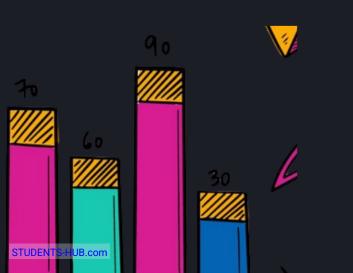
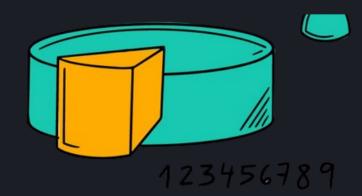




STATESTES

By Rawan Alfares





شعاره الصبر ، وراحته التعب)

common discrete random variables

- I. Binomial Distribution :-
 - · A Random experiment Consisting of (n) repeated trials, Such that :-

الاحتمالان فقط

- b= Each trial results in only two possible oul Comes, a Success or Sail + Success المعانية
- C. the Probability of Success (P) on each trial remains Constant bland bail of

* the probability mass function s-
$$p(X=X) = \begin{cases} \binom{n}{x} p^{X} (1-p)^{n-X}, & X=0,1,2,...n \end{cases}$$

 $egin{array}{c} \dot{\omega}$ نفهم القانون

$$b(\lambda = x) = {x \choose u} b_x (1-b)_{u-x}$$

n: number of trials

X: number which Successful will occurs.

px: probability of success.

(1-p) : Probability of fail

Mean value
$$\Rightarrow$$
 $M_X = E(X) = np$

Nob. of Success.

* Variance = $\sigma_X = Var(X) = np(1-p)$ prob. of Success

Example 8- Consider the exp. of flipping a Coin 3 times. Assume $p(H) = \frac{1}{4}$, and $p(T) = \frac{3}{4}$ a determine the prob. of getting a head for 2 times.

- b. what the prob. of getting at least one head.
- a what the expected number of heads to be observed in the exp.

1st, we want to ensure that this example will be solved in Bionomial.

- 1. only two out comes.
- 2. Prob. of Success is lixed.
- 3. the prob. of Success doesn't Alfect on the prob of fail. So, yes its Binomial.

$$p(\chi = \lambda) = \begin{pmatrix} 3 \\ \chi \end{pmatrix} \begin{pmatrix} \frac{1}{4} \end{pmatrix}^{\chi} \begin{pmatrix} \frac{3}{4} \end{pmatrix}^{\chi}, \quad n = 0, 1, 2, 3 \end{pmatrix}$$

$$p(\chi = \lambda) = \begin{pmatrix} 3 \\ 2 \end{pmatrix} \begin{pmatrix} \frac{1}{4} \end{pmatrix}^{2} \begin{pmatrix} \frac{3}{4} \end{pmatrix}^{\chi}, \quad n = 0, 1, 2, 3 \end{pmatrix}$$

$$= \frac{3!}{2!(3-2)!} \cdot \frac{1}{16} \cdot \frac{3}{4} = \frac{9}{64}$$

$$\rho(\chi=2) = \begin{cases} \frac{q}{64}, & n = 0,1,2,3 \end{cases}$$

* notes-

you determine the Success according to the question, for example in this question, it requires to find prob. When head Occurs so, we assume that occuring head is the success.

b.
$$P(x_{7}) = p(x_{1}) + p(x_{2}) + p(x_{3})$$
 white consuming or instead, $p(x_{7}) = 1 - p(x_{2})$

$$p(x_{1}) = {3 \choose 4} {1 \choose 4} = \frac{27}{64}$$

c. expected number means
$$\mu_x$$
 - mean or avarage.

$$\mu_{X} = n\rho = 3. \frac{1}{4} = \frac{3}{4}$$

$$g^{2} = n\rho(1-\rho) = 3. \frac{1}{4} \cdot \frac{3}{4} = \frac{9}{16}$$

Example 2 & Consider the exp. of tocing a die, for 3 times

$$p(S) = \frac{1}{6}$$
, $p(F) = \frac{5}{6}$

$$p(X=1) = {3 \choose 1} {6 \choose 5} {6 \choose 5} = {35 \over 36}$$

$$n=3$$
, $\chi=a$

$$p(S) = \frac{2}{6} = \frac{1}{3}$$
, $p(F) = \frac{4}{6} = \frac{2}{3}$

$$P(X=2) = {3 \choose 2} {1 \choose 3}^2 {2 \choose 3}^1$$

$$= {31 \choose 2!(3-2)!} \cdot {1 \over 9} \cdot {3 \over 3} = {2 \over 9}$$



* notes

note that it has 6 out comes, which con't be Binomial until we change the exp into 2 out comes. and that will be determined according to the question as you see above

