

L19 - part 2

ENEE2360 Analog Electronics

T10: FET Amplifiers ac small signal analysis

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1

$g_m = \frac{\partial I_D}{\partial V_{GS}} \rightarrow \frac{A}{V} = \frac{1}{\Omega} \times$
 $= \Omega^{-1} \times$
 $= \text{mho} \times$
 $= \text{Siemens} \checkmark$

JFET
 DMOSFET $\rightarrow I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2$
 EMOSFET $\rightarrow I_D = K_n (V_{GS} - V_T)^2$

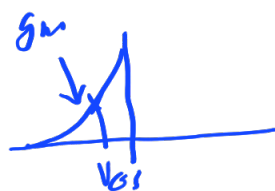
Definition: Transconductance

g_m

For JFETs and DMOSFETs

$$g_m = \frac{\partial I_D}{\partial V_{GS}} = \frac{2I_{DSS}}{|V_P|} \left[1 - \frac{V_{GS}}{V_P}\right]$$

$$g_m = g_{m0} \left[1 - \frac{V_{GS}}{V_P}\right] = g_{m0} \sqrt{\frac{I_D}{I_{DSS}}}$$



always positive

$$g_{m0} = \frac{2I_{DSS}}{|V_P|} = g_m|_{V_{GS}=0}$$

For EMOSFET

$$I_D = K(V_{GS} - V_{GS(TH)})^2$$

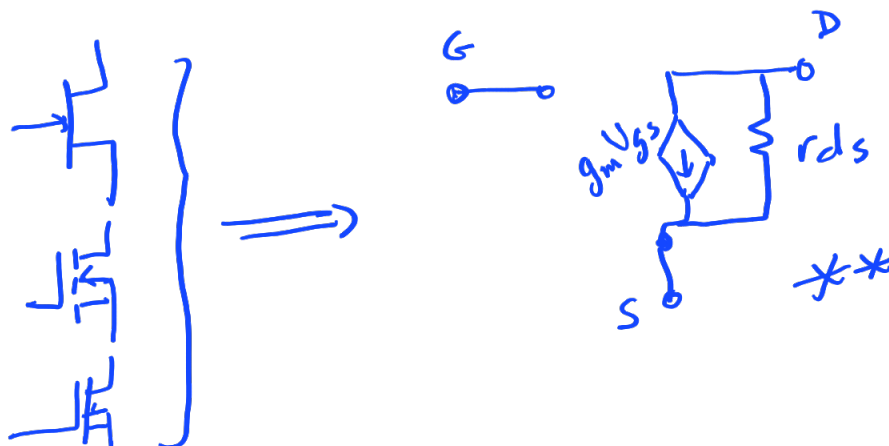
$$g_m = \frac{\partial I_D}{\partial V_{GS}} = 2K(V_{GS} - V_{GS(TH)})$$

$$(V_{GS} - V_{GS(TH)}) = \sqrt{\frac{I_D}{K}}$$

$$K = \frac{I_{D(on)}}{(V_{GS(on)} - V_{GS(TH)})^2}$$

$$\therefore g_m = 2K \sqrt{\frac{I_D}{K}} = 2\sqrt{I_D K}$$

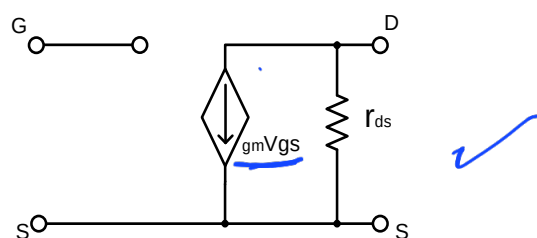
operating point



AC Small Signal Equivalent Circuit (MODEL Valid for all FET Types)

- In ac

$$g_m = \frac{i_d}{v_{gs}} \Rightarrow i_d = g_m v_{gs}$$

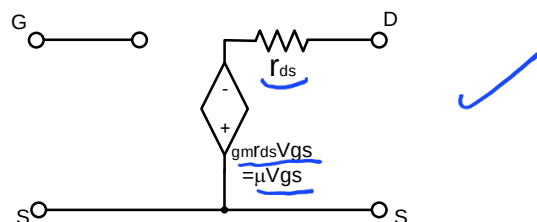


Source Transformation

- Or

$$\mu = g_m r_{ds} \text{ - amplification factor}$$

unitless



$$g_m v_{gs} r_{ds} = \frac{g_m r_{ds} v_{gs}}{1} = \mu v_{gs}$$

FET amplifiers

same ac eq. circuit {

1. Common Source (CS)	$\Rightarrow$	CE
2. " Drain (CD)	$\Rightarrow$	CC
3. " Gate (CG)	$\Rightarrow$	CB

BJT

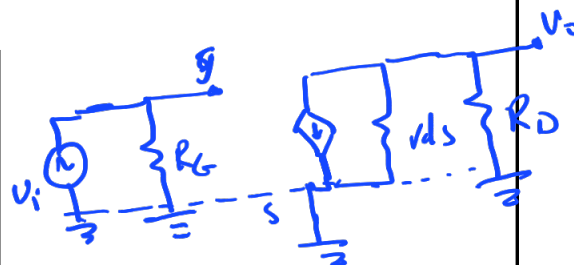
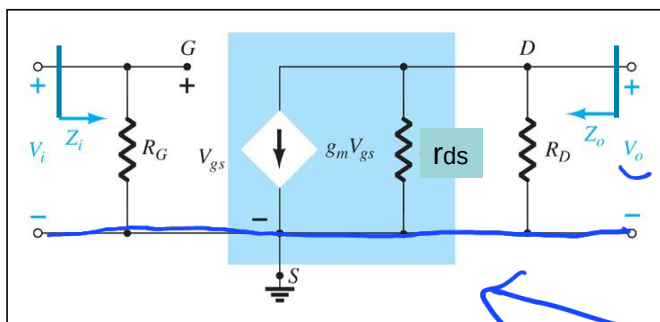
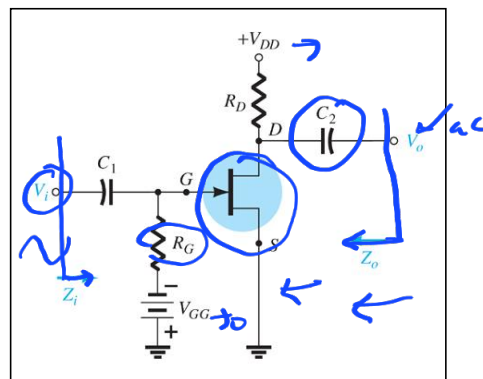
Common-Source (CS) Fixed-Bias

The input is applied to the gate and the output is taken from the drain

There is a 180° phase shift between the circuit input and output

To construct ac ss equivalent circuit

- 1) C_1 & C_2 are replaced by short
- 2) $V_{DD}=0$ V (short), $V_{GG}=0 \rightarrow$ short
- 3) FET ac ss MODEL



Calculations

Input impedance:

$$Z_i = R_G$$

Output impedance:

$$Z_o \Big|_{V_i=0} = R_D \parallel r_{ds}$$

$$Z_o \Big|_{V_i=0} \cong R_D \quad r_{ds} \geq 10 R_D$$

Voltage gain:

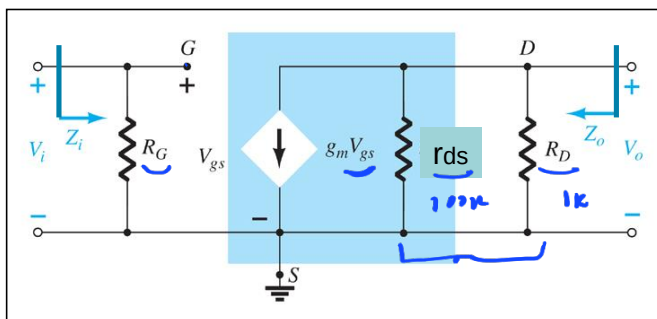
$$V_i = V_{gs}$$

$$V_o = V_{ds}$$

$$A_v = \frac{V_o}{V_i} = \frac{V_{ds}}{V_{gs}}$$

$$V_{ds} = -g_m V_{gs} (r_{ds} \parallel R_D)$$

$$, V_{gs} = V_i$$



$$A_v = \frac{V_o}{V_i} ; V_o = (R_D \parallel r_{ds}) - g_m V_{gs}$$

$$A_v = \frac{V_{ds}}{V_{gs}} = -g_m (r_{ds} \parallel R_D)$$

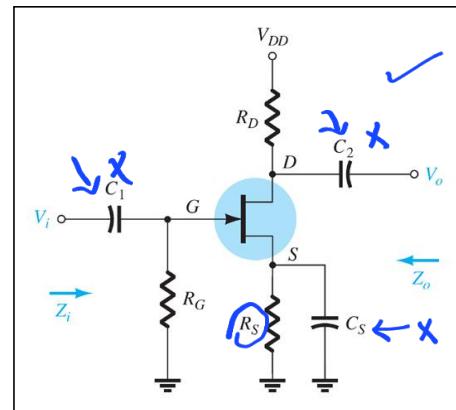
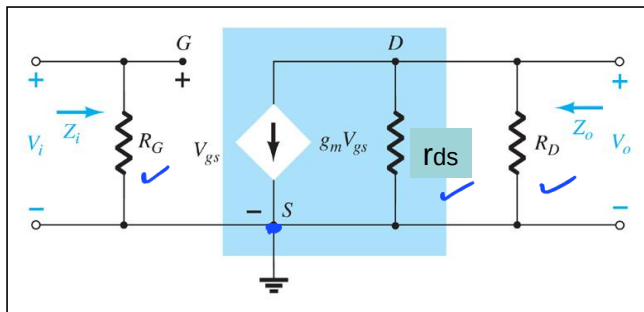
$$A_v = \frac{V_o}{V_i} = -g_m R_D \quad r_{ds} \geq 10 R_D$$

$\sim \rightarrow \sim$

180° shift $\rightarrow$ $\times -1$

Common-Source (CS) Self-Bias

This is a common-source amplifier configuration, so the input is applied to the gate and the output is taken from the drain.



