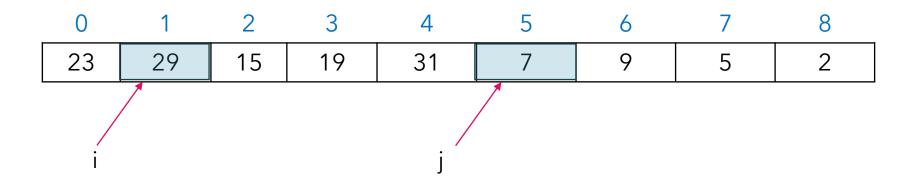
```
void insertionSort(int[] ar)
        int index,j;
        for (int i=1; i < ar.length; i++)
            index = ar[i];
            j = i;
            while (j > 0 \&\& ar[j-1] > index)
              ar[j] = ar[j-1];
               j--;
           ar[j] = index;
```

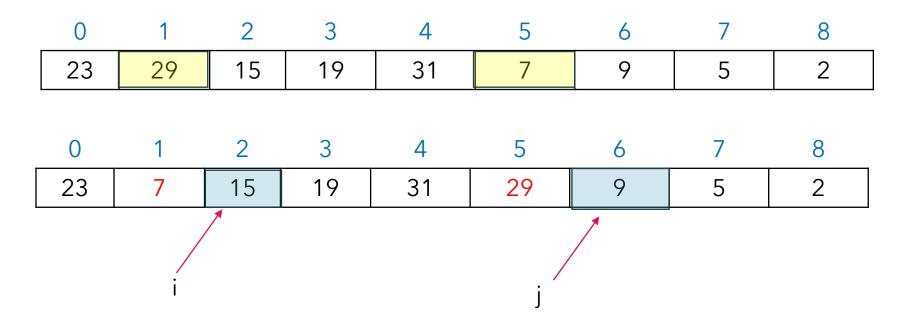
Shell sort











0	1	2	3	4	5	6	7	8
23	29	15	19	31	7	9	5	2
0	1	2	3	4	5	6	7	8
23	7	15	19	31	29	9	5	2
0	1	2	3	4	5	6	7	8
23	7	9	19	31	29	15	5	2
						. /	1	

0	1	2	3	4	5	6	7	8
23	29	15	19	31	7	9	5	2
0	1	2	3	4	5	6	7	8
23	7	15	19	31	29	9	5	2
0	1	2	3	4	5	6	7	8
23	7	9	19	31	29	15	5	2
0	1	2	3	4	5	6	7	8
23	7	9	5	31	29	15	19	2

0	1	2	3	4	5	6	7	8
23	29	15	19	31	7	9	5	2
	4	0	2	4			7	0
0	1	2	3	4	5	6	7	8
23	7	15	19	31	29	9	5	2
					-			
0	1	2	3	4	5	6	7	8
23	7	9	19	31	29	15	5	2
	-		-					
0	1	2	3	4	5	6	7	8
23	7	9	5	31	29	15	19	2
		•						•
0	1	2	3	4	5	6	7	8
23	7	9	5	2	29	15	19	31

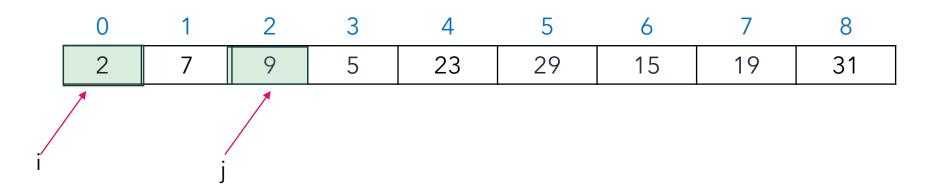
	0	1	2	3	4	5	6	7	8
	23	29	15	19	31	7	9	5	2
	0	1	2	3	4	5	6	7	8
	23	7	15	19	31	29	9	5	2
	0	1	2	3	4	5	6	7	8
	23	7	9	19	31	29	15	5	2
	0	1	2	3	4	5	6	7	8
	23	7	9	5	31	29	15	19	2
	0	1	2	3	4	5	6	7	8
	23	7	9	5	2	29	15	19	31
Swap i									1