II. The Geometric Distribution

- · it's a random exp. Consists of infinity trials Such that s
- a. the trials are indep. > ناموس على المعالي بأ يوس على المعالم المعا

الاحتمالات فقط

- b- Each trial results in only two possible out Comes, a Success or Sail + Success إلما عنه إما
- C. the Probability of Success (P) on each trial remains Constant مناع مناع عليه المناع المنا

﴿ بِاللَّهُ عَلَى الْمُرْدِ الْمَجْرِبِ حَقَ تَحْدَثُ أُولَ هِمْ نَجْلِح ، والـ عَلَمْ بِيحَلَيْنَا الْمُحَادِلَةُ وَقَى الْمُحَادِلَةُ وَلَى الْمُحَادِلَةُ وَلَى الْمُحَادِلَةُ وَقَى الْمُحَادِلِةُ وَلَى الْمُحَادِلَةُ وَقَى الْمُحَادِلَةُ وَلَى الْمُحَادِلَةُ وَقَى الْمُحَادِلِةُ وَلَى الْمُحَادِلِةُ وَلَى الْمُحَادِلِةُ وَلَى الْمُحَادِلِةُ وَلَى اللَّهُ وَلَى اللَّهُ وَلَا اللّهُ وَلَى اللَّهُ وَلَى اللَّهُ وَلَى اللَّهُ وَلَى اللَّهُ وَلَا اللَّهُ وَلَا اللَّهُ وَلَا اللَّهُ وَلَا اللَّهُ وَلَا اللَّهُ وَلَى اللَّهُ وَلَا اللَّهُ اللَّهُ وَلَا اللَّهُ وَلَا اللَّهُ وَلَى اللَّهُ وَلَا لَا اللَّهُ وَلَا اللَّهُ وَلَا لَا اللَّهُ وَلَ

* the probability mass functions 8-

$$p(X=x) = (1-p) p$$
, $X = 1,2,3...$

- * mean value = $\mu_X = E(x) = \frac{1}{D}$
- * Variance = $g_x^2 = \text{Var}(x) = \frac{1-\rho^2}{\rho^2}$

EXAMPLE (3-17):

Let the probability of occurrence of a flood of magnitude greater than a critical magnitude in a given year be 0.02. Assuming that floods occur independently, determine the "return period" defined as the average number of years between floods.

 $\mu_{x} = 1 = 1 = 50$ مش معناها یونکل ۵۰ مست به به بیرطوفان $\rho = 0.00$ مش معناها یونکل ۵۰ مست و پانه کل ۵۰

مملت بصبي طعفان.

sarb en dillo

III Hyper geometric distribution.

Type I Type II

(n) aue

(n)

The probability mass function is
$$p(X=X) = \frac{\binom{R}{X}\binom{N-R}{n-X}}{\binom{N}{N}}$$

R: number of item from type I in N

X: number of items from type I was selected in n

«الحد الله " ما Comes من الحد الله " «الحد الله عن العد الله الله عن العد الله عن الله ع

n: number of selected items. "عبدالعينة"

$$x = mean Value = \frac{nR}{N} = nP$$

$$\star g_{x}^{2} = np(1-p) \left[\frac{N-n}{N-1} \right]$$

Example 8-

X = 2

a what the prob. of having 2 red balls in 3 selected balls. $P(X=X) = \underbrace{\left(\frac{5}{2}\right)\left(\frac{7}{3}-X\right)}_{\left(\frac{12}{3}\right)} = \underbrace{\left(\frac{5}{2}\right)\left(\frac{7}{1}\right)}_{\left(\frac{12}{3}\right)}, \quad X=0,1,2,..., \min(3,5)$

b. what the prob. of selecting at least one red ball.