There is a 180° phase shift between input and output.

Calculations

Input impedance:

$$Z_i = R_G$$

Output impedance:

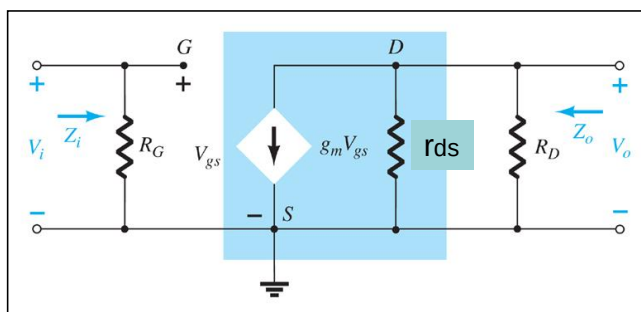
$$Z_o = r_{ds} || R_D$$

$$Z_o \cong R_D \Big|_{r_{ds} \geq 10 R_D}$$

Voltage gain:

$$A_v = -g_m (r_{ds} || R_D)$$

$$A_v \cong -g_m R_D \Big|_{r_{ds} \geq 10 R_D}$$



*same as
previous
circuit*

$$V_o = -g_m V_{gs} R_D \quad \dots (1) \quad \rightarrow \quad \frac{V_o}{V_{gs}} = -g_m R_D$$

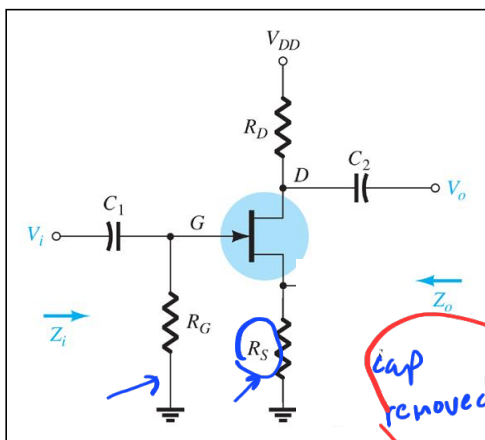
$$V_{gs} = V_g - V_s ; V_g = V_i, V_s = g_m V_{gs} R_s$$

$$V_{gs} = V_i - g_m V_{gs} R_s \Rightarrow V_i = V_{gs} (1 + g_m R_s) \quad \dots (2)$$

$$\frac{V_{gs}}{V_i} = \frac{1}{1 + g_m R_s}$$

Common-Source (CS) Self-Bias

Effect of R_s (ignore r_{ds}) $\rightarrow r_{ds} = \infty$



$$A_v = \frac{V_o}{V_i}$$

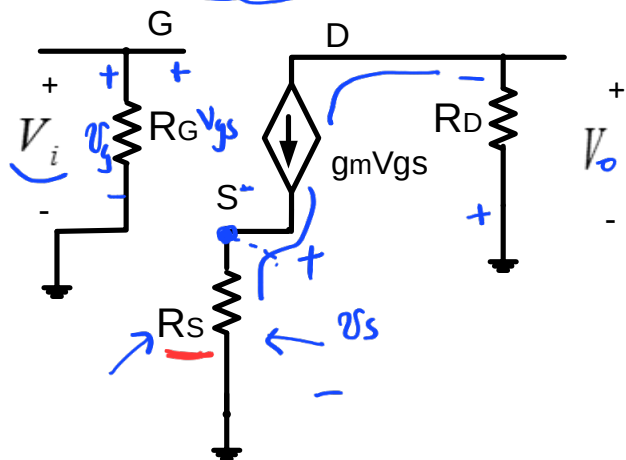
$$V_o = -g_m V_{gs} (R_D)$$

$$V_s = g_m V_{gs} (R_s)$$

$$V_g = V_i$$

$$V_{gs} = V_g - V_s = V_i - g_m V_{gs} R_s$$

$$\Rightarrow V_i = V_{gs} + g_m V_{gs} R_s$$

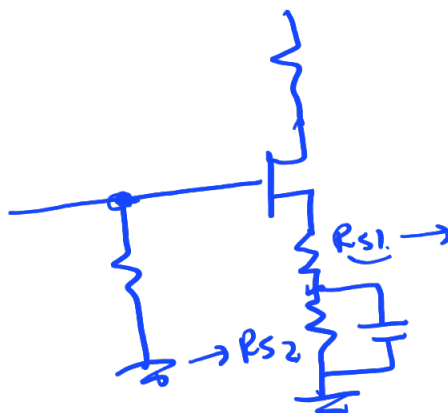


$$A_v = \frac{V_o}{V_i} = \frac{-g_m V_{gs} R_D}{V_{gs} + g_m V_{gs} R_s}$$

$$A_v = \frac{-g_m R_D}{1 + g_m R_s}$$

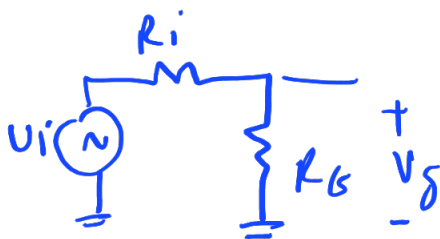
Gain is reduced due to R_s

previous circuit without R_s



$$R_{s1} + R_{s2} = R_s$$

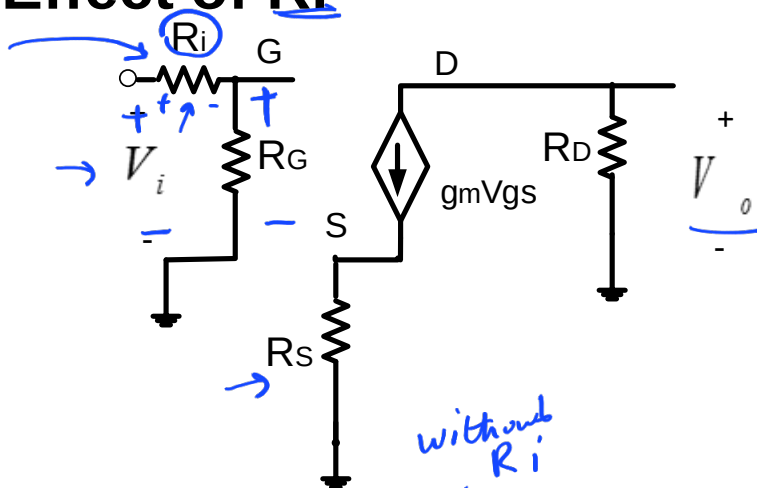
$\uparrow$
dc



$V_i = V_g \rightarrow \text{without } R_i$

$V_g = V_i \frac{R_G}{R_G + R_i} *$

Common-Source (CS) Self-Bias Effect of R_i



$$A_v = \frac{V_o}{V_i}$$

$$V_o = -g_m V_{gs} (R_D)$$

$$V_s = g_m V_{gs} (R_S)$$

$$V_g = \frac{R_G}{R_G + R_i} V_i$$

$$V_{gs} = V_g - V_s = \frac{R_G}{R_G + R_i} V_i - g_m V_{gs} R_S$$

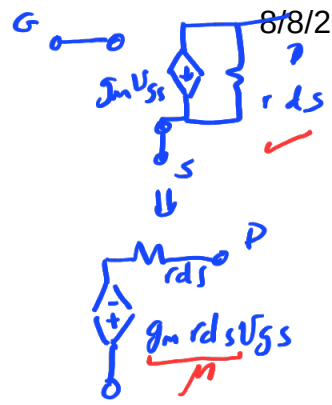
$$\Rightarrow V_i = V_{gs} (1 + g_m R_S) \frac{R_G + R_i}{R_G}$$

