

Ch 3.1:-

$$\{\forall x \in D \mid P(x)\}$$

The set of x in D such that $P(x)$

- Q₁
- | | |
|----------------|-----------|
| 7 brown dogs | (a) False |
| 2 black dogs | (b) True |
| 6 gray cats | (c) False |
| 10 black cats | (d) True |
| 5 blue birds | (e) false |
| 6 yellow birds | (f) True |
| 1 black bird | |

- Q₂
- (a) True, Real numbers include Rational and irrational numbers, and integers
they are Real numbers are considered to be part of rational numbers then
- (b) False, 0 is neither positive nor negative
- (c) counter example $\Rightarrow r = -2 \Rightarrow -r = +2$ nonnegative numbers
- (d) False, counter example $\Rightarrow r = 2.2 \Rightarrow$ not an integer

- Q₃
- $P(x) \Rightarrow x > \frac{1}{2}$
- $P(2) \Rightarrow 2 > \frac{1}{2}$ true (b) $\Rightarrow x > 1$ or $-1 < x < 0$
- $P(\frac{1}{2}) \Rightarrow \frac{1}{2} > \frac{1}{2}$ false
- $P(-1) \Rightarrow -1 > -1$ false (c) $\Rightarrow x > 1$
- $P(-\frac{1}{2}) \Rightarrow -\frac{1}{2} > -2$ true
- $P(-8) \Rightarrow -8 > -\frac{1}{8}$ false

- Q₄
- $n^2 \leq 30$
- $Q(2) \quad Q(-2)$ true
- $Q(7) \quad Q(-7)$ false

(b) $\{-5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5\}$

(c) $\{1, 2, 3, 4, 5\}$

- Q₅
- $x < y \rightarrow x^2 < y^2$
- (a) $-2 < 1$ true but $4 < 1$ false
true \rightarrow false \therefore false
- (c) $x < y \Rightarrow 3 < 8$ true
 $x^2 < y^2 \Rightarrow 9 < 64$ true
true \rightarrow true \therefore true
- (b) $x = -4, y = 2$
conclusion is false then the conditional statement is false too
- $x = 8$
 $y = 9$

Q₆ if m is a factor of n^2 then m is a factor of n

25 is a factor of 100

Premise is true

but 25 isn't a factor of 10

$(10 \nmid 25) \Rightarrow$ false conclusion

Then the conditional statement is false.

$b + c + d$ skip

Q₇ (a) $\{1, 2, 3, 4, -1, -2, -3, -6\}$

(b) $\{1, 2, 3, 6\}$

(c) $1 \leq x^2 \leq 4 \quad \mathbb{R} \Rightarrow [-2, 0] \cup [1, 2]$

(d) $\{-1, -2, 1, 2\}$

Q₈ $-10 < x < 10$

(a) $\{-9, -8, -7, -6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$

(b) $\mathbb{Z}^+ \Rightarrow \{1, 2, 3, 4, 5, 6, 7, 8, 9\}$

(c) $\Rightarrow \{2, 4, 6, 8, 0, -2, -4, -6, -8\}$

Q₉ (a) $x = \frac{1}{2}$

Q₁₀ $a = -1$

Q₁₁ $m=1, n=2$

Q₁₂ $x=1, y=1 \quad \sqrt{2} \neq 2$

Q₁₃ (a) / (c) / (f)

Q₁₄ (b) / (f) / (c) / (e)

Q₁₅ (a) All rectangles are quadrilateral

(b) There is at least one set that has 16 subsets

$$Q_{16}(a) \forall x, \text{dinosaur}(x) \rightarrow \text{extinct}(x)$$

$$(b) \forall x \in \mathbb{R}, \text{positive}(x) \vee \text{negative}(x) \vee \text{zero}(x)$$

$$(c) \forall x, \text{irrational}(x) \rightarrow \sim \text{int}(x)$$

$$(d) \forall p \in \text{person}, \text{logicians}(x) \rightarrow \sim \text{lazy}(x)$$

$$(e) \forall x \in \text{integers}, x^2 \neq 2147581953$$

$$(f) \forall x \in \mathbb{R}, x^2 \neq -1$$

$$Q_{17} (a) \exists e \in \text{exercises such that have answers}(e)$$

$$\text{or } \exists e (\text{exercises}(e) \wedge \text{have ans}(e))$$

$$(b) \exists x \in \mathbb{R} \text{ such that rational}(x)$$

$$Q_{18} M(s) \rightarrow \text{Math major student}$$

$$C(s) \rightarrow \text{Computer science student}$$

$$E(s) \rightarrow \text{Engineering students}$$

$$(a) \exists s \in \text{student such that } (E(s) \wedge M(s))$$

$$(b) \forall s \in \text{student}, C(s) \rightarrow E(s)$$

$$(c) \forall s \in \text{student}, C(s) \rightarrow \sim E(s)$$

$$(d) \exists s \in \text{student such that } (C(s) \wedge M(s))$$

$$(e) \exists s \in \text{student such that } (C(s) \wedge E(s)) \wedge \exists s \in \text{student } (C(s) \wedge \sim E(s))$$