P(xy) = P(x=1) + P(x=2) + P(x=3)

or
$$p(x_{7/1}) = 1 - p(x_{=0})$$

= $1 - \left[\frac{\binom{5}{3}\binom{7}{3}}{\binom{12}{3}}\right] = \left[\frac{\binom{12}{3}}{\binom{12}{3}}\right]$

c at least two messages will arrive in 1 hr

$$b = \lambda T = 10 \times 1 = 10$$

$$\rho(\chi > 2) = 1 - \rho(\chi < 2)$$

$$= 1 - \left[e \times \frac{10}{0!} + e \times \frac{10}{1!} \right]$$

شقوق

EXAMPLE (3-22):

The number of cracks in a section of a highway that are significant enough to require repair is assumed to follow a Poisson distribution with a mean of two cracks per mile.

- a- What is the probability that there are no cracks in 5 miles of highway?
- b- What is the probability that at least one crack requires repair in ½ miles of highway?
- c- What is the probability that at least one crack in 5 miles of highway?

a)
$$T = 5$$
 mile, $b = AT = 2 \times 5 = 10$ cracks
$$\rho(X_{=0}) = e^{-10} \times \frac{(10)^{2}}{01} = e^{-10}$$

$$b(x \gg i) = 1 - b(x < i)$$

$$b(x \ge 1) = 1 - b(x < 1)$$

$$= 1 - b(x < 1)$$

$$= 1 - b(x < 1)$$

$$= 1 - b(x < 1)$$

Common Continuous Random Variables: I. uniform distribution 8-

$$f_{X}(x) = \begin{cases} \frac{1}{b-a}, & a \leqslant x \leqslant b \end{cases}, \qquad f_{X} = \frac{a+b}{2}, \qquad f_{X}^{2} = \frac{(b-a)^{2}}{12}$$

examples let X be Random voicable that follows uniform distribution, in the interval [-2, 5],

* pdf =
$$\begin{cases} \frac{1}{5-2} = \frac{1}{7}, -2 < X < 5 \end{cases}$$

b. what the prob. that x is less than Zero.
$$P(X \le 0) = \int_{-\frac{\pi}{4}}^{\infty} \frac{1}{4} dx = \frac{1}{4}(2) = \frac{2}{4}$$

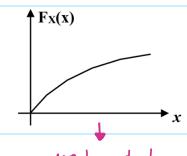
C. find
$$\mu_x$$
 and σ_x^2

$$\mu_x = \frac{b_1a}{2} = \frac{5-2}{2} = \frac{3}{2}$$

$$\theta_{\chi}^{2} = \underline{(b-q)}^{2} = \underline{(5-2)}^{2} = \underline{49}$$

 $f_X(x)$

20-12-2023 II. exponential Distribution 8-
$$f_X(x) = \int e^{-ix}, \quad x = \frac{1}{4}$$
bounded in the appearance of the property of t



Important

1 in poisson distribution means avorage occurrence per unit However in exp. dist. it's a constant. (doesn't equal avarage).

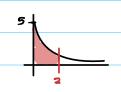
example so let x be an exponential random variable with amean at 0.2

a) write and plot the pdf at X.

$$f_{X}(x) = \begin{cases} 5e & x > 0.0 \end{cases}$$

$$A = \frac{1}{\mu_{x}} = \frac{1}{0.2} = 5$$

$$\int_{0}^{2} 5 e^{-5x} dx = -e^{x} \Big|_{0}^{2} = 1 - e^{x}$$



$$=\frac{1}{A^2}=\frac{1}{(5)^2}=0.04$$

EXAMPLE (3-24):

w Suppose that the depth of water, measured in meters, behind a dam is described by an

exponential random variable with pdf:
$$f_X(x) = \begin{cases} \frac{1}{13.5} & \frac{-x}{0} \\ 0 & \text{o. w} \end{cases}$$
 random variable.



