

$$10. \lim_{t \rightarrow 1} \frac{t^3 - 1}{4t^3 - t - 3}$$

$$\lim_{t \rightarrow 1} \frac{3t^2}{12t^2 - 1}$$

$$\frac{3}{12-1} = \frac{3}{11}$$

$\frac{0}{0}$

7.5

$\lim_{x \rightarrow 0}$

$\frac{0}{0}, \frac{\infty}{\infty}$
↓
L'Hôpital

$\infty \cdot 0, \infty - \infty$
↓
نقطه
تقاطع

$\frac{\infty}{\infty}, \frac{0}{0}, \dots$
↓
 $f(x) = e^{\ln f(x)}$

$$21. \lim_{x \rightarrow 0} \frac{x^2}{\ln(\sec x)}$$

$$\frac{0}{\ln 1} = \frac{0}{0}$$

$$\lim_{x \rightarrow 0} \frac{2x}{\frac{\sec x \tan x}{\sec x}} = \lim_{x \rightarrow 0} \frac{2x}{\tan x} \quad \frac{0}{0}$$

$$= \lim_{x \rightarrow 0} \frac{2}{\sec^2 x} = \frac{2}{1^2} = 2$$

$$34. \lim_{x \rightarrow 0^+} \frac{\ln(e^x - 1)}{\ln x}$$

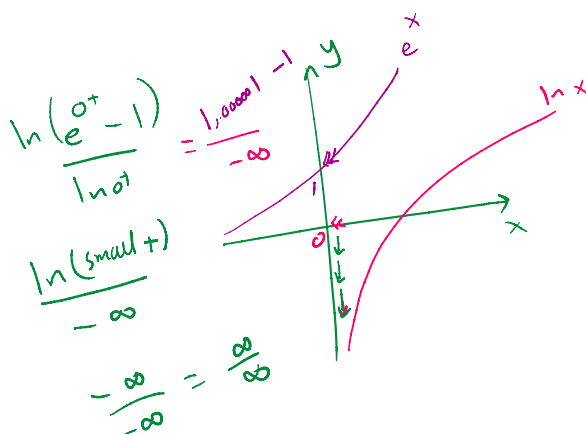
$$= \lim_{x \rightarrow 0^+} \frac{\frac{e^x}{e^x - 1}}{\frac{1}{x}}$$

$$= \lim_{x \rightarrow 0^+} \frac{x e^x}{e^x - 1}$$

$$\frac{0}{1-1} = \frac{0}{0}$$

$$= \lim_{x \rightarrow 0^+} \frac{x e^x + e^x}{e^x}$$

$$= \lim_{x \rightarrow 0^+} \frac{e^x (x+1)}{e^x} = \lim_{x \rightarrow 0^+} (x+1) = 0+1 = 1$$



$$= \lim_{x \rightarrow 0^+} \frac{x e^{-1/x}}{e^x} = \lim_{x \rightarrow 0^+} \frac{x}{e^x}$$

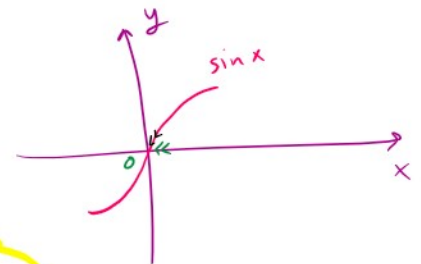
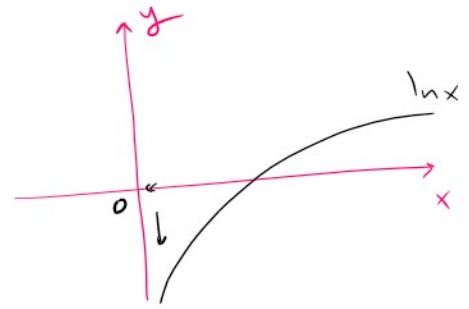
38. $\lim_{x \rightarrow 0^+} (\ln x - \ln \sin x)$

$-\infty - \ln 0^+$

$-\infty - -\infty$

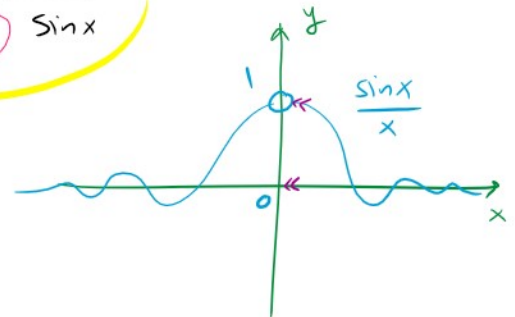
$-\infty + \infty$

$\infty - \infty$



$$\lim_{x \rightarrow 0^+} \ln \frac{x}{\sin x} = \ln \lim_{x \rightarrow 0^+} \frac{x}{\sin x}$$

cont.
on +



$$= \ln \lim_{x \rightarrow 0^+} \frac{1}{\frac{\sin x}{x}}$$

$$= \ln \frac{1}{1} = \ln 1 = 0$$

52. $\lim_{x \rightarrow 1^+} x^{1/(x-1)}$

f(x)