$$A_v = \frac{V_o}{V_i} = \frac{-g_m R_D}{1 + g_m R_S} \frac{R_G}{R_G + R_i}$$

Gain is reduced more due to R_i

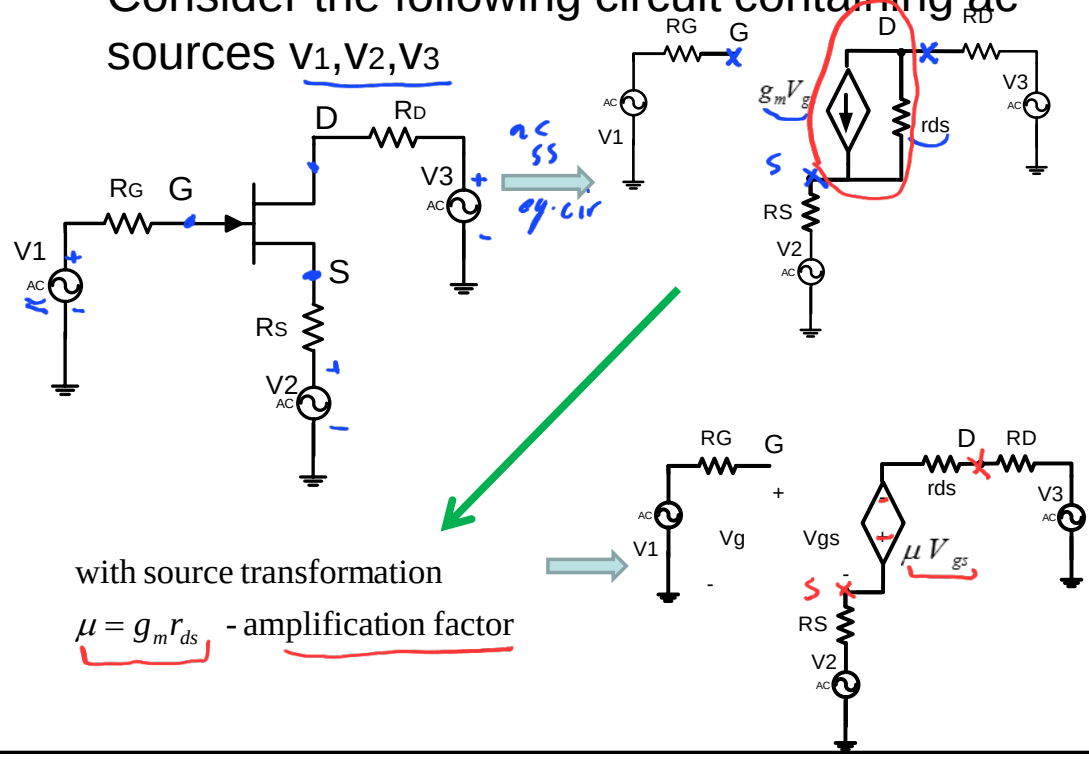
End of L19
12/8/2021

FET's $\rightarrow$ ss equivalent circuit $\rightarrow$



Impedance Reflection

- Consider the following circuit containing ac sources V_1, V_2, V_3



with source transformation
 $\mu = g_m r_{ds}$ - amplification factor

Impedance Reflection

KVL for the drain - source loop

$$V_3 - i_D R_D - i_D r_{ds} - i_D R_S + \mu V_{gs} - V_2 = 0 \dots \dots \dots (1)$$

but

$$V_{gs} = V_g - V_s = V_g - (i_D R_S + V_2) \dots \dots \dots (2)$$

substituting (2) in (1) yields:

$$V_3 - i_D R_D - i_D r_{ds} - i_D R_S + \mu (V_g - (i_D R_S + V_2)) - V_2 = 0$$

$$V_3 - i_D R_D - i_D r_{ds} - i_D R_S + \mu V_g - \mu i_D R_S - \mu V_2 - V_2 = 0$$

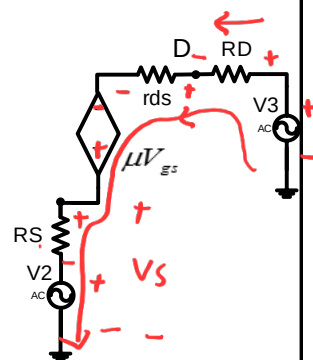
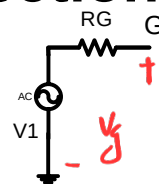
$$V_3 - i_D R_D - i_D r_{ds} - i_D R_S (\mu + 1) + \mu V_g - V_2 (\mu + 1) = 0$$

$$i_D R_D + i_D r_{ds} + i_D R_S (\mu + 1) = V_3 + \mu V_g - V_2 (\mu + 1)$$

$$V_3 - i_D R_D - i_D r_{ds} - i_D R_S + \mu (V_g - (i_D R_S + V_2)) - V_2 = 0$$

$$i_D = \frac{V_3 + \mu V_g - V_2 (\mu + 1)}{R_D + r_{ds} + R_S (\mu + 1)} \dots \dots \dots (3) *$$

(3) is the drain Equivalent circuit equation



→ i_D ?

original circuit

$$i_D = \frac{V_3 + \mu V_g - V_2(\mu + 1)}{R_D + r_{ds} + R_s(\mu + 1)} \dots\dots\dots (3)$$

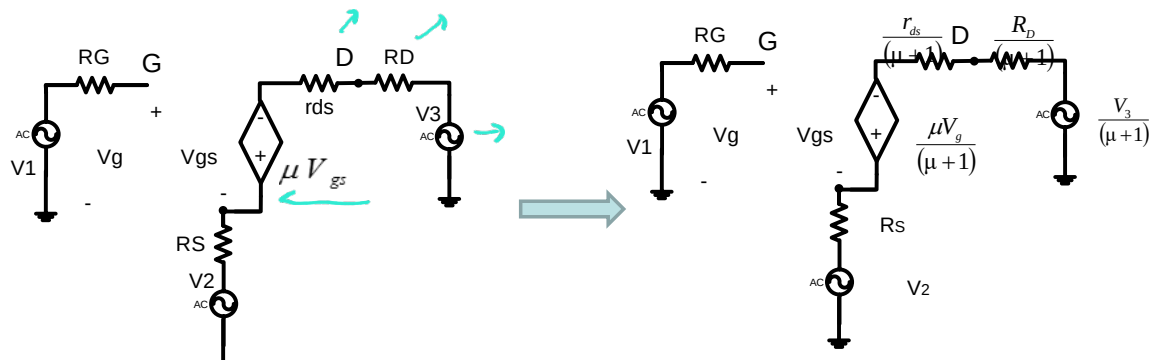
(3) is the drain Equivalent circuit equation

Reflection from Source to Drain

$$\mu V_{gs} \Rightarrow \mu V_g$$

$$R_s \Rightarrow R_s(\mu + 1)$$

$$V_2 \Rightarrow V_2(\mu + 1)$$



divide eq. (3) by $(\mu + 1)$

$$i_D = \frac{\frac{V_3}{(\mu + 1)} + \frac{\mu V_g}{(\mu + 1)} - V_2}{\frac{R_D}{(\mu + 1)} + \frac{r_{ds}}{(\mu + 1)} + R_S} \dots\dots\dots(4)$$

(4) is the source equivalent circuit equation

Reflection Drain to Source

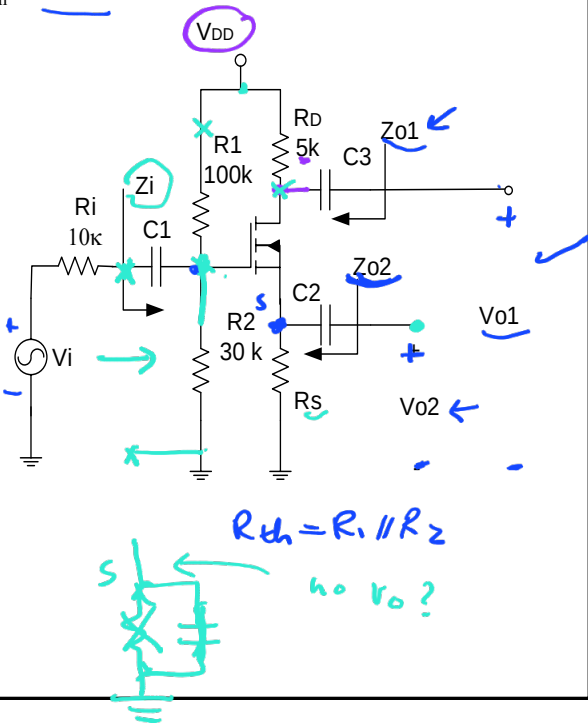
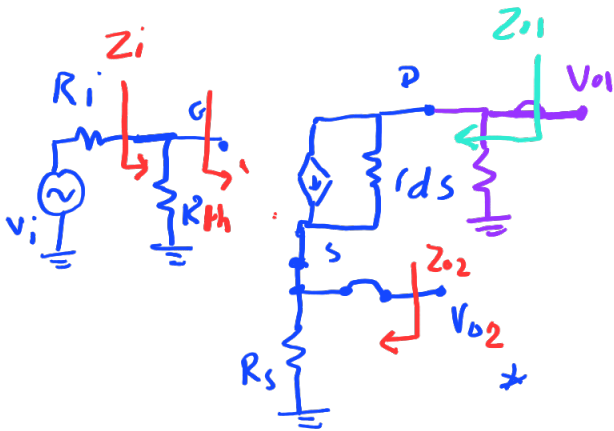
$$\mu V_{gs} \Rightarrow \frac{\mu V_g}{(\mu + 1)}$$
$$R_D \Rightarrow \frac{R_D}{(\mu + 1)}$$
$$r_{ds} \Rightarrow \frac{r_{ds}}{(\mu + 1)}$$
$$v_3 \Rightarrow \frac{v_3}{(\mu + 1)}$$