There is an emergency overflow at the top of the dam that prevents the depth from exceeding 40.6 m. There is a pipe placed 32.0 m below the overflow that feeds water to a hydroelectric generator (turbine).

a- What is the probability that water is wasted though emergency overflow?b What is the probability that water will be too low to produce power?

c- Given that water is not wasted in overflow, what is the probability that the generator will have water to derive it?

will have water to derive it?

a)
$$P(X7, 40.6) = \int_{40.6}^{40.6} f_X(x) dx = -e^{\frac{-X}{13.5}} \Big|_{40.6}^{\infty}$$

p)
$$b(x \le 8.9) = \int_{8.9}^{9} f^{x}(x) dx = -\frac{6}{-x} \Big|_{8.9}^{9} = 1 - \frac{6}{-x}$$

c)
$$\rho(X > 8.6 / X < 40.6) = \frac{\rho(X > 8.6) \times 40.6}{\rho(X < 40.6)} = \frac{8.6}{\sqrt[40.6]{\frac{1}{13.5}}} e^{\frac{1}{13.5}} dx$$

, يعني المياه مش راع

تطلع عن العاسورة.

important

IV. Rayleigh Distribution 8-

$$f_{x}(x) = \frac{2}{b} x e^{\frac{-x^{2}}{b}}$$
 ; x7, 0

$$f_{x}(x) = \frac{2}{h} x e^{\frac{-x^{2}}{b}}$$
; x7,0, $F_{x}(x) = 1 - e^{\frac{-x^{2}}{b}}$, x7,0

$$\mu_{x} = E(x) = \sqrt{\frac{\pi b}{y}}$$

$$\mu_{x} = E(x) = \sqrt{\frac{\pi b}{4}}$$
, $\theta_{x}' = loc(x) = \frac{b(4-\pi)}{4}$

not _ important

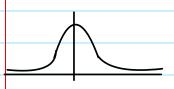
V. Cauchy Random Voriable

$$f_{\chi}(\hat{x}) = \frac{\alpha}{T}$$

$$F_{\chi}(\chi) = \frac{1}{2} + \frac{1}{11} \tan^{-1}\left(\frac{\chi}{Q}\right)$$

recorded lecture 23-12-2023

Gaussian (Normal) Distribution

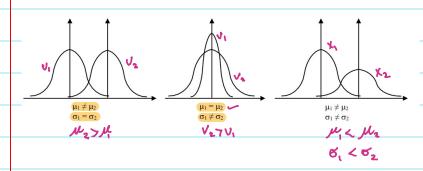


$$f_{x}(x) = \frac{1}{\sqrt{2\pi\sigma_{x}^{2}}} e^{\frac{-(x-\mu_{x})^{2}}{2\sigma_{x}^{2}}}, -\infty < x < \infty$$

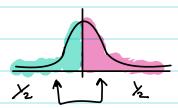
$$E(X) = \mu_X$$
, $Varz = \theta_X^2 \rightarrow Javiliarian Times$