$\frac{1}{\text{small}^+}$

$$= \infty$$

power

$$f(x) = e^{\ln f(x)}$$

$$\lim_{x \rightarrow 1^+} e^{\frac{1}{x-1} \ln x}$$

$$= \lim_{x \rightarrow 1^+} e^{\frac{1}{x-1} \ln x}$$

$$\lim_{x \rightarrow 1^+} \frac{\ln x}{x-1} = \frac{0}{0}$$

$$e^{\ln 7} = 7$$

$$\underline{\underline{e^{\ln f} = f}}$$

$$= e$$

$$= \lim_{x \rightarrow 1^+} \frac{\frac{1}{x}}{1} = \lim_{x \rightarrow 1^+} \frac{1}{x} = \frac{1}{e} = e$$

$$\lim_{x \rightarrow 0^+} \sin x \cdot \ln x$$

$$\lim_{x \rightarrow 0^+} \frac{\ln x}{\frac{1}{\sin x}}$$

$\frac{1}{\sin x}$
small +

$$(0) \cdot (-\infty)$$

not power

$$\lim_{x \rightarrow 0^+} \frac{\ln x}{\csc x}$$

$$\lim_{x \rightarrow 0^+} \frac{\frac{1}{x}}{-\csc x \cot x}$$

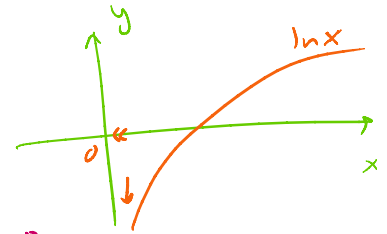
$$\lim_{x \rightarrow 0^+} \frac{\frac{1}{x}}{\frac{1}{\sin x} \frac{\cos x}{\sin x}}$$

$$\lim_{x \rightarrow 0^+} \frac{\sin x \tan x}{x}$$

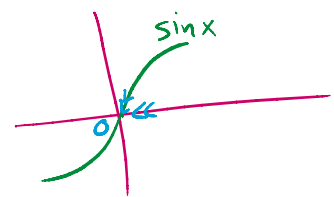
$$\lim_{x \rightarrow 0^+} \frac{\sin x}{x} \quad \lim_{x \rightarrow 0^+} \tan x$$

$$= (1)(0)$$

$$= 0$$



$-\infty$
 ∞



$\frac{0}{0}$

$$46. \lim_{x \rightarrow \infty} x^2 e^{-x} = (\infty) \cdot (0)$$

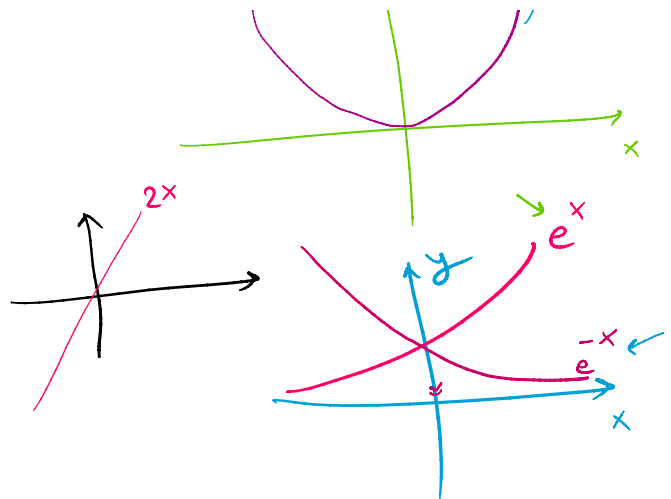


$$x \rightarrow \infty = (\infty)(0)$$

$$\lim_{x \rightarrow \infty} \frac{x^2}{e^x} = \frac{\infty}{\infty}$$

$$\lim_{x \rightarrow \infty} \frac{2x}{e^x} = \frac{\infty}{\infty}$$

$$\lim_{x \rightarrow \infty} \frac{2}{e^x} = 2 \lim_{x \rightarrow \infty} e^{-x} = (2)(0) = 0$$



49. $\lim_{\theta \rightarrow 0} \frac{\theta - \sin \theta \cos \theta}{\tan \theta - \theta}$

$$\frac{0-0}{0-0} = \frac{0}{0}$$

$$\lim_{\theta \rightarrow 0} \frac{1 - (-\sin \theta \sin \theta + \cos \theta \cos \theta)}{\sec^2 \theta - 1}$$

$$1 - \cos^2 \theta = \sin^2 \theta$$

$$\lim_{\theta \rightarrow 0} \frac{1 + \sin^2 \theta - \cos^2 \theta}{\sec^2 \theta - 1}$$

$$\lim_{\theta \rightarrow 0} \frac{\sin^2 \theta + \sin^2 \theta}{\tan^2 \theta} = \lim_{\theta \rightarrow 0} \frac{2 \sin^2 \theta}{\tan^2 \theta}$$

$$1. \dots \tan^2 \theta$$

$$\lim_{\theta \rightarrow 0} 2 \sin^2 \theta \cot^2 \theta$$

$$\lim_{\theta \rightarrow 0} 2 \cancel{\sin^2 \theta} \frac{\cancel{\cos^2 \theta}}{\cancel{\sin^2 \theta}}$$

$$2 \lim_{\theta \rightarrow 0} \cos^2 \theta = 2 (1^2) = 2$$