Example: Phase Splitting circuit

- Two outputs:
 - Vo1 from drain
 - Vo2 from source

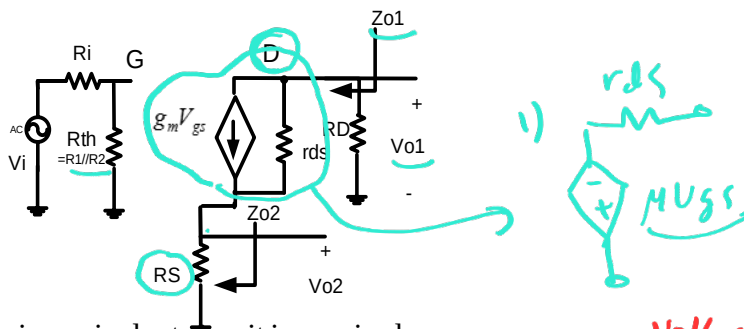
$r_{ds} = 100\text{ k}\Omega$
 $g_m = 1\text{ mS}$

Find A_v, A_i, Z_{O1}, Z_{O2} and Z_i

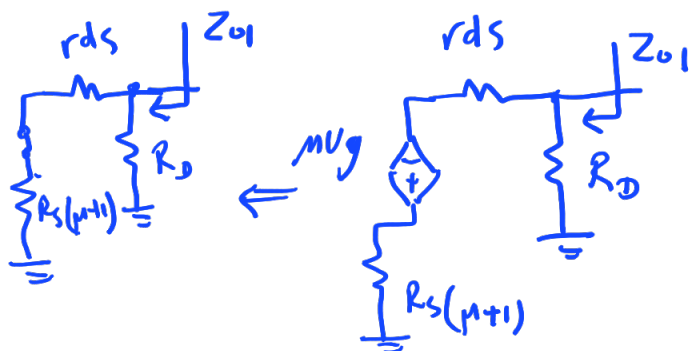
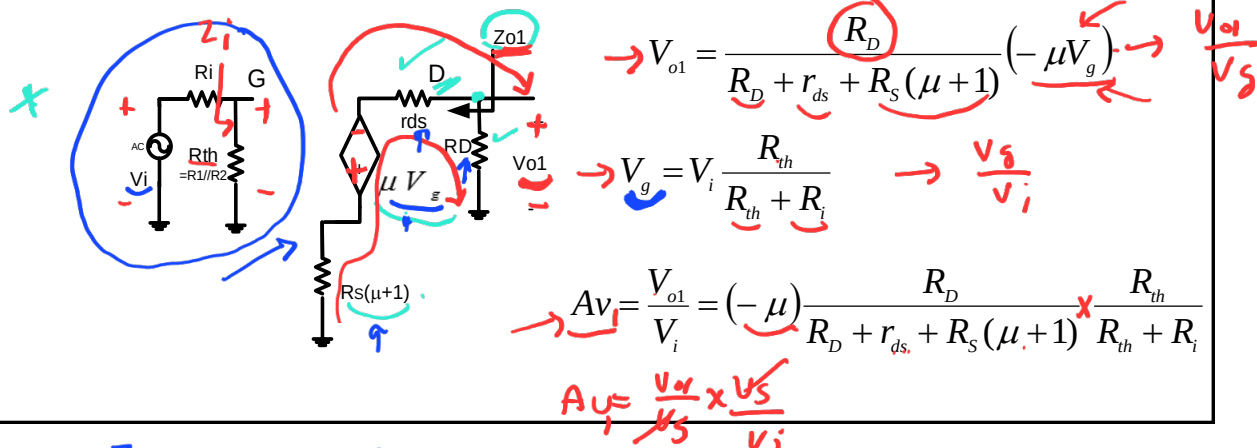


$Z_{in} = R_{th}$

Solution: ac ss equivalent circuit



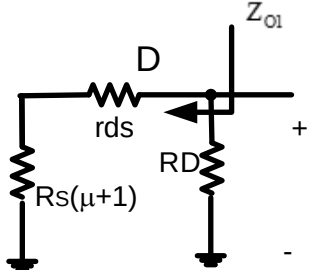
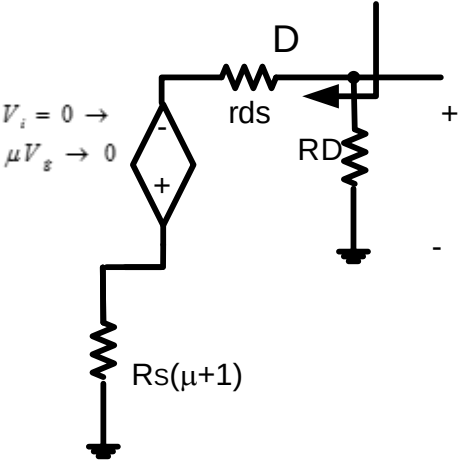
1) To Find Z_{O1} , V_{O1} Drain equivalent circuit is required since both of these quantities are seen from the drain



$$Z_{O1} = R_D \parallel (r_{ds} + R_S(\mu+1))$$

$$\begin{aligned} V_i &= 0 \\ V_g &= 0 \\ \mu V_g &= 0 \\ &\text{(Short)} \end{aligned}$$

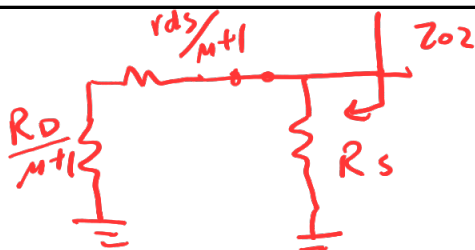
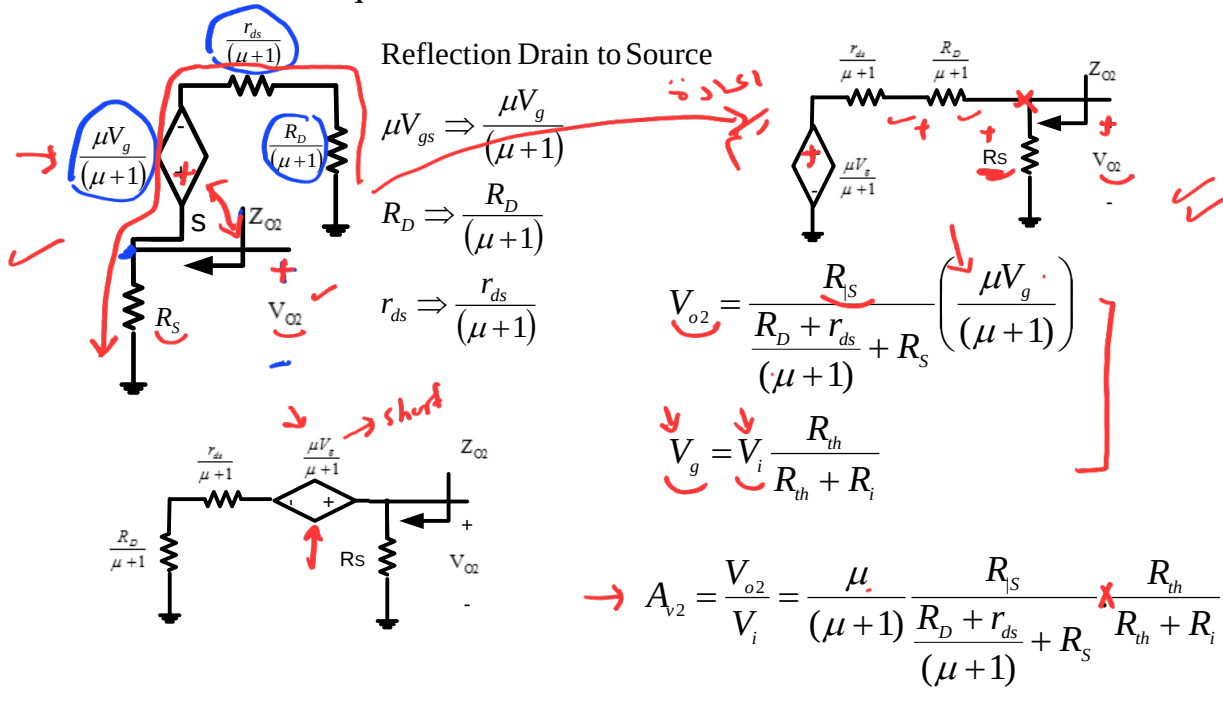
2) To Find $Z_{O1}|_{V_i=0, V_g=0}$



$$Z_{O1}|_{V_i=0, V_g=0} = R_D // [r_{ds} + R_s(\mu+1)]$$

Solution: continued

3) To Find Z_{O2} , V_{O2} Source equivalent circuit is required since both of these quantities are seen from the source



$$Z_{O2} = R_S \parallel \left(\frac{r_{ds} + R_D}{\mu + 1} \right)$$

$V_i = 0$
 $V_S = 0$
 $\frac{\mu V_S}{\mu + 1} = 0$

if $r_{ds} \rightarrow \infty$

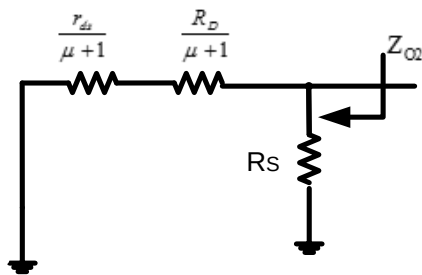
$$Z_{O2} \Big|_{r_{ds} \rightarrow \infty} = R_S \parallel \frac{1}{g_m}$$

$$Z_{O2} = R_S \parallel \frac{r_{ds} + R_D}{\mu + 1}$$

$$\lim_{r_{ds} \rightarrow \infty} \frac{r_{ds} + R_D}{\mu + 1} = \lim_{r_{ds} \rightarrow \infty} \frac{r_{ds} + R_D}{g_m r_{ds} + 1} = \lim_{r_{ds} \rightarrow \infty} \frac{1 + \frac{R_D}{r_{ds}}}{g_m + \frac{1}{r_{ds}}} = \frac{1}{g_m}$$

