

Exercises:

7. The following estimated regression equation based on ten observations

$$\hat{y} = 29.127 + 0.5906 X_1 + 0.4980 X_2$$

$$SST = 6724.125$$

$$SSR = 6216.375$$

a. Find the SSE:

$$SSE = SST - SSR$$

$$= 6724.125 - 6216.375$$

$$= 507.75$$

b. Compute R^2 :

$$R^2 = \frac{SSR}{SST} = \frac{6216.375}{6724.125} = 0.92$$

c. Compute Adj R^2 :

$$\text{Adj } R^2 = 1 - (1 - R^2) \left(\frac{n-1}{n-p-1} \right)$$

$$= 1 - (1 - 0.92) \left(\frac{10-1}{10-2-1} \right) = \underline{0.90}$$

d. Comment on the goodness of fit.

8. $n = 10$, $p = 2$

$SST = 15182.9$ and $SSR = 14052.2$

a. Compute R^2 :

$$R^2 = \frac{SSR}{SST} = 0.93$$

b. Compute $\text{adj} R^2$:

$$\text{adj} R^2 = 1 - (1 - R^2) \left(\frac{n-1}{n-p-1} \right) = 1 - (1 - 0.93) \left(\frac{9}{7} \right) = 0.91$$

c. "pp" $\text{adj} R^2$

9. $n = 30$

$$\hat{y} = 17.6 + 3.8 X_1 - 2.3 X_2 + 1.6 X_3 + 2.7 X_4 \rightarrow p = 4$$

$SST = 1805$, $SSR = 1760$.

a. compute R^2 :

$$R^2 = \frac{SSR}{SST} = 0.98$$

b. compute $\text{adj} R^2$:

$$\text{adj} R^2 = 1 - (1 - R^2) \left(\frac{n-1}{n-p-1} \right) = 1 - (1 - 0.98) \left(\frac{29}{25} \right) = \underline{0.98}$$

10. $n = 10$

$$\hat{y} = 25 + 10X_1 + 8X_2 \quad S.S.E = 1200 \rightarrow p = 2$$

$$SST = 16000, \quad SSR = 12000$$

a. compute R^2 :

$$R^2 = \frac{SSR}{SST} = 0.75$$

b. compute $adj R^2$:

$$adj R^2 = 1 - (1 - R^2) \left(\frac{n-1}{n-p-1} \right) = 1 - (1 - 0.75) \left(\frac{9}{7} \right) = 0.68$$

c.

11. $\hat{y} = 83.2 + 2.29X_1 + 1.3X_2, \quad n = 8, \quad p = 2$

$$SST = 25.5, \quad SSR = 23.435$$

a. compute R^2 and $adj R^2$:

$$R^2 = \frac{SSR}{SST} = 0.92$$

$$adj R^2 = 1 - (1 - R^2) \left(\frac{n-1}{n-p-1} \right) = 1 - (0.08)(1.4) = 0.89$$