Q19 (b)/(d)/(e)

(a) \rightarrow isn't correct

\rightarrow لا يوجد حكمة انزل

ان $(int)^2$ \leftarrow even وعل

ان int \leftarrow even

Q20 the square root of any positive real number is also positive

Q21 The total degree of G is even, for any ---

The base angles of T ---- \rightarrow for any isosceles---

p is even for some prime numbers p

f isn't diff for some cont functions f

Q22 (a) $\forall x$, Java(x) \rightarrow have at least 5(x)

(b) $\forall x$ (valid argument(x) \wedge true premises(x)) \rightarrow true conclusion(x)

Q23 (a) $\forall x$, equilateral triangles(x) \rightarrow isosceles(x)

(b) $\forall x \in$ computer science student, Take data structure(x)

Q24 (a) $\exists x \in$ letters, mad(x)

(b) $\exists x \in$ questions, easy(x)

Q25 (a) $\forall x \in$ Nonzero fraction, Fraction Reciprocal(x) \rightarrow $\exists y \in$ fraction such that $xy = 1$
صاد نالي

(b) $\forall x \in$ poly nomial, Derivative(x) \rightarrow Poly Derivative(x)

(c) $\forall x, y \in$ Angles, (Triangle Angle(x) \wedge Triangle angle(y)) \rightarrow Sum Is 180(x, y)

(d) $\forall x \in$ irrational, irrational negative form(x)

(e) $\forall x, y \in$ integers, (even(x) \wedge even(y)) \rightarrow even($x+y$)

(f) $\forall x, y \in$ fraction, Fraction($x \cdot y$)

Q26 $\forall x, (\text{int}(x) \rightarrow \text{rational}(x)) \wedge \exists x \in \text{rational such that } \neg \text{int}(x)$

Q27

				
				
				
				
				

↓ black ↓ grey

(a) false, there is a black circle

(b) true

(c) false

(d) true

Q28

$\text{Real}(x) \rightarrow$ real num

$\text{Pos}(x) \rightarrow$ positive Real num

$\text{Neg}(x) \rightarrow$ negative Real num

$\text{Int}(x) \rightarrow$ int

(a) zero is a positive Real number
(false \rightarrow it's neither negative nor positive)

(b) the negative of any negative Real number is a positive Real number
(true)

(c) any integer is a real number (true) $\Rightarrow x = 1$ int & real

(d) There is at least one Real num that's not an int (true)
1.2 real but not an int \leftrightarrow

Q29

(a) true

(b) true

(c) true

there's a rectangle that is also a square

there is a rectangle that isn't a square

all squares are rectangles too

Q₃₀ (a) true $\Rightarrow x = 2$

(b) true $x = 2, 3, 5, 7, \dots$

(c) $x = 25$ true

Q₃₁ skip

Q₃₂ (a) $x > 2 \Rightarrow x > 1$

true

(b) $x > 2 \Rightarrow x^2 > 4$

true

(c) $x^2 > 4 \Rightarrow x > 2$

false

$x = -3 \Rightarrow x^2 > 4$ but $(-3 > 2) \times$
 $9 > 4$

(d) $x^2 > 4 \Leftrightarrow |x| > 2$

true

Q₃₃

(a) true

(b) false $\Rightarrow -1 = a < 0$

$-2 = b < 0$

$ab = 2 > 0$

(c) true

(d) $-10 < 1$ $-10 < 1$ false

Ch 3.2

Q₁ (a)/(e)