Solution: continued

4) To Find $Z_{O2} \Big|_{V_i=0, V_g=0}$



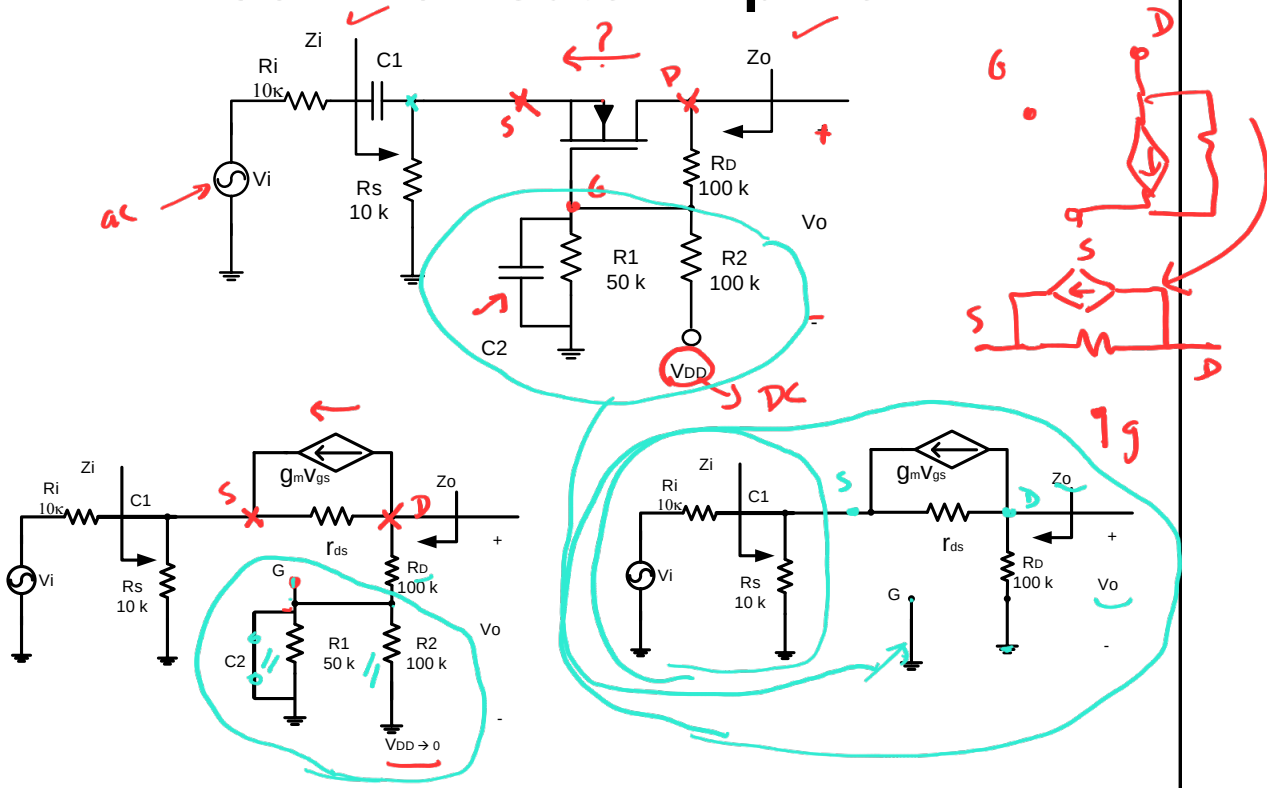
$$Z_{O2} \Big|_{V_i=0, V_g=0} = R_S \parallel \left[\frac{r_{ds} + R_D}{(\mu + 1)} \right]$$

$$Z_{O2} \Big|_{V_i=0, V_g=0} \Big|_{r_{ds} \rightarrow \infty} = R_S \parallel \frac{1}{g_m}$$

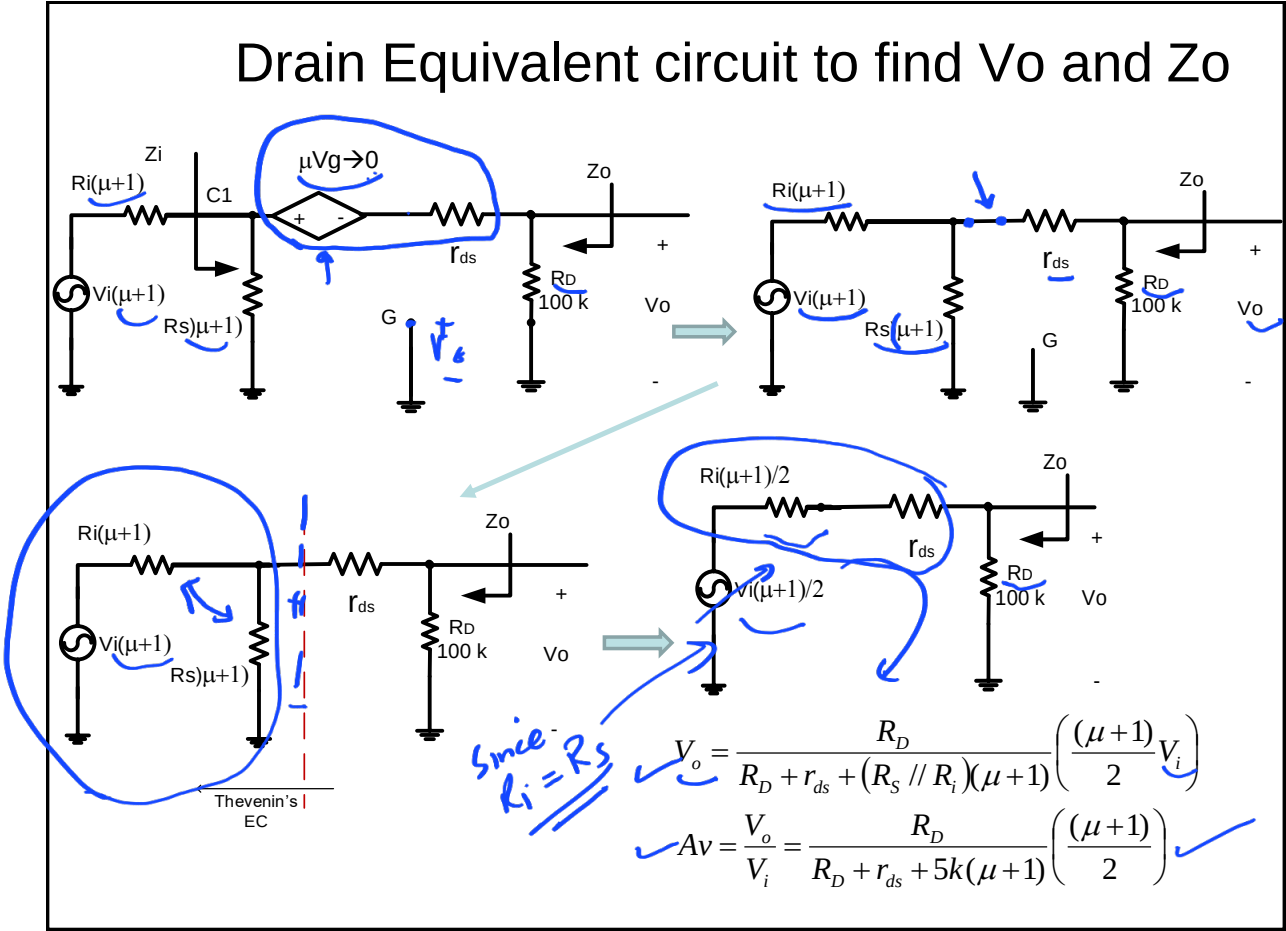
since $\lim_{r_{ds} \rightarrow \infty} \frac{r_{ds} + R_D}{\mu + 1} = \lim_{r_{ds} \rightarrow \infty} \frac{\frac{r_{ds}}{r_{ds}} + \frac{R_D}{r_{ds}}}{\frac{g_m r_{ds}}{r_{ds}} + \frac{1}{r_{ds}}} = \lim_{r_{ds} \rightarrow \infty} \frac{1 + \frac{R_D}{r_{ds}}}{g_m + \frac{1}{r_{ds}}} = \frac{1}{g_m}$ ✓

$$Z_i = R_{th} = R_1 \parallel R_2$$

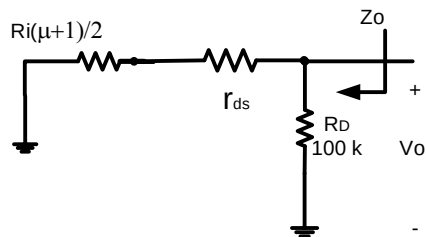
Common Gate Amplifier



$\mu V_{gs} \rightarrow \mu V_g \rightarrow$
 $R_i = R_s \leftarrow$ in this example