Gap=N/2 Gap=9/2=4

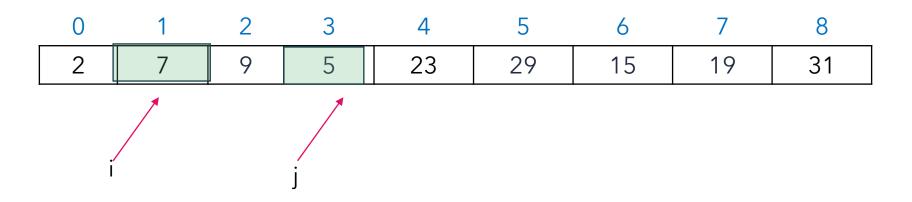
Uploaded By: Ayham Nobani

0	1	2	3	4	5	6	7	8
23	29	15	19	31	7	9	5	2
0	1	2	3	4	5	6	7	8
23	7	15	19	31	29	9	5	2
0	1	2	3	4	5	6	7	8
23	7	9	19	31	29	15	5	2
0	1	2	3	4	5	6	7	8
23	7	9	5	31	29	15	19	2
0	1	2	3	4	5	6	7	8
23	7	9	5	2	29	15	19	31
0	1	2	3	4	5	6	7	8
2	7	9	5	23	29	15	19	31

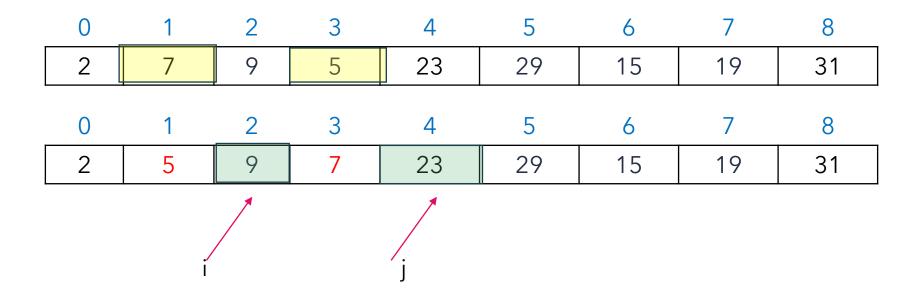
Gap=N/2	
Gap = 4/2 = 2	2



Gap=N/2	
Gap = 4/2 = 3	2



Gap=N/2	
Gap = 4/2 = 2	2



Gap=N/2
Gap = 4/2 = 2

0	1	2	3	4	5	6	7	8
2	7	9	5	23	29	15	19	31
0	1	2	3	4	5	6	7	8
2	5	9	7	23	29	15	19	31
					-			
0	1	2	3	4	5	6	7	8
2	5	9	7	23	29	15	19	31
		./ i	1	j	1			

Gap=N/2	
Gap = 4/2 = 2)

0	1	2	3	4	5	6	7	8
2	7	9	5	23	29	15	19	31
0	1	2	3	4	5	6	7	8
2	5	9	7	23	29	15	19	31
0	1	2	3	4	5	6	7	8
2	5	9	7	23	29	15	19	31
0	1	2	3	4	5	6	7	8
2	5	9	7	23	29	15	19	31
				i	/	j		

Gap=N/2	
Gap = 4/2 = 2)

0	1	2	3	4	5	6	7	8
2	7	9	5	23	29	15	19	31
	_		_	_	_	_	_	
0	1	2	3	4	5	6	7	8
2	5	9	7	23	29	15	19	31
0	1	2	3	4	5	6	7	8
2	5	9	7	23	29	15	19	31
					•			
0	1	2	3	4	5	6	7	8
2	5	9	7	23	29	15	19	31
0	1	2	3	4	5	6	7	8
2	5	9	7	15	29	23	19	31
					1		1	
					i	j	/	

0	1	2	3	4	5	6	7	8
2	7	9	5	23	29	15	19	31
0	1	2	3	4	5	4	7	8
	· ·	<u> </u>			ı	6		
2	5	9	7	23	29	15	19	31
0	1	2	3	4	5	6	7	8
2	5	9	7	23	29	15	19	31
								_
0	1	2	3	4	5	6	7	8
2	5	9	7	23	29	15	19	31
								_
0	1	2	3	4	5	6	7	8
2	5	9	7	15	29	23	19	31
0	1	2	3	4	5	6	7	8
2	5	9	7	15	19	23	29	31
	-	•	•	•	•	#	•	*

