

Wireless and Mobile Networks, ENCS5323
Equations Sheet

Equations of Chapter 1

- Speed of light (c) $\rightarrow c = 3 \times 10^8$ meter/s
- Wave Length (λ) $\rightarrow \lambda = \frac{c \text{ (m/s)}}{f \text{ (Hz)}} = \frac{3 \cdot 10^8 \text{ (m/s)}}{f \text{ (Hz)}}$
- Convert to dB $\rightarrow P_{x,dB} = 10 \log_{10} P_x$
- Convert dB to dBm $\rightarrow X \text{ dB} = (X+30) \text{ dBm}$
- Nyquist channel capacity $\rightarrow C = 2B \log_2(M)$
- Shannon–Hartley theorem for Channel Capacity, $C = B \log_2(1 + \text{SNR})$
- Antenna Gain (G) and Antenna Effective Area (A_e) $\rightarrow G = \frac{4\pi A_e}{\lambda^2} = \frac{4\pi f^2 A_e}{c^2}$
- Free Space Path Loss (L_p) $\rightarrow L_p = \frac{(4\pi d)^2}{\lambda^2} = \frac{(4\pi f d)^2}{c^2}$
- Power Received (P_r) $\rightarrow P_r = \frac{P_t G_t G_r A_t A_r}{L_p L_f L_o F_{margin}}$, A_t : Amplifier at transmitter, A_r : Amplifier at receiver, L_f : feeders (cables) losses. L_o : other losses, F_{margin} : Fading Margin.
- Effective Isotropic Radiated Power (EIRP) $\rightarrow EIRP = \frac{P_t A_t G_t}{L_{f,t} L_{o,t}}$, $L_{f,t}$: cable loss at transmitter, $L_{o,t}$: other losses at transmitter.
- Doppler Shift $\rightarrow f_d = \frac{v}{\lambda} \cos \theta$, v is the moving speed
- Frequency deviation due to doppler shift $\rightarrow f_r = f_c - f_d$, f_c : frequency of source
- Diameter of First Fresnel Zone in foot $\rightarrow D_3 = 72.1 \sqrt{\frac{(D1)(D2)}{f(D1 + D2)}}$, $D1$ and $D2$ in miles
- Thermal Noise Power at receiver (N) $\rightarrow N = kTB_w$; k : Boltzmann's constant (1.38×10^{-23} W/Kelvin-Hz)
- Spectral noise density (N_0) $\rightarrow N_0 = \frac{N}{B_w} = kT$, B_w : Bandwidth at receiver

- $\frac{E_b}{N_0}$ before modulator $\rightarrow \left(\frac{E_b}{N_0}\right)_{\text{at detector}} = \frac{P_r}{kTN_{f,\text{total}}R}$, $N_{f,\text{total}}$: Noise figure of receiver
- $\frac{E_b}{N_0}$ margin before modulator (M) $\rightarrow M = \frac{P_r}{kTN_{f,\text{total}}R\left(\frac{E_b}{N_0}\right)_{\text{required}}}$
- Power Received (P_r) based on a reference distance power $\rightarrow P_r(d) = P_r(d_o) \left(\frac{d_o}{d}\right)^\gamma$
- Power Received (P_r) based on a reference distance power and shadowing $\rightarrow P_r(d) = P_r(d_o) \left(\frac{d_o}{d}\right)^\gamma + X_\sigma$

Equations of Chapter 2

- Throughput of pure ALOHA, $S_{th} = gTe^{-2gT}$
- Throughput of slotted ALOHA, $S_{th} = gTe^{-gT}$
- Throughput unslotted nonpersistent CSMA, $S_{th} = \frac{Ge^{-2\alpha T}}{G(1+2\alpha) + e^{-\alpha G}}$
- Throughput slotted nonpersistent CSMA, $S_{th} = \frac{\alpha Ge^{-2\alpha T}}{G(1 - e^{-2\alpha G}) + \alpha}$
- Throughput unslotted 1-persistent CSMA,

$$S_{th} = \frac{G \left[1 + G + \alpha G \left(1 + G + \frac{\alpha G}{2} \right) \right] e^{-G(1+2\alpha)}}{G(1 + 2\alpha) - (1 - e^{-2\alpha G}) + (1 + \alpha G)e^{-G(1+\alpha)}}$$

- Throughput slotted 1-persistent CSMA,

$$S_{th} = \frac{G(1 + \alpha - e^{-\alpha G})e^{-G(1+\alpha)}}{(1 + \alpha)(1 - e^{-\alpha G}) + \alpha e^{-G(1+\alpha)}}$$