Q₂ (c)/(f) /

Q₃ a) \exists fish x ... such that x hasn't gills

b) \exists com... such that c hasn't

c) if movie \supset m isn't over

d) if a and $b \supset b$ hasn't won 10 Gram

Q₄

a) Some dogs aren't - -

b) Some people aren't - - -

c) All sun weren't - - -

d) All es - aren't ac - - -

Q₅ a) Some v - haven't a true con - -

b) Some v - aren't positive, aren't negative and aren't zero

Q₆ a) Sets A and B have some points

b) Towns P - are connected by some - - -

Q₇ No orders from store A for item B

\Rightarrow universal

There is at least one order from stor - - -

$\forall o \in \text{orders}, \neg \text{order}(A, B)$

negation $\exists o \in \text{order}, \text{order}(A, B)$

Q₈ there is at least one simple solution

$\exists S$, Simple sol(S) \wedge solves problem(S)

Q₉ \exists real num x such that $x > 3 \wedge x^2 \leq 9$

Q₁₀ \exists comp prog such that P compiles without error messages and P isn't correct

Q₁₁ The " \leq " of at least two irrational num is rational
(false)

Q₁₂ The product of some irrational and some rational num is rational
(false)

Q₁₃ There is an integer n such that n^2 is even and n is not even
(false)

Q₁₄ For some real num x_1 and x_2 such that $x_1^2 = x_2^2$ and $x_1 \neq x_2$
(false)

Q₁₅ (a) T (d) T
(b) T (c) F $\rightarrow x = 36$ (counter example)
(c) F \Rightarrow counter example $\Rightarrow x = 16 > 0$
and it's even

Q₁₆ $\exists \mathbb{R} x$ such that $x^2 \geq 1$ and $x \leq 0$

Q₁₇ \exists int d such that $\frac{6}{d}$ is an int and $d \neq 3$

Q₁₈ $\exists x \in \mathbb{R}$ such that $x(x+1) > 0$ and $x \leq 0$ and $x \geq -1$

(نحوه) n is even

Q19 $\exists n \in \mathbb{Z}$ such that n is prime and n isn't odd and $n \neq 2$
سببهای اینجاست

Q20 \exists int a, b & c, a-b is even and b-c is even and a-c isn't even.

Q21 \exists int n, n is divisible by 6 and n isn't div by 2 or n isn't div by 3

Q22 a square of an int is odd and the int isn't odd

Q23 a function is diff & it isn't cont
or There exist at least one function

Q24 (a) $f: C, \text{Children In Tom's Family}(C) \rightarrow \text{female}(C)$
 $g: C, \text{female In Tom's Family}(C) \rightarrow \text{Children}(C)$ } converse

(b) $\forall x \in \text{int}, x > 5 \wedge \text{end with } 1 \text{ or } 3 \text{ or } 7 \text{ or } 9 (x) \rightarrow \text{prime}(x)$
 $\forall x \in \text{int}, x > 5 \wedge \text{prime}(x) \rightarrow \text{end with } 1 \text{ or } 3 \text{ or } 7 \text{ or } 9 (x)$ } converse
من کثیر منطقیه skip

Q25 if $n+1$ is even then n is any prime - - -

(a) $n=1 \Rightarrow n+1=2$ even
but $n=1$ isn't a prime num } نبرد عن الوجود لانز
فشيك لا بينه
(ما اصبحتي بين انواعه)
or $n=9, 9+1=10 \rightarrow$ even
but 9 isn't a prime num

(b) if $2m$ is even then m is any odd int

$2 \times 4 = 8$ even
but $m=4 \Rightarrow$ it's not odd

(c) if 2 circles don't have common center then they intersect in exactly 2 points



Q26 - Q32 skip (easy enochallah)

Q34 a) if n is div by some prime num between 1 and \sqrt{n} strictly then n isn't prime

b) if A and B aren't disjoint then A and B have some elements in common

Q35 skip

Q36 skip

Q37 $\forall x \in \text{int}, (x=1 \wedge \text{SequenceHas}(x) \rightarrow \text{leftOf}(x,0))$

we can't determine since we can't decide whether the premise is true or not

$\neg(\forall x \in \text{int}, (x=1 \wedge \text{SequenceHas}(x) \rightarrow \text{leftOf}(x,0)))$

$\exists x \in \text{int}, (x=1 \wedge \text{SequenceHas}(x) \wedge \neg \text{leftOf}(x,0))$

\hookrightarrow this is false since the sequence doesn't contain 1

\rightarrow the negation is false

Then the statement itself is true.

Q38 $\forall x \in \text{characters}, \text{U occurs In Discrete Mathematics}(x) \rightarrow \text{lowercase}(x)$

$\exists x \in \text{chr}, \text{U occurs}(x) \wedge \neg \text{lowercase}(x)$

\Rightarrow U doesn't occur then the negation is false

Q 39 - Q 48 easy (skip)