Insertion sort

0	1	2	3	4	5	6	7	8
2	5	9	7	15	19	23	29	31
0	1	2	3	4	5	6	7	8
2	5	9	7	15	19	23	29	31
0	1	2	3	4	5	6	7	8
2	5	9	7	15	19	23	29	31
0	1	2	3	4	5	6	7	8
2	5	7	9	15	19	23	29	31
0	1	2	3	4	5	6	7	8
2	5	7	9	15	19	23	29	31
0	1	2	3	4	5	6	7	8
2	5	7	9	15	19	23	29	31
0	1	2	3	4	5	6	7	8
2	5	7	9	15	19	23	29	31
0	1	2	3	4	5	6	7	8
2	5	7	9	15	19	23	29	31
0	1	2	3	4	5	6	7	8
2	5	7	9	15	19 l	Jploæded	By2Ayh	am Blobani

Example:

	Example.													
		0	1	2	3	4	5	6	7	8	9	10	11	12
	inc\Data	81	94	11	96	12	35	17	95	28	58	41	75	15
13/2	6	17	94	11	58	12	35	81	95	28	96	41	75	
10, _	6	15						17						81
		15	94	11	58	12	35	17	95	28	96	41	75	81
		15	12	11	58	94	35							
6/2	3	15	12	11	17	94	28	58	95	35	96			
S. =	3					41			94			95	75	
											81			96
		15	12	11	17	41	28	58	94	35	81	95	75	96
		12	15											
2/2		11	12	15	17	41								
3/2	1					28	41	58	94					
	1						35	41	58	94				
										81	94	95		
										75	81	94	95	96
OTUE	NTC LILID •	11	12	15	17	28	35	41	58	75	81	94	95 ed By	96 Ayha
SIUDE Dr. Abdallah K	Arakra	om									. (pload	ed By	Ayha

Shell sort

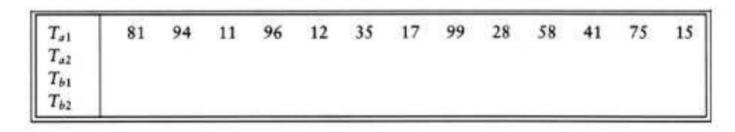
```
for (gap=N/2; gap>=1; gap=gap/2)\{ //No. of passes
  for (j=gap; j<N; j++){}
     for (i=j-gap;i>=0;i=i-gap){ //backward
         if (a[i+gap]>a[i]) {
            break;
         else{
          swap (a[i+gap],a[i])
```

Time complexity when gap=N/2 is O(N²)
Uploaded By: Ayham Nobani

External Sorting

All the internal sorting algorithms require that the input fit into main memory. There are, however, applications where the input is much too large to fit into memory. For those external sorting algorithms, which are designed to handle very large inputs

The basic external sorting algorithm uses the merge routine from merge sort. Suppose we have four tapes, Ta1, Ta2, Tb1, Tb2, which are two input and two output tapes. Depending on the point in the algorithm, the a and b tapes are either input tapes or output tapes. Suppose the data is initially on Ta1. Suppose further that the internal memory can hold (and sort) m records at a time. A natural first step is to read m records at a time from the input tape, sort the records internally, and then write the sorted records alternately to Tb1 and Tb2. We will call each set of sorted records a run. When this is done, we rewind all the tapes. Suppose we have the same input as our example for Shell sort



If m = 3, then after the runs are constructed, the tapes will contain the data indicated in the following figure.

T _{a1}							
T _{b1}	11	81	94	17	28	99	15
T ₆₂	12	35	96	41	58	75	

T_{a1}	11	12	35	81	94	96	15
Taz	17	28	35 41	81 58	94 75	96 99	
T 61							
T_{b2}							

Γ_{a1}												
F-2	100000000000000000000000000000000000000	2.20.409		-54000			1740 (1940)	Contact Contact				
T _{b1}	11	12	17	28	35	51	58	75	81	94	96	99
F62	1.5											

Summary

Continu Almorithma		Space Complexity		
Sorting Algorithms	Best Case	Average Case	Worst Case	Worst Case
Bubble Sort	O(n)	O(n^2)	O(n^2)	0(1)
Selection Sort	O(n^2)	O(n^2)	O(n^2)	0(1)
Insertion Sort	O(n)	O(n^2)	O(n^2)	0(1)
Merge Sort	O(nlogn)	O(nlogn)	O(nlogn)	O(n)
Quick Sort	O(nlogn)	O(nlogn)	O(n^2)	O(n)
Heap Sort	O(nlogn)	O(nlogn)	O(nlogn)	0(1)
Counting Sort	O(n + k)	O(n + k)	O(n + k)	O(k)
Radix Sort	O(nk)	O(nk)	O(nk)	O(n + k)
Bucket Sort	O(n + k)	O(n + k)	O(n^2)	O(n)