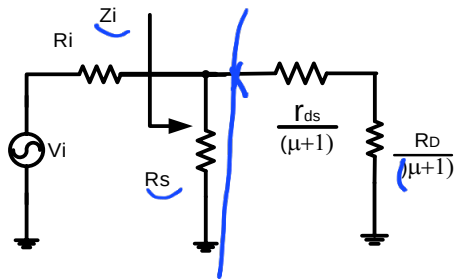
- Drain Equivalent circuit to find V_o and Z_o



$$Z_o|_{V_i=0} = R_D // \left(r_{ds} + \frac{R_i(\mu+1)}{2} \right)$$

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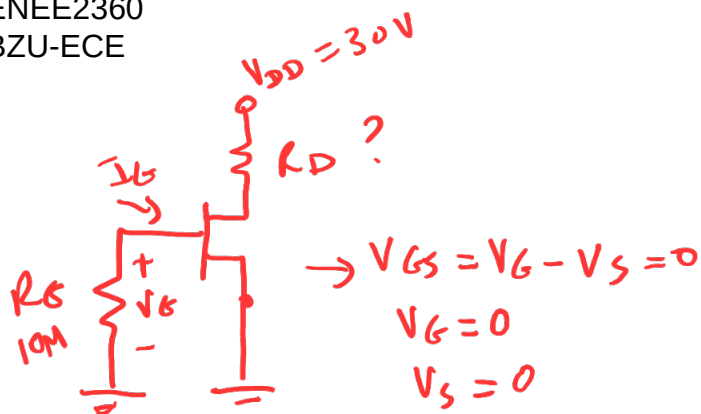
- To find Z_i source equivalent circuit is needed



$$Z_i = R_S \parallel \left[\frac{r_{ds} + R_D}{(\mu + 1)} \right]$$

$$Z_i \Big|_{r_{ds} \rightarrow \infty} = R_S \parallel \frac{1}{g_m}$$

End of L20



L21

16-8-2021

$$g_m = \frac{2 I_{DSS}}{|V_P|} \left(1 - \frac{V_{GS}}{V_P}\right)$$

$$= \frac{2 \times 10 \text{ mA}}{4} = 5 \text{ mS}$$

FET Amplifier Design (Important)

- Design a fixed bias network such that the ac voltage gain $|A_v| = 10$, i.e. find value of R_D .

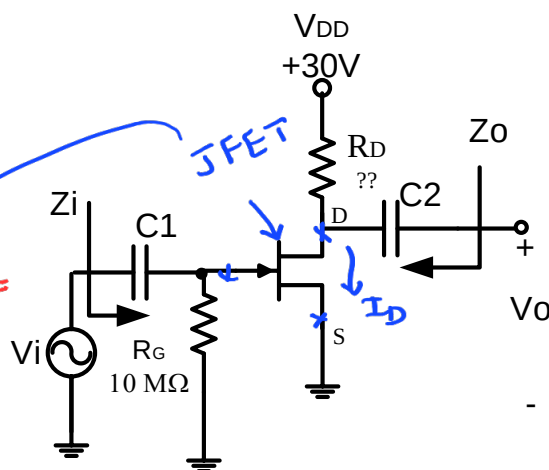
$$V_P = -4 \text{ V}$$

$$I_{DSS} = 10 \text{ mA}$$

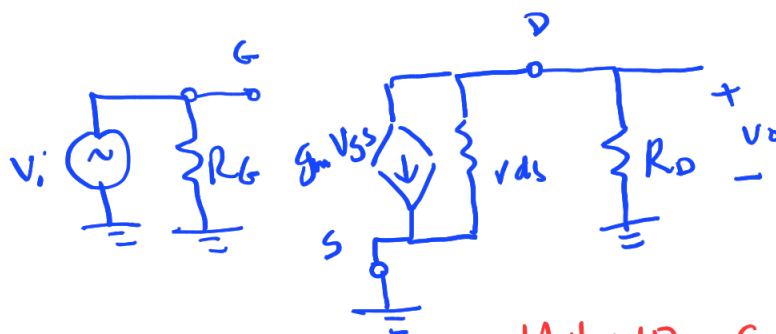
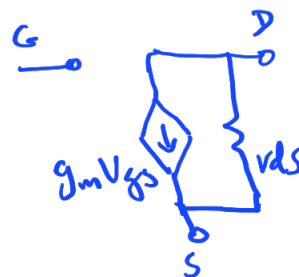
$$r_{ds} = 50 \text{ k}\Omega$$

$$g_m = \frac{\partial I_D}{\partial V_{GS}}$$

$$= \frac{2 I_{DSS}}{|V_P|} \left(1 - \frac{V_{GS}}{V_P}\right)$$



DC analysis
AC analysis
 $A_v = f(g_m, r_{ds})$



$$A_v = \frac{V_o}{V_i}$$

$$V_o = -g_m V_{GS} (r_{ds} \parallel R_D)$$

$$V_{GS} = V_i$$

$$A_v = -g_m (r_{ds} \parallel R_D)$$

$$|A_v| = 10 = g_m \frac{r_{ds} \cdot R_D}{r_{ds} + R_D}$$

$\therefore R_D =$ Uploaded By: anonymous

Solution

ac ss equivalent circuit

$$V_{GS} = V_G - V_S = 0V$$

$$I_D = I_{DSS} \left(1 - \frac{0}{-4} \right)^2 = I_{DSS} = 10mA$$

For JFETs

$$g_m = \frac{2I_{DSS}}{|V_P|} \left[1 - \frac{V_{GS}}{V_P} \right]$$

$$= \frac{2(10mA)}{|-4|} \left[1 - \frac{0}{-4} \right] = 5 mS$$

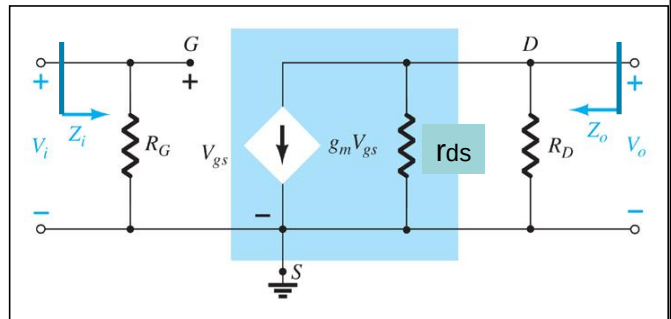
$$V_{gs} = V_i$$

$$A_v = \frac{V_o}{V_i}$$

$$V_o = -g_m V_{gs} (r_{ds} || R_D)$$

$$V_o = -g_m V_i (r_{ds} || R_D)$$

$$|A_v| = \left| \frac{V_o}{V_i} \right| = | -g_m (r_{ds} || R_D) |$$



Since A_v & g_m are known, then

$$|A_v| = \left| \frac{V_o}{V_i} \right| = | -g_m (r_{ds} || R_D) | = 10$$

$$\therefore (r_{ds} || R_D) = \frac{10}{g_m} = \frac{10}{5 mS} = 2 k\Omega$$

Substitute $r_{ds} = 50 k\Omega$

$$(r_{ds} || R_D) = \frac{r_{ds} \cdot R_D}{r_{ds} + R_D} = \frac{50 k\Omega \cdot R_D}{50 k\Omega + R_D} = 2 k\Omega$$

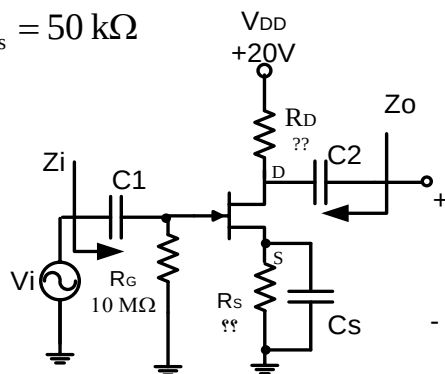
$$\rightarrow R_D = \frac{2 k\Omega \cdot 50 k\Omega}{48 k\Omega} = 2.08 k\Omega$$

Design Example 2 (Important)

Choose the values of R_D and R_S that will result in

voltage gain $|A_v| = 8$ using the value of g_m defined at $V_{GSQ} = \frac{1}{4} V_p$

$$\left\{ \begin{array}{l} V_p = -4 \text{ V} \\ I_{DSS} = 10 \text{ mA} \\ r_{ds} = 50 \text{ k}\Omega \end{array} \right.$$



$$\begin{aligned} g_m &= \frac{2I_{DSS}}{|V_p|} \left(1 - \frac{V_{GS}}{V_p} \right) \\ g_m &= \frac{2I_{DSS}}{4} \left(1 - \frac{-1}{-4} \right) \\ &= \frac{2 \times 10 \text{ mA}}{4} \left(1 - \frac{1}{4} \right) \\ &= 3.75 \text{ mS} \end{aligned}$$