نقطة الارتلاز حا

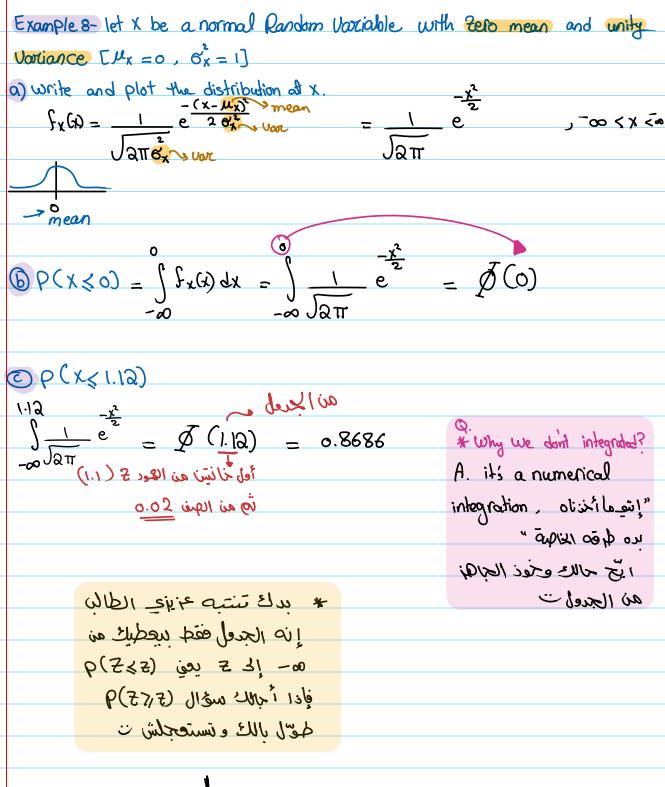
mean 11



🗶 gausian dist. is Symmetric



ع م نین متساوین کلم: احتمالیت معن valid polf حال علا عتمالمتما يغيف



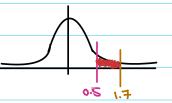
only for Standard normal Distribution

Important Note 8-
$$\emptyset(-a) = 1 - \emptyset(a)$$

$$= 1 - \emptyset(3.19)$$
= 1-6(X\leq 3.19)

$$= 1 - 0.9991 = 9 \times 10^{-4}$$

 $(7.1 \geqslant \chi \geqslant 7.0) \neq (9.0)$ $= \emptyset(1.1) - \emptyset(0.0)$



Examples-let X be normal random variable with
$$x=1$$
, $\theta_x^2=9$

a) write and plot the pdf of
$$x$$
.
$$f_{X}(x) = \frac{1}{\sqrt{2\pi\theta_{X}^{2}}} e^{\frac{-(x-1)^{2}}{2\theta_{X}^{2}}} = \frac{1}{3\sqrt{3\pi}} e^{\frac{-(x-1)^{2}}{2(2)(9)}}$$

$$= 1 - \underline{A}(\underline{y})$$

$$= 1 - \underline{A}(\underline{y})$$

$$\underline{P} b (x < -g) = \underline{Q} (-g - 1) = \underline{Q}(-1)$$

* السؤال هذا عابينفع نجب الجوان ai الحبول في أن المعلم ton

standard 3/ or p is stalle

$$\emptyset \left(\frac{x - \mu_x}{x} \right) \quad \text{(a)}$$

Normal Approximation of the Binomial and Poisson Distribution:

EXAMPLE (3-28):

Consider a binomial experiment with n = 1000 and p = 0.2. if X is the number of successes, find the probability that $X \le 240$.

 $b(X \leq 340) = \sum_{540} {\binom{x}{0.9}} {\binom{0.9}{0.9}} {\binom{0.9}{0.9}} {\binom{0.9}{0.9}} {\binom{0.9}{0.9}} {\binom{0.9}{0.9}}$

Ly we can't do this, so we will approximate it using normal dist.

 $\mu_{x} = np = (1000)(0.2) = 200$ $\theta_{k}' = \eta \rho(1-\rho) = (1000)(0.2)(0.8) = 160$

EXAMPLE (3-29):

Assume the number of asbestos particles in a cm³ of dust follow a Poisson distribution with a mean of 1000. If a cm³ of dust is analyzed, what is the probability that less than 950 particles are found in 1 cm³?

 $P(X=X) = e \frac{b}{x!}, \quad \chi = e^{2} = b = 1000 \text{ abs. } x \text{ cm}^{3} = 1600$ $P(X=X) = e \frac{(1000)}{x!}$ X!

 $P(X \leqslant 950) = \underset{450}{\overset{x=0}{\leq}} e \frac{(1000)}{\chi}$

$$\oint \left(\frac{950 - 1000}{1000}\right) = \oint (-1.581)$$
= $1 - \oint (1.581)$

Transformation of Random Variables:

I. Discreat

EXAMPLE (3-30):

Let (X) be a binomial r.v with parameters (n = 3) and (p = 0.75). Let Y = g(x) = 2X + 3 P(Y = y) = P(X = x)

$$P(X=X) = \begin{cases} \binom{x}{3} (0.75) & (0.05) \\ 0 & 0.05 \end{cases}, \quad X=0,1,2,3$$

X	$P(\chi=\chi)$	y= 2 x +3	P(Y=y)
0	$ \frac{3}{3}(0.75)(0.25) = \frac{1}{64} $ $ \frac{3}{3}(0.75)(0.25) = \frac{9}{64} $ $ \frac{3}{3}(0.75)(0.25) = \frac{27}{64} $ $ \frac{3}{3}(0.75)(0.25) = \frac{27}{64} $ $ \frac{3}{3}(0.75)(0.25) = \frac{27}{64} $	M	- 64
1	$(3)(0.75)(0.25) = \frac{9}{4}$	5	<u>१</u> 6५
2	(3) (0.75) (0.25)=27	7	<u>27</u> 69
3	$\binom{3}{3}$ (6.25) = 27	9	2 7 64
	64		67

EXAMPLE (3-31):

Let (X) has the distribution $P\{X = x\} = \frac{1}{6}$; x = -3, -2, -1, 0, 1, 2Define $Y = g(x) = X^2$. Find the pdf of the random variable Y.

