

Def A sequence is an order list of numbers
 $a_1, a_2, a_3, a_4, \dots, a_n, \dots$

where

a_1 : 1st term

a_2 : 2nd term

a_3 : 3rd term

a_n : nth term

Exp Write the first four terms of the sequence

$$a_n = \frac{(-1)^n}{2^n}, \quad n = 1, 2, \dots$$

1st term is

$$a_{\boxed{1}} = \frac{(-1)^{\boxed{1}}}{2^{\boxed{1}}} = \frac{-1}{2}$$

نکته
nth term

2nd term is

$$a_{\boxed{2}} = \frac{(-1)^{\boxed{2}}}{2^{\boxed{2}}} = \frac{1}{4}$$

3rd term is

$$a_{\boxed{3}} = \frac{(-1)^{\boxed{3}}}{2^{\boxed{3}}} = \frac{-1}{8}$$

4th

$a_{\boxed{4}}$

4^{th} term is $a_4 = \frac{(-1)^4}{2 \cdot 4} = \frac{1}{8}$

Def A sequence is called **arithmetic** if the difference between any two successive terms is fixed d

$$a_n - a_{n-1} = d \rightarrow \text{Common difference}$$

for all $n = 2, 3, 4, \dots$

Exp which of the following sequences are arithmetic?!

① 1, 3, 5, 7, ...

$$\begin{aligned} 3 - 1 &= 2 \\ 5 - 3 &= 2 \\ 7 - 5 &= 2 \end{aligned} \rightarrow d = 2$$

Yes it's **arithmetic** with $d = 2$

② 10, 8, 4, 2, 1, ---

$$8 - 10 = -2$$
$$4 - 8 = -4$$

no it is not arithmetic

③ $\frac{1}{2}$, $\frac{5}{6}$, $\frac{7}{6}$, ---

$$\frac{5}{6} - \frac{1 \times 3}{2 \times 3} = \frac{5}{6} - \frac{3}{6} = \frac{5-3}{6} = \frac{2}{6}$$

$$\frac{7}{6} - \frac{5}{6} = \frac{7-5}{6} = \frac{2}{6}$$

Yes it is arithmetic

with $d = \frac{2}{6} = \frac{1}{3}$

Def The n^{th} term of any arithmetic sequence is

$$a_n = a_1 + (n-1)d$$

st
1 term

Common
difference
 d

Exp Find the 11th term in the following arithmetic sequences

① $1, 3, 5, 7, \dots$
 a_1

جد 11th حد
 $1, 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, \dots$
 a_1 1 2 3 4 5 6 7 8 9 10 11 n

Find 11th

جد 11th حد

$$a_n = a_1 + (n-1)d$$

$$a_{11} = a_1 + (11-1)d$$

$$= 1 + 10 \cdot 2$$

$$= 1 + 20$$

$$= 21$$

$$d = 3 - 1$$

$$= 2$$

$$n = 11$$

$$a_1 = 1$$

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$$a_{11} = \frac{1 + 10 \cdot 2}{2}$$

$$= \frac{1 + 20}{2}$$

$$= \frac{21}{2}$$

$$= 10.5$$

② $\frac{1}{2}, \frac{5}{6}, \frac{7}{6}, \dots$
 a_1

$$d = \frac{7}{6} - \frac{5}{6} = \frac{2}{6} = \frac{1}{3}, \quad n = 11$$

$$a_n = a_1 + (n-1)d$$

$$a_n = a_1 + (n-1)d$$

$$a_{11} = a_1 + (11-1)d$$

$$= \frac{1}{2} + 10 \cdot \frac{1}{3}$$

$$= \frac{1 \times 3}{2 \times 3} + \frac{10 \times 2}{3 \times 2}$$

$$= \frac{3}{6} + \frac{20}{6}$$

$$= \frac{23}{6}$$

Exp = If the first term of an arithmetic sequence is 4 and the 9th term is 20.

Find the 75th term.

$$a_1 = 4$$

$$a_9 = 20$$

$$a_n = a_1 + (n-1)d$$

$$a_9 = a_1 + (9-1)d$$

$$20 = 4 + 8d$$

Find a_{75}

$$a_n = a_1 + (n-1)d$$

$$a_{75} = a_1 + (75-1)d$$

$$= 4 + 74(d)$$

$$= 4 + 74.2$$

$$\begin{array}{l}
 20 - 4 = 16 \\
 \frac{16}{8} = \frac{8d}{8} \\
 \boxed{2 = d}
 \end{array}
 \quad
 \begin{array}{l}
 = 4 + 74.2 \\
 = 4 + 148 \\
 = 152
 \end{array}$$

Def The Sum of the first n terms of an arithmetic sequence is

$$S_n = \frac{n}{2} [a_1 + a_n]$$

$\uparrow$ 1st term $\uparrow$ n^{th} term

$$n^{\text{th}} \text{ term} \Rightarrow \boxed{a_n = a_1 + (n-1)d}$$

Exp Find the sum of the first 10 terms of the arithmetic sequence whose first term is 2 and its common difference 4

Find S_{10}

$$S_n = \frac{n}{2} [a_1 + a_n]$$

$$n = 10$$

$$a_1 = 2$$

$$d = 4$$

$$\boxed{a_n = a_1 + (n-1)d}$$

$$S_n = \frac{n}{2} [a_1 + a_n]$$

$$S_{10} = \frac{10}{2} [a_1 + a_{10}]$$

$$= 5 [2 + 38]$$

$$= 5 \cdot 40$$

$$= 200$$

$$a_n = a_1 + (n-1)d$$

$$a_{10} = 2 + (10-1)4$$

$$= 2 + 9 \cdot 4$$

$$= 2 + 36$$

$$= 38$$

$$a_1 = 2, \quad d = 4$$

$$2, \boxed{6}, \boxed{10}, \boxed{14}, \boxed{18}, \boxed{22}, \boxed{26}, \boxed{30}, \boxed{34}, \boxed{38}, \dots$$

1 2 3 4 5 6 7 8 9 10

$18 - 14 = 4$ $30 - 26 = 4$

$$2 + 6 + 10 + 14 + 18 + 22 + 26 + 30 + 34 + 38 = 200$$

Exp Find the sum of the first 51 terms for the arithmetic sequence:

$$-10, -6, -2, \dots$$

Find S_{51}

$$S_n = \frac{n}{2} [a_1 + a_n]$$

$$a_1 = -10$$

$$d = -2 - (-6)$$

Find S_{51}
 $n = 51$

$$S_n = \frac{n}{2} [a_1 + a_n]$$

$$S_{51} = \frac{51}{2} [-10 + a_{51}]$$

$$= \frac{51}{2} [-10 + 190]$$

$$d = -2 - -6$$

$$= -2 + 6$$

$$= 4$$

$$d = -6 - -10$$

$$= -6 + 10$$

$$= 4$$

$$a_n = a_1 + (n-1)d$$

$$a_{51} = a_1 + (51-1)d$$

$$= -10 + 50 \cdot 4$$

$$= -10 + 200$$

$$a_{51} = 190$$

$$= \frac{51}{2} [180]$$

$$= 4590$$