Solution (value of R_D ?)

ac ss equivalent circuit

$$g_m = \frac{2I_{DSS}}{|V_p|} \left[1 - \frac{V_{GS}}{V_p} \right]$$

$$= \frac{2(10\text{mA})}{|-4|} \left[1 - \frac{-1}{-4} \right] = 3.75 \text{ mS} \quad \checkmark$$

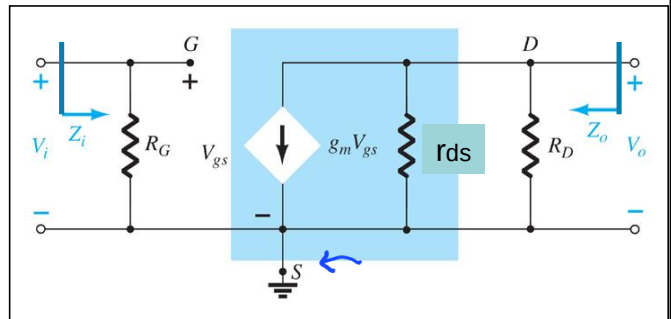
$$V_{gs} = V_i$$

$$A_v = \frac{V_o}{V_i}$$

$$V_o = -g_m V_{gs} (r_{ds} || R_D)$$

$$V_o = -g_m V_i (r_{ds} || R_D)$$

$$|A_v| = \left| \frac{V_o}{V_i} \right| = | -g_m (r_{ds} || R_D) |$$



Since A_v & g_m are known, then

$$|A_v| = \left| \frac{V_o}{V_i} \right| = | -g_m (r_{ds} || R_D) | = 8 \quad \checkmark \checkmark ? \checkmark$$

$$\therefore (r_{ds} || R_D) = \frac{8}{g_m} = \frac{8}{3.75 \text{ mS}} = 2.133 \text{ k}\Omega \quad \checkmark$$

Substitute $r_{ds} = 50 \text{ k}\Omega$

$$(r_{ds} || R_D) = \frac{r_{ds} \cdot R_D}{r_{ds} + R_D} = \frac{50 \text{ k}\Omega \cdot R_D}{50 \text{ k}\Omega + R_D} = 2.133 \text{ k}\Omega$$

$$\rightarrow R_D = \frac{2.133 \text{ k}\Omega \cdot 50 \text{ k}\Omega}{47.867 \text{ k}\Omega} = 2.22 \text{ k}\Omega$$

Value of R_s ?

The value of R_s is determined from DC analysis

Given

$$V_{GS} = V_G - V_S = \frac{1}{4} V_P = -1 \quad \checkmark$$

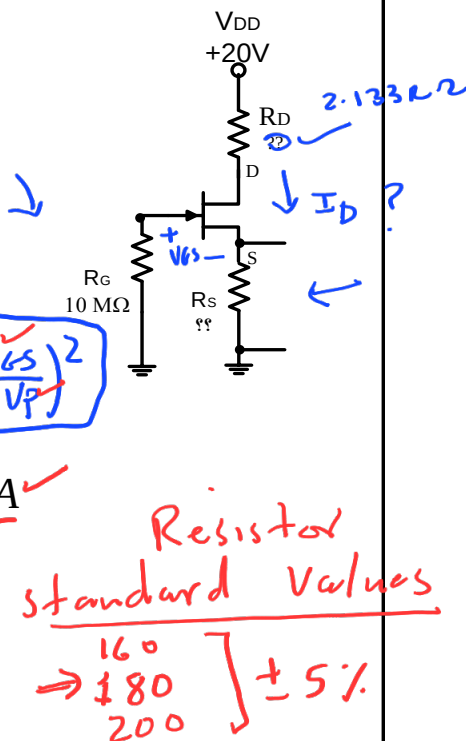
$$V_G = 0 \quad ?$$

$$V_S = I_D R_s = 1 \quad \text{0.75}$$

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P} \right)^2$$

$$\text{but } I_D = I_{DSS} \left(1 - \frac{-1}{-4} \right)^2 = I_{DSS} \cdot 0.5625 = 5.625 \text{ mA} \quad \checkmark$$

$$\therefore R_s = \frac{V_S}{I_D} = \frac{1 \text{ V}}{5.625 \text{ mA}} = 177.8 \, \Omega \quad \leftarrow$$



Design Example 3

Choose the values of R_D and R_S that will result in

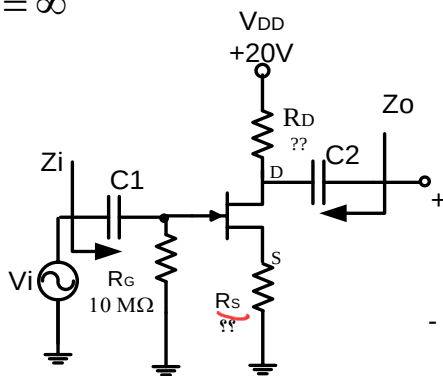
voltage gain $|A_v| = 8$ using the value of g_m defined at $V_{GSQ} = \frac{1}{4} V_p = -1 \text{ V}$

$$V_p = -4 \text{ V}$$

$$I_{DSS} = 10 \text{ mA}$$

$$r_{ds} = \infty$$

Note: This is the same previous example except that no C_s (source capacitor)



Solution

ac ss equivalent circuit

$$V_{GS} = -1 \text{ V}$$

$$I_D = 5.625 \text{ mA}$$

$$g_m = 3.75 \text{ mS} \text{ (from previous example)}$$

$$A_v = \frac{V_o}{V_i}$$

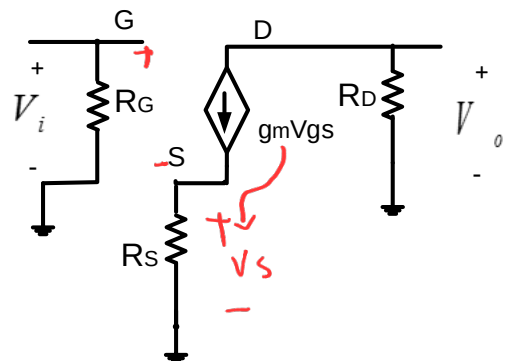
$$V_o = -g_m V_{gs} (r_{ds} || R_D) \leftarrow$$

$$V_{gs} = V_g - g_m V_{gs} R_S$$

$$V_g = V_i$$

$$V_{gs} = V_i - g_m V_{gs} R_S$$

$$V_i = V_{gs} + g_m V_{gs} R_S$$



$$A_v = \frac{V_o}{V_i} = \frac{-g_m V_{gs} (R_D)}{V_{gs} + g_m V_{gs} R_S} = \frac{-g_m R_D}{1 + g_m R_S}$$

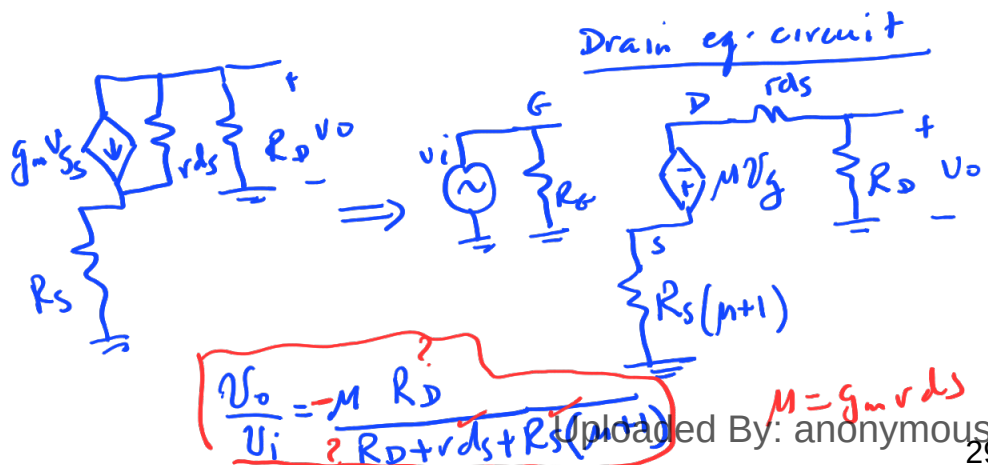
$$|A_v| = \left| \frac{V_o}{V_i} \right| = \left| \frac{-g_m R_D}{1 + g_m R_S} \right| = 8$$

Since A_v & g_m and R_S are known, then

$$R_S = 180 \, \Omega \text{ (based on DC analysis)}$$

$$\therefore R_D = 3.573 \text{ k}\Omega$$

if $r_{ds} \neq \infty$



Value of Rs?