Y = X					
X	P(X = x)	Y = 1/2	P(y=5)		
-3	1/8	9	1/6		
-2	<i>Y</i> ₆	4	<i>Y</i> 6		
-1	<i>Y</i> ₆		<i>Y</i> ₆		
O	<i>Y</i> ₆	0	76		
l	%		<i>Y</i> 6		
2	Y ₆	Ч	16		

 $E[Y] = E[x^{2}] - \mu_{x}^{2}$ $P(Y=y) = \begin{cases} 6 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 & y=9 \end{cases}$ $\begin{cases} 8+1 & y=9 \\ 8+1 &$

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$$f_{y}(y) = \frac{f_{x}(x)}{\left|\frac{dy}{dx}\right|}$$

Let (X) be a Gaussian r.v with mean (0) variance (1). Let $Y = X^2$. Find $f_Y(y)$

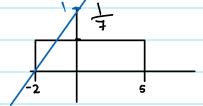
SOLUTION:

$$\int_{2\pi}^{-x} f_{x}(x) = \frac{1}{\sqrt{2\pi}} e^{\frac{-x^{2}}{2}}$$

$$Y) \quad f_y(y) = 2 \qquad f_x(x)$$

gaussian

example: let x be a Random variable that follow a uniform Distribution over the interval [-2,5], y= ax+1, Find pdf of y?



$$fy(y) = \frac{fx(x)}{\left|\frac{dy}{dx}\right|} = \frac{\frac{1}{2}}{2} = \frac{1}{14}$$

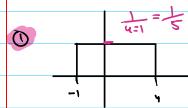
$$x = \frac{3}{3-1}$$

$$\left|\frac{\partial x}{\partial \beta}\right| = g$$

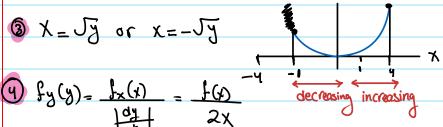
$$\begin{cases}
9 & \text{fy}(y) = \begin{cases}
\frac{1}{14}, & -3 \leq x \leq 11
\end{cases}
\end{cases}$$

EXAMPLE (3-33):

Let (X) be a uniform r.v in the interval (-1, 4). If $Y = X^2$. Find $f_Y(y)$



$$f_{x}(x) = \int_{0}^{\infty} f_{x}(x) = \int_{0}^{\infty} f_{x}(x$$



$$\frac{9}{9} f_y(y) = \frac{f_x(x)}{10y} = \frac{f(y)}{2x}$$

Case 18
$$\times -4$$
 and $\times -4$ $\Rightarrow f_{y}(y) = 0$

Case 28 $-1 < \times <0 \Rightarrow 0 < y < 1 \Rightarrow f_{y}(y) = \frac{1}{|2x|} + \frac{1}{|2x|} = \frac{2}{|0xy|} = \frac{1}{|5xy|}$

Case 2 \(\text{As } \) $= \frac{1}{|2x|} = \frac{1}{|2x|}$

* Case 3:
$$1 < x < y \rightarrow 1 < y < 16 \rightarrow fy(y) = \frac{1}{|x|} = \frac{1}{|x|}$$

$$\begin{cases}
\frac{1}{5\sqrt{8}}, & 0 \leqslant 4 \leqslant 1 \\
\frac{1}{10\sqrt{9}}, & 1 \leqslant 4 \leqslant 1
\end{cases}$$

Notes

Y is Gaussian with mean ($\mu_Y = a \mu_X + b$) and variance ($\sigma_Y^2 = a^2 \sigma_X^2$)

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