The value of R_S is determined from DC analysis

Given

$$V_{GS} = V_G - V_S = \frac{1}{4} V_p = -1$$

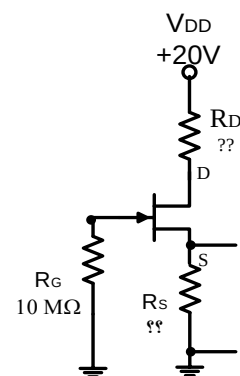
$$V_G = 0$$

$$V_S = I_D R_S = -1$$

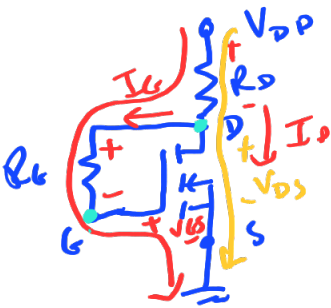
$$\text{but } I_D = I_{DSS} \left(1 - \frac{-1}{-4} \right)^2 = I_{DSS} \cdot 0.5625 = 5.625 \text{ mA}$$

$$\therefore R_S = \frac{V_S}{I_D} = \frac{1 \text{ V}}{5.625 \text{ mA}} = 177.8 \text{ } \Omega$$

choose standard value 180Ω



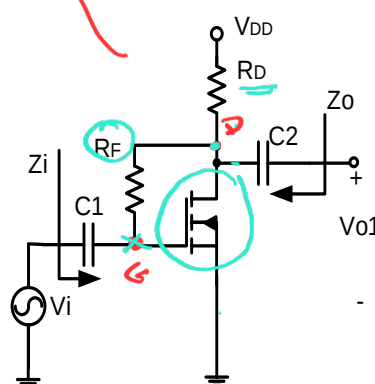
DC analysis



$V_{GS} = V_G - V_S = V_{DD} - I_D R_D$
 $V_S = 0$
 $V_G =$
 $V_{DD} - I_D R_D - I_G R_G - V_{GS} = 0$
 $V_{DD} - I_D R_D - V_{DS} = 0 \Rightarrow$
 $V_{DS} = V_{DD} - I_D R_D$

$V_{GS} = V_{DS}$
OR
 $V_G = V_D$

Drain Feedback Configuration (self study)

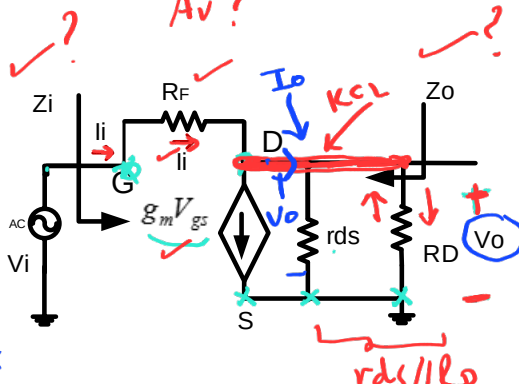


$A_v = \frac{V_o}{V_i}$

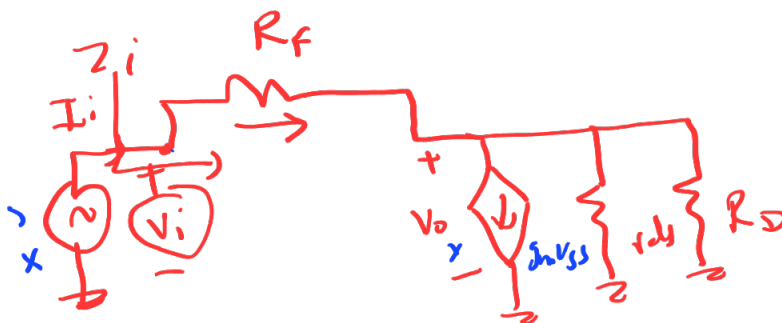
KCL

$I_i = g_m V_{gs} + \frac{V_o}{R_D // r_{ds}}$
 $V_{gs} = V_i$

$I_i = g_m V_i + \frac{V_o}{R_D // r_{ds}}$
 $I_i - g_m V_i = \frac{V_o}{R_D // r_{ds}}$



$r_{ds} // R_D$



$$V_o = (I_i - g_m V_i)(R_D // r_{ds}) \quad \checkmark \quad \dots (1)$$

also

$$I_i = \frac{V_i - V_o}{R_F} \quad \checkmark \quad \dots (2)$$

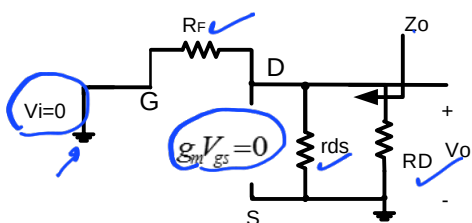
$$\checkmark I_i = \frac{V_i - ((I_i - g_m V_i)(R_D // r_{ds}))}{R_F}$$

$$\checkmark I_i R_F = \checkmark V_i - ((\checkmark I_i - \checkmark g_m \checkmark V_i)(\checkmark R_D // \checkmark r_{ds}))$$

$$\checkmark V_i [1 + g_m (R_D // r_{ds})] = \checkmark I_i [R_F + (R_D // r_{ds})]$$

$\therefore$

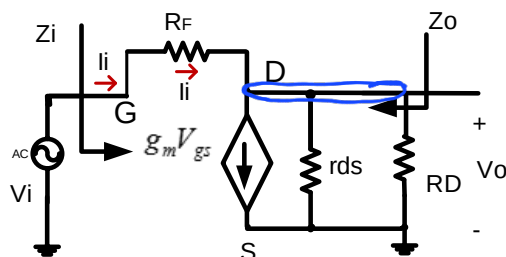
$$Z_i = \frac{V_i}{I_i} = \frac{[R_F + (R_D // r_{ds})]}{[1 + g_m (R_D // r_{ds})]}$$



$$Z_o|_{V_i=0} = R_D // r_{ds} // R_F$$

$$A_v = \frac{V_o}{V_i}$$

$$Z_i = \frac{V_i}{I_i}$$



$$I_i = g_m V_{gs} + \frac{V_o}{(R_D // r_{ds})}$$

$$V_{gs} = V_i \quad \text{also} \quad I_i = \frac{V_i - V_o}{R_F}$$

$$\frac{V_i - V_o}{R_F} = g_m V_{gs} + \frac{V_o}{(R_D // r_{ds})}$$

$$\frac{V_i}{R_F} - \frac{V_o}{R_F} = g_m V_i + \frac{V_o}{(R_D // r_{ds})}$$

$$\frac{V_i}{R_F} - g_m V_i = \frac{V_o}{(R_D // r_{ds})} + \frac{V_o}{R_F}$$

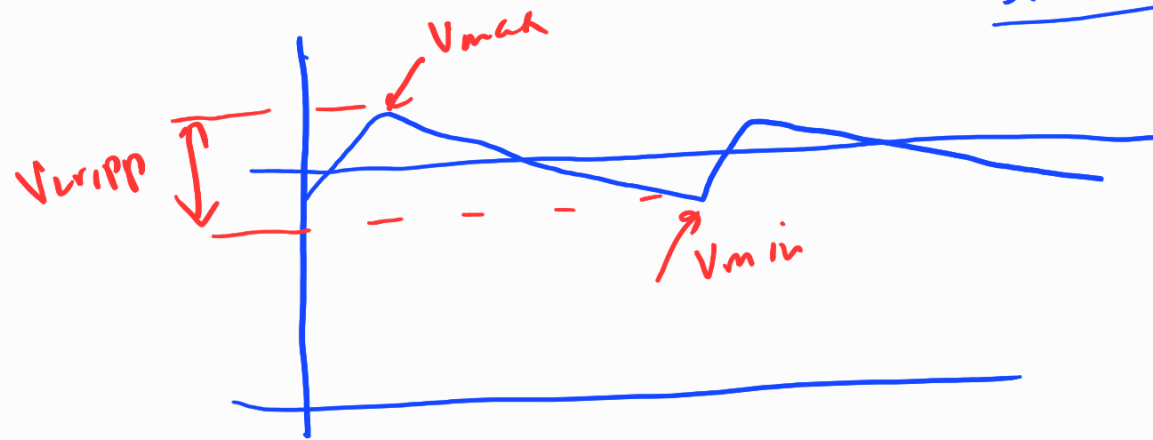
$$V_i \left(\frac{1}{R_F} - g_m \right) = V_o \left(\frac{1}{(R_D // r_{ds})} + \frac{1}{R_F} \right)$$

$$A_v = \frac{V_o}{V_i} = \frac{\left(\frac{1}{R_F} - g_m \right)}{\left(\frac{1}{(R_D // r_{ds})} + \frac{1}{R_F} \right)}$$

Best 3
of 4 quizzes
will be counted

End of T10
FET TOPIC
Monday 23/8
Quiz #4
T10

From Simulation



70 V - ω

80 V ? ω

$V_{avg} =$

$V_{Lripp} =$

$\checkmark$
 $5V \rightarrow 4V$

$$V_{rms} = \frac{V_{Lripp}}{2\sqrt{3}}$$

$r\% = 9$

$\checkmark$
 $10\% \rightarrow 7\%$

error $80 - 70 = 10$

$\% \text{ error } \frac{10}{70} \times 100\% \leq 2\%$

$\checkmark$
 $C?$
 